#### **Universal laws and architecture 3:**

Constraints on robust efficiency

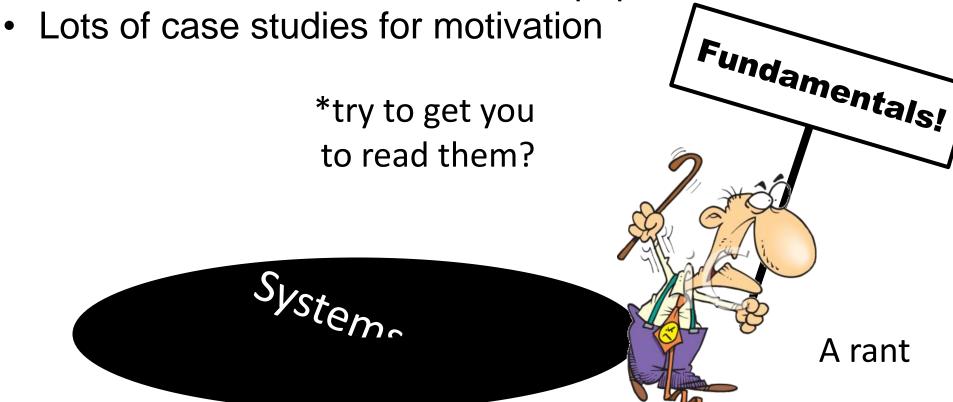
John Doyle
John G Braun Professor
Control and Dynamical Systems, EE, BE
Caltech

#### Outline

- Review Turing, universal laws and architectures
- Compare with cells and brains
- Horizontal gene, app, and meme transfer
- Laws, constraints, tradeoffs
  - phage survival and multiply rate
  - glycolytic oscillations, robust efficiency, and autocatalysis
  - stabilizing an inverted pendulum

#### "Universal laws and architectures?"

- Universal "conservation laws" (constraints)
- Universal architectures (constraints that deconstrain)
- Mention recent papers\*
- Focus on broader context not in papers



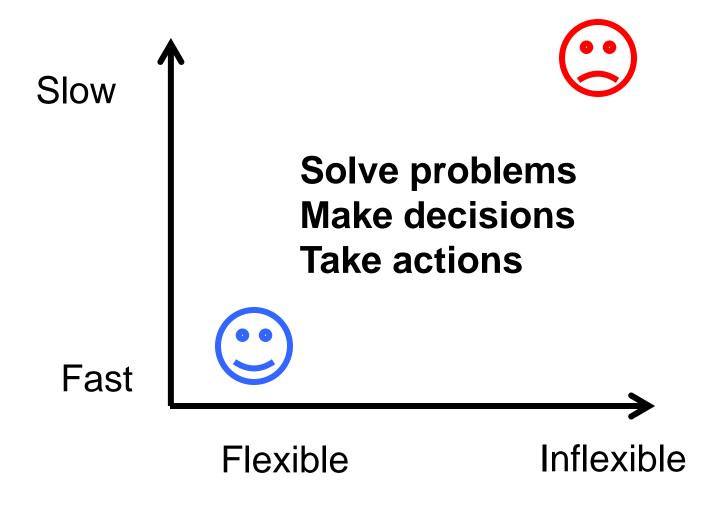
- Turing 100<sup>th</sup> birthday in 2012
- Turing
  - machine (math, CS)
  - test (AI, neuroscience)
  - pattern (biology)
- Arguably greatest\*
  - all time math/engineering combination
  - WW2 hero
  - "invented" software

**Turing (1912-1954)** 

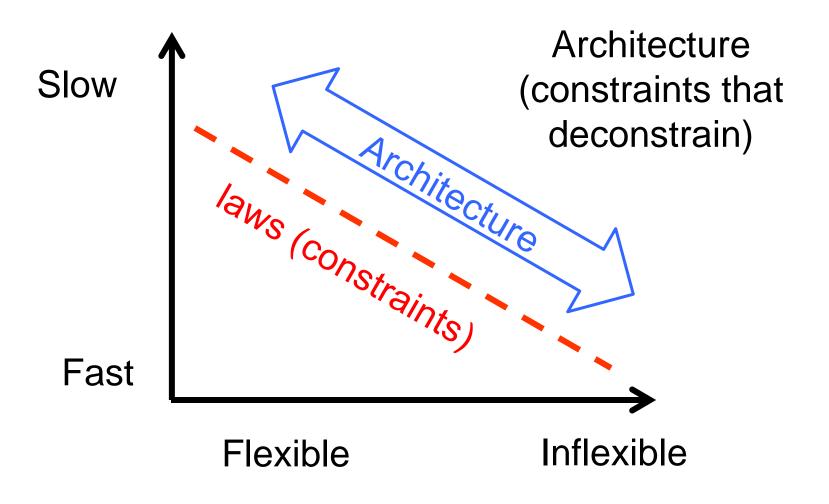
#### Key papers/results

- Theory (1936): Turing machine (TM), computability, (un)decidability, universal machine (UTM)
- Practical design (early 1940s): code-breaking, including the design of code-breaking machines
- Practical design (late 1940s): general purpose digital computers and software, layered architecture
- Theory (1950): Turing test for machine intelligence
- Theory (1952): Reaction diffusion model of morphogenesis, plus practical use of digital computers to simulate biochemical reactions

#### **Fast and flexible**



#### **Laws and architectures**

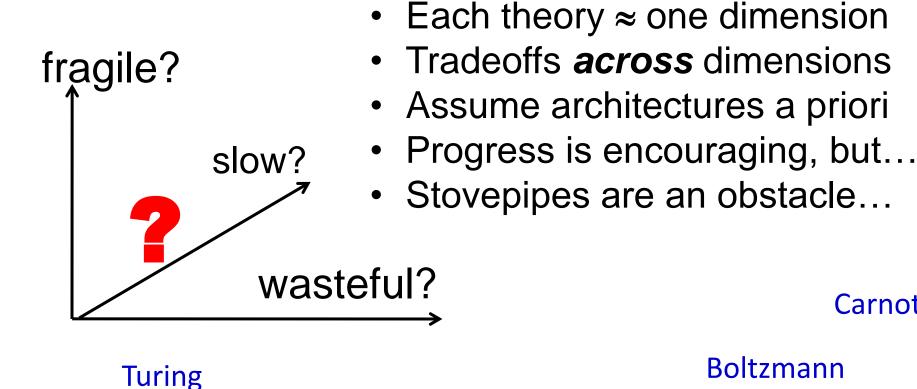


Control

Compute

Comms

Shannon Bode



Godel

Einstein

Heisenberg

**Physics** 

Carnot

#### **Compute**

**Turing** 

Delay is most important

Bode

Control, OR

#### **Communicate**

**Shannon** 

Delay is least important

Carnot

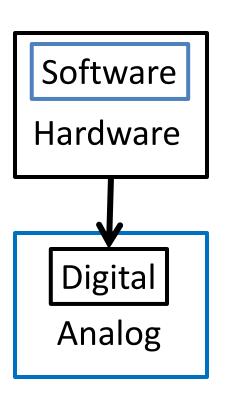
**Boltzmann** 

Heisenberg

**Physics** 

Einstein

Turing as
"new"
starting
point?



#### Compute

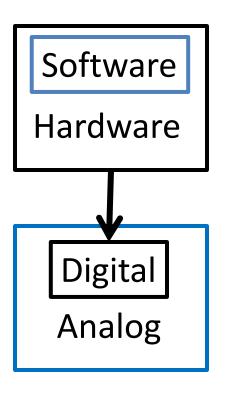
**Turing** 

Delay is most important

**Bode** 

Control, OR

Turing as "new" starting point?



#### **Essentials:**

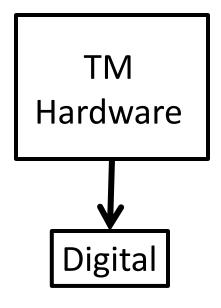
- 0. Model
- 1. Universal laws
- 2. Universal architecture
- 3. Practical implementation

#### Turing's 3 step research:

- 0. Virtual (TM) machines
- hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)

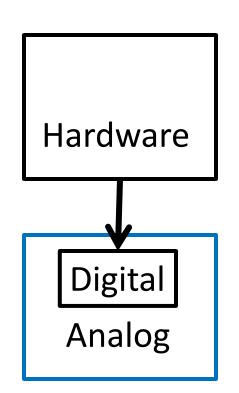
#### **Essentials:**

- 0. Model
- Universal laws
- 2. Universal architecture
- 3. Practical implementation



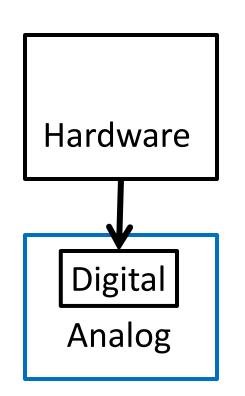
#### Turing's 3 step research:

- 0. Virtual (TM) machines
  - hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)



- ...being digital should be of greater interest than that of being electronic. That it is electronic is certainly important because these machines owe their high speed to this... But this is virtually all that there is to be said on that subject.
- That the machine is digital however has more subtle significance. ... One can therefore work to any desired degree of accuracy.

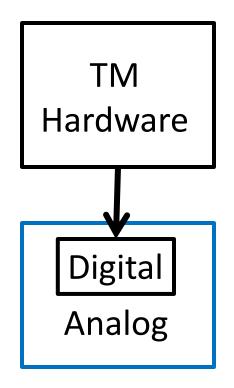
1947 Lecture to LMS



- ... digital ... of greater interest than that of being electronic ...
- ...any desired degree of accuracy...
- This accuracy is not obtained by more careful machining of parts, control of temperature variations, and such means, but by a slight increase in the amount of equipment in the machine.

1947 Lecture to LMS

- Digital more important than electronic...
- Robustness: accuracy and repeatability.
- Achieved more by internal hidden complexity than precise components or environments.



Turing Machine (TM)

- Digital
- Symbolic
- Logical
- Repeatable

## avalanche The butterfly effect

• ... quite small errors in the initial conditions can have an overwhelming effect at a later time. The displacement of a single electron by a billionth of a centimetre at one moment might make the difference between a man being killed by an avalanche a year later, or escaping.

1950, Computing Machinery and Intelligence, *Mind* 

- ... quite small errors in the initial conditions can have an overwhelming effect at a later time....
- It is an essential property of the mechanical systems which we have called 'discrete state machines' that this phenomenon does not occur.
- Even when we consider the actual physical machines instead of the idealised machines, reasonably accurate knowledge of the state at one moment yields reasonably accurate knowledge any number of steps later.

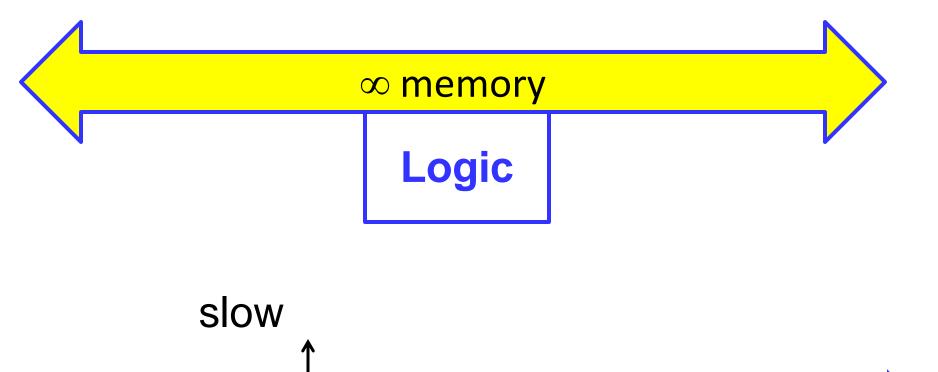
1950, Computing Machinery and Intelligence, Mind

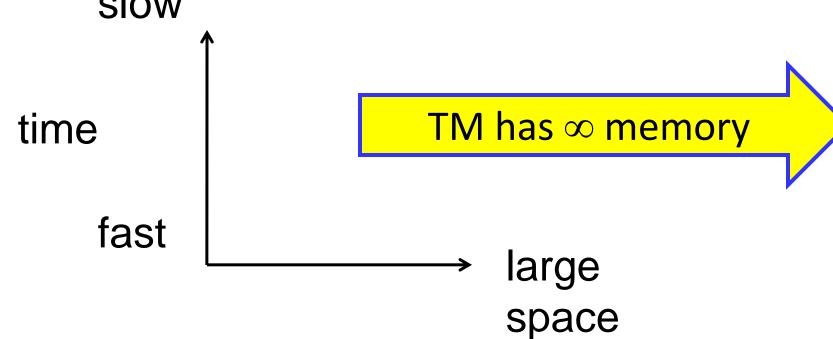
#### 

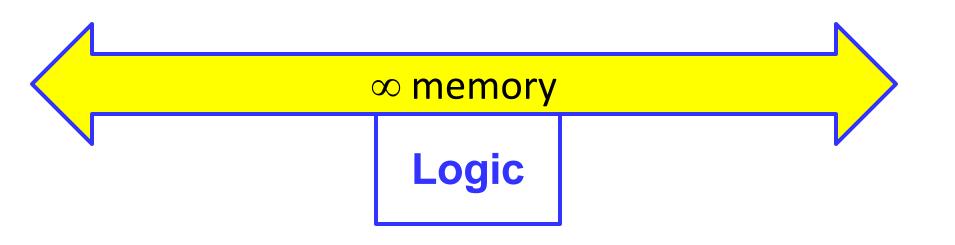
#### Logic

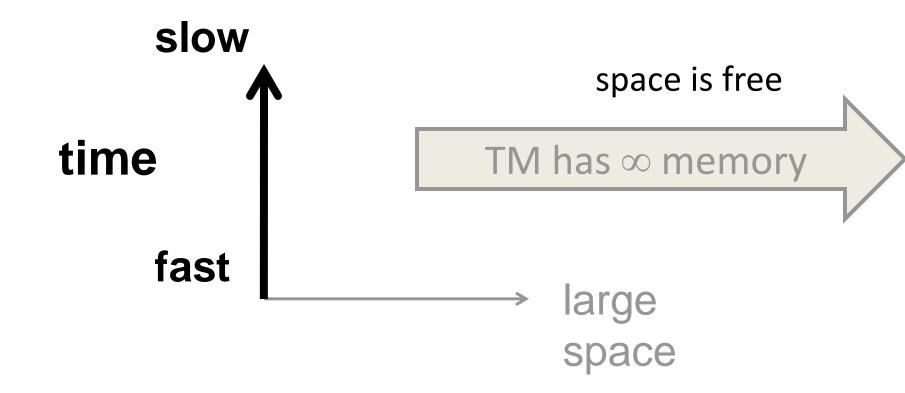
TM Hardware Turing's 3 step research:

- 0. Virtual (TM) machines
- 1. hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)









#### <mark>∞ memory</mark>

Logic

#### time?

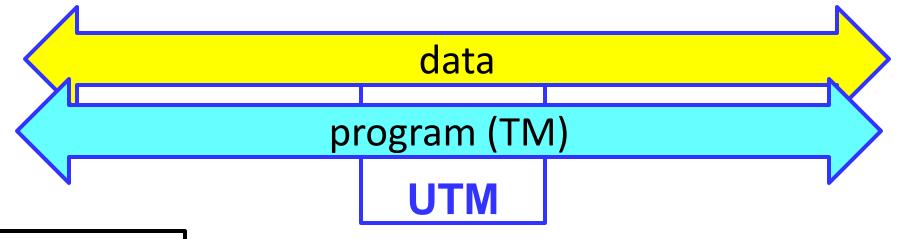
**Decidable problem** = ∃ algorithm that solves it

Most naively posed problems are undecidable.

# program (TM) UTM

Turing's 3 step research:

- 0. Virtual (TM) machines
- 1. hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)



Software Hardware

### 2. Universal architecture achieving hard limits (UTM)

- Software: A Turing machine (TM) can be data for another Turing machine
- A Universal Turing Machine can run any TM
- A UTM is a virtual machine.
- There are lots of UTMs, differ only (but greatly) in speed and programmability (space assumed free)

## TM program HALT UTM

The halting problem

- Given a TM (i.e. a computer program)
- Does it halt (or run forever)?
- Or do more or less anything in particular.
- Undecidable! There does not exist a special TM that can tell if any other TM halts.
- i.e. the program HALT does not exist. 🕾

Thm: TM H=HALT does not exist.

That is, there does not exist a program like this:

$$H(TM,input) \triangleq \begin{cases} 1 \text{ if } TM(input) \text{ halts} \\ 0 \text{ otherwise} \end{cases}$$

**Proof** is by contradiction. Sorry, don't know any alternative. And Turing is a god.

$$H(TM, input) \triangleq \begin{cases} 1 \text{ if } TM(input) \text{ halts} \\ 0 \text{ otherwise} \end{cases}$$

Thm: No such H exists.

**Proof**: Suppose it does. Then define 2 more programs:

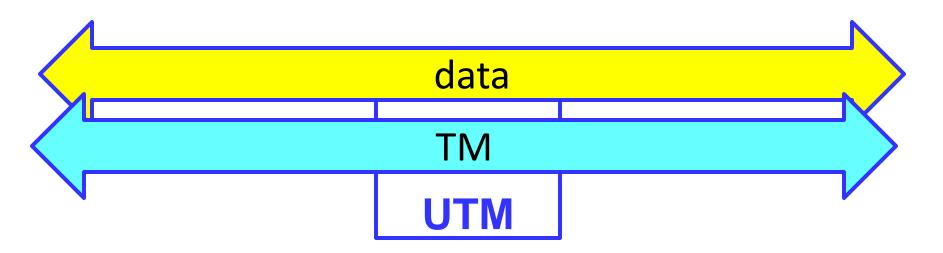
$$H'(TM,input) \triangleq \begin{cases} 1 \text{ if } H(TM,input) = 0 \\ \text{loop forever otherwise} \end{cases}$$

$$H*(TM) \triangleq H'(TM,TM)$$

$$Run \ H*(H*) = H'(H*,H*)$$

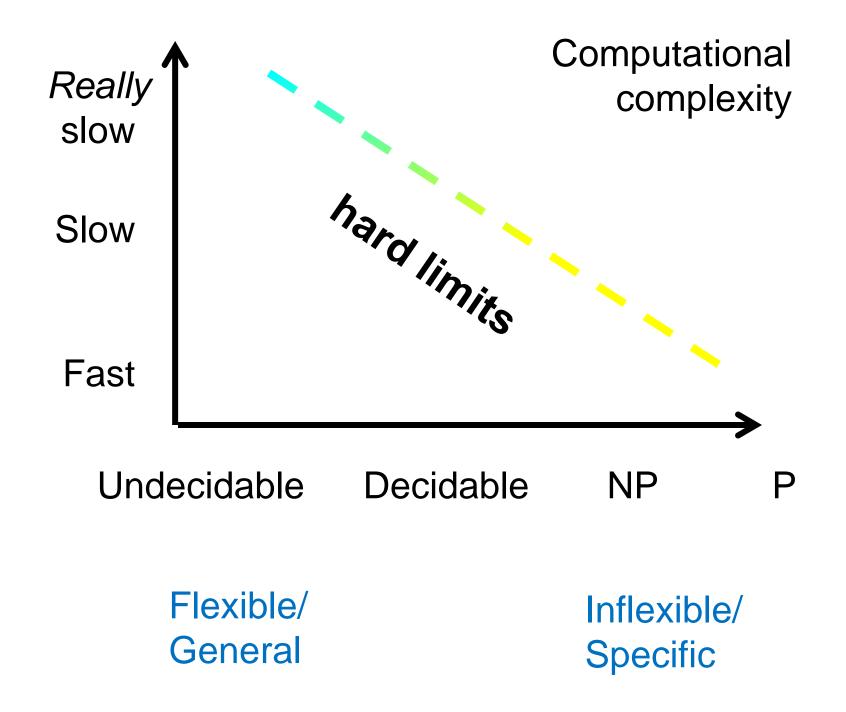
$$= \begin{cases} \text{halt if } H*(H*) \text{ loops forever} \\ \text{loop forever otherwise} \end{cases}$$

#### **Contradiction!**

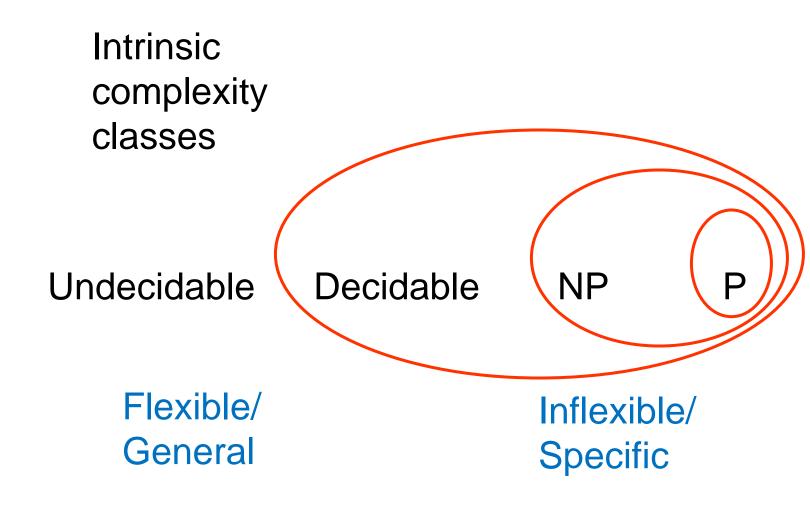


#### **Implications**

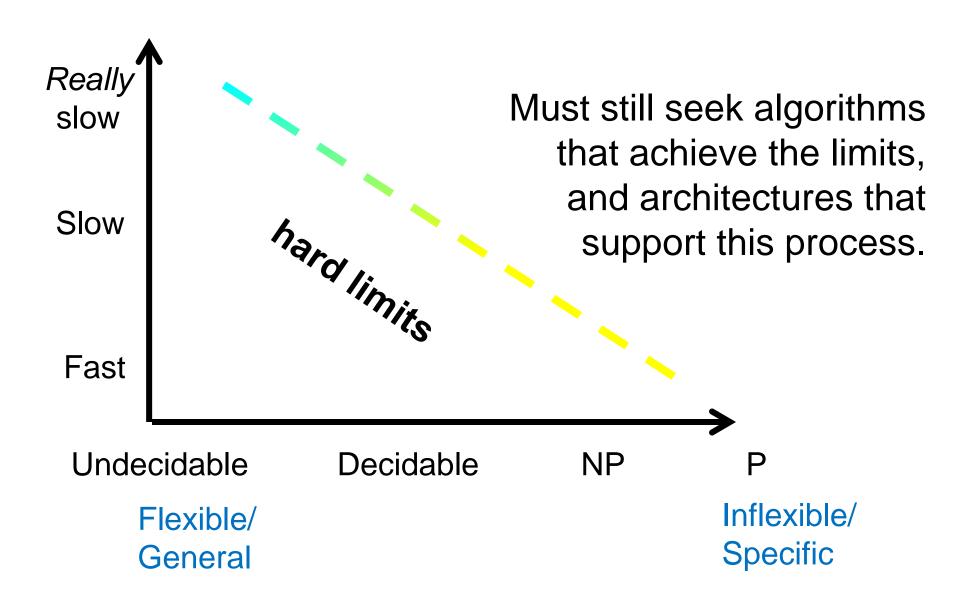
- TMs and UTMs are perfectly repeatable
- But perfectly unpredictable
- Undecidable: Will a TM halt? Is a TM a UTM? Does a TM do X (for almost any X)?
- Easy to make UTMs, but hard to recognize them.
- Is anything decidable? Yes, many questions NOT about TMs.
- Large, thin, nonconvex everywhere...



### Computational complexity



These are hard limits on the *intrinsic* computational complexity of *problems*.



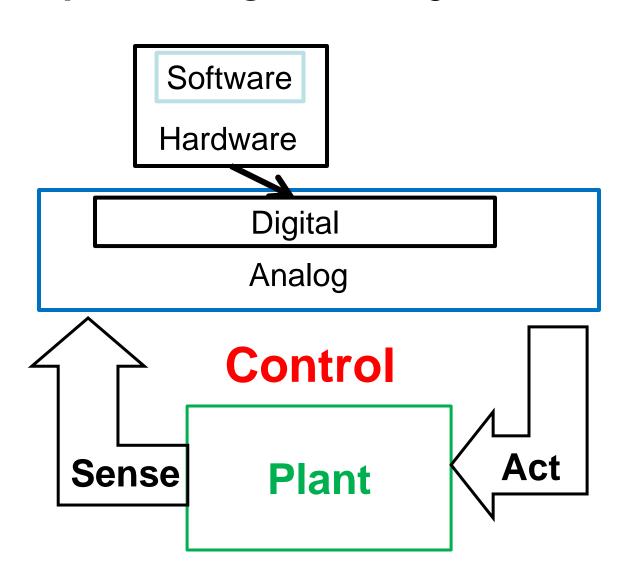
#### Compute

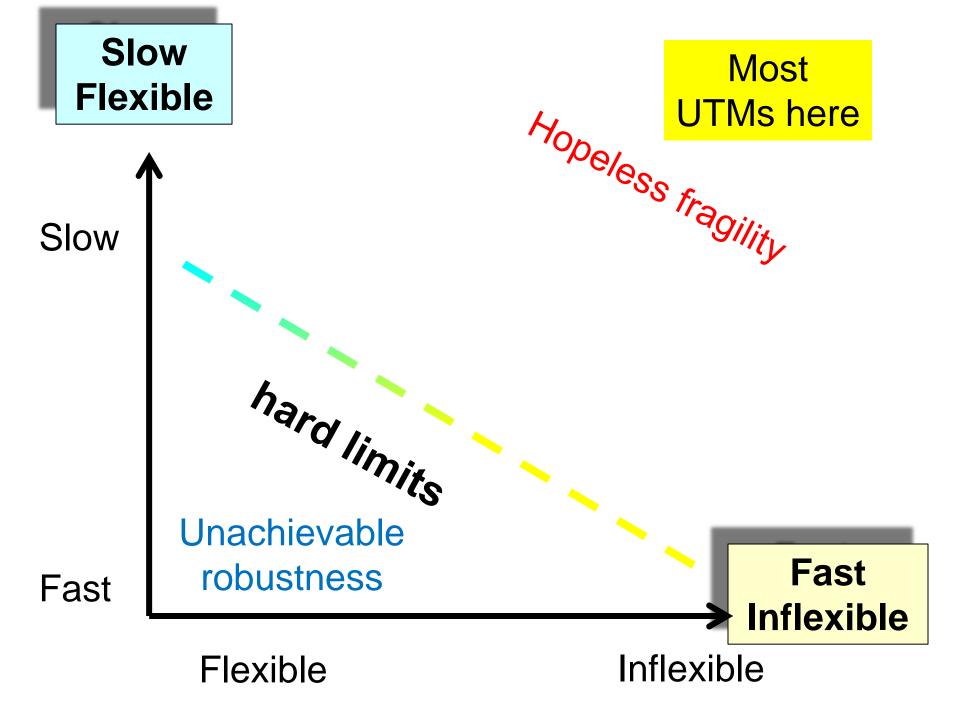
Computational complexity of

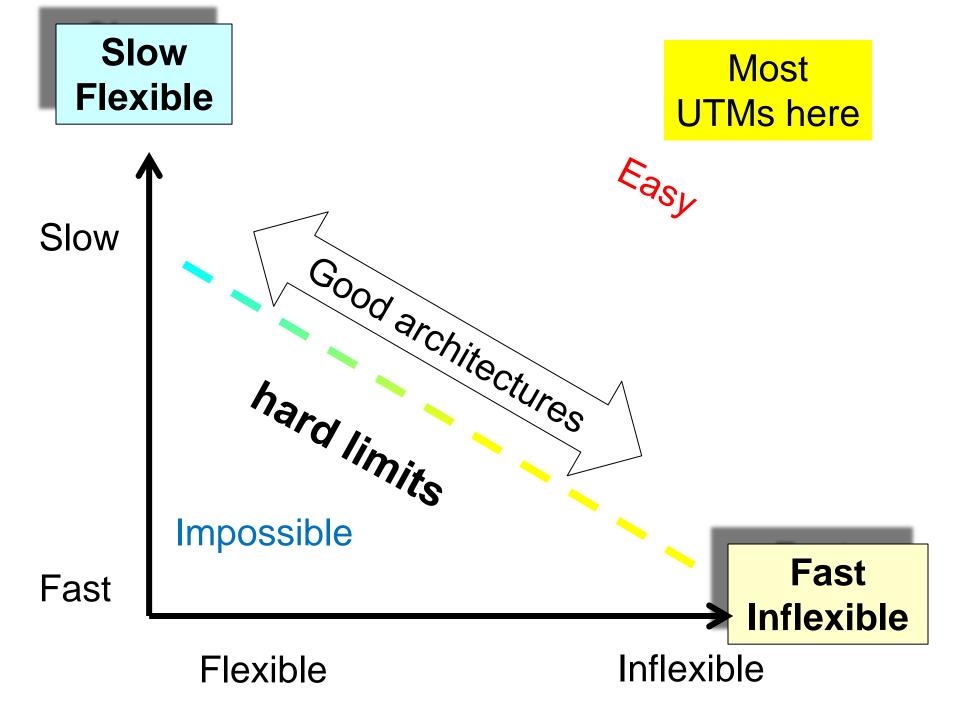
- Designing control algorithms
- Implementing control algorithms

Delay is even more important in control

**Control** 







#### Issues for engineering

- Turing remarkably relevant for 76 years
- UTMs are ≈ implementable
  - Differ only (but greatly) in speed and programmability
  - Time/speed/delay is most critical resource
  - Space (memory) almost free for most purposes
- Read/write random access memory hierarchies
- Further gradations of decidable (P/NP/coNP)

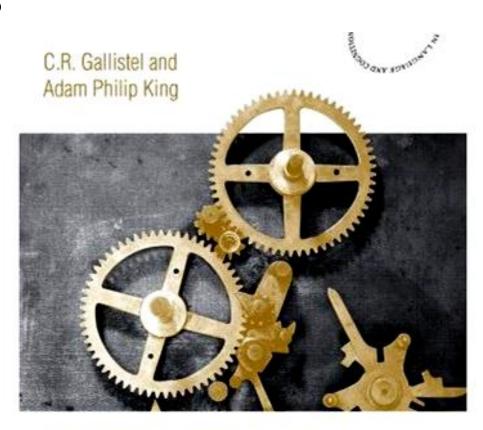
#### Most crucial:

- UTMs differ vastly in speed, usability, and programmability
- You can fix bugs but it is hard to automate finding/avoiding them

#### Issues for neuroscience

- Brains and UTMs?
  - Time is most critical resource?
  - Space (memory) almost free?
- Read/write random access memory hierarchies?
- Brain >> UTM?

#### Gallistel and King



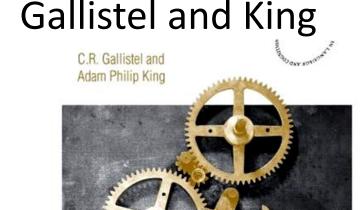
#### Memory and the Computational Brain

Why Cognitive Science Will Transform Neuroscience

WILEY-BLACKWELL

#### Conjecture

- Memory potential ≈ ∞
- Examples
  - Insects
  - Scrub jays
  - Autistic Savants





- But why so rare and/or accidental?
- Large memory, computation of limited value?
- Selection favors fast robust action?

# **Compute**

**Turing** 

Delay is most important

Bode

Control, OR

# **Communicate**

**Shannon** 

Delay is least important

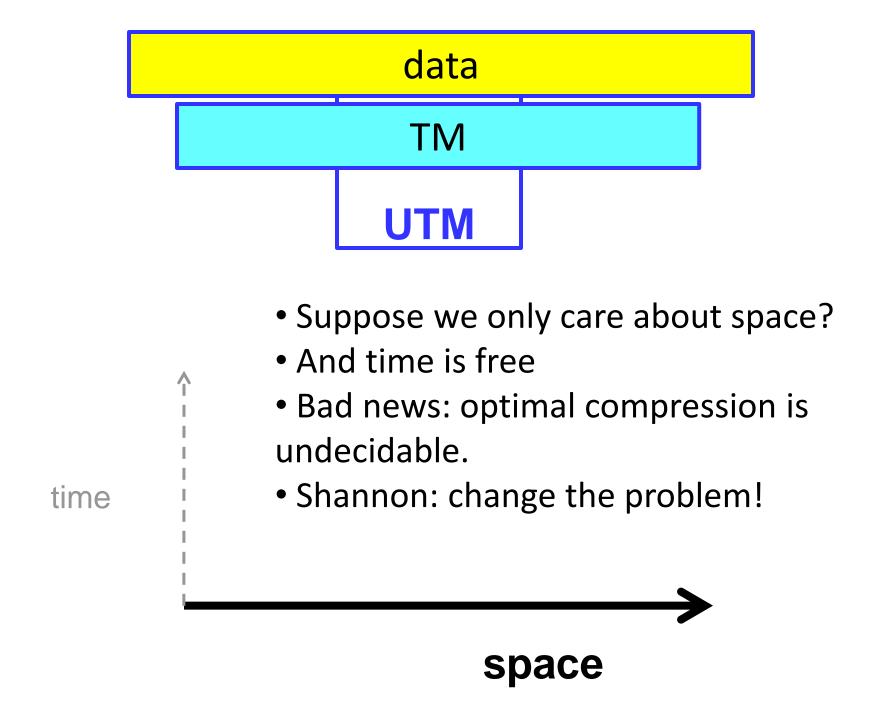
Carnot

**Boltzmann** 

Heisenberg

**Physics** 

Einstein



# **Communications**

## Shannon's brilliant insight

#### **Shannon**

- Forget time
- Forget files, use *infinite random ensembles*

#### **Good news**

- Laws and architecture!
- Info theory most popular and accessible topic in systems engineering
- Fantastic for some engineering problems

# **Communications**

## Shannon's brilliant insight

#### **Shannon**

- Forget time
- Forget files, use infinite random ensembles

#### **Bad** news

Laws and architecture very brittle

- Less than zero impact on internet architecture
- Almost useless for biology (But see Lestas et al, 2010)
- Misled, distracted generations of biologists (and neuroscientists)

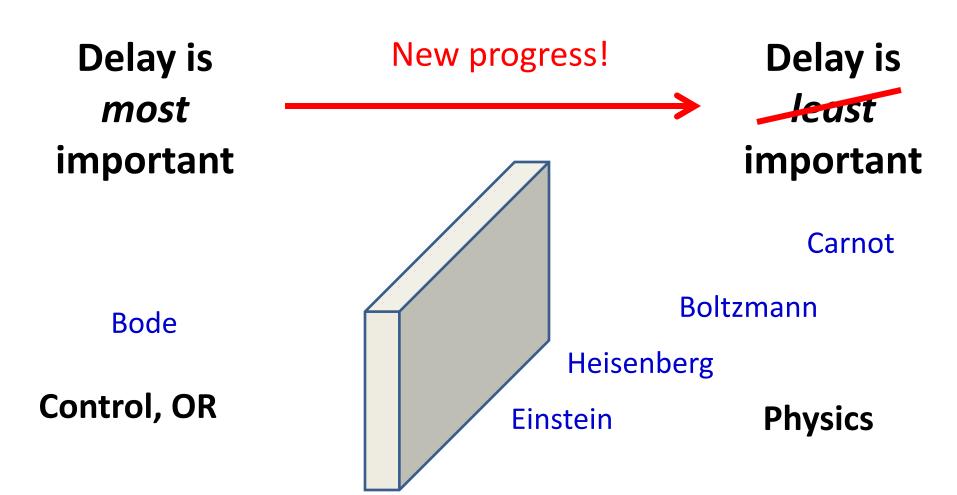
# **Compute**

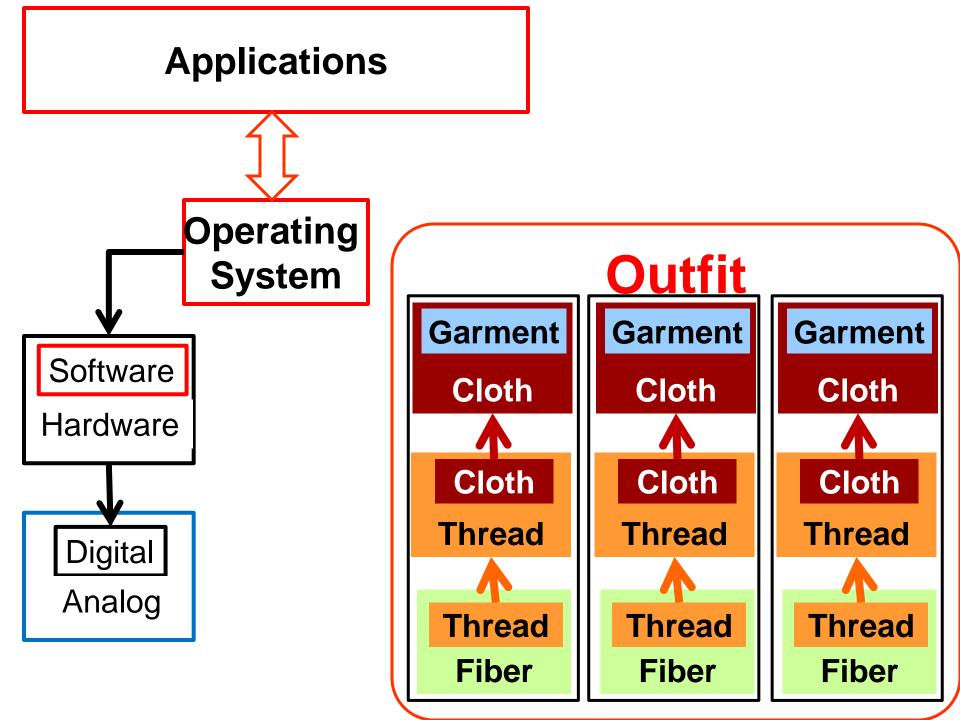
**Communicate** 

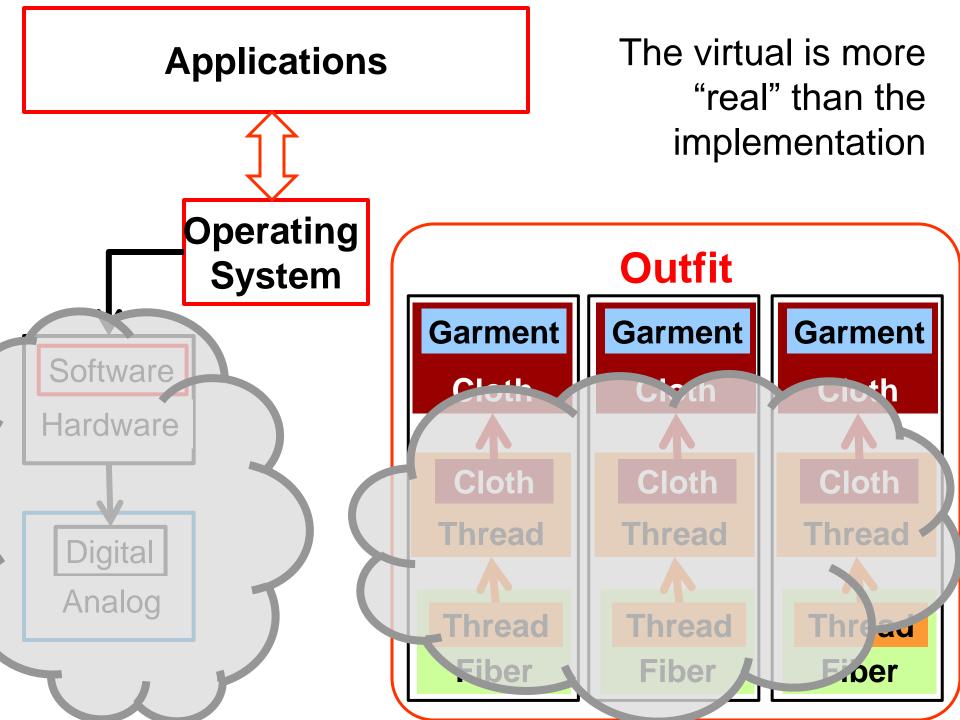
**Turing** 

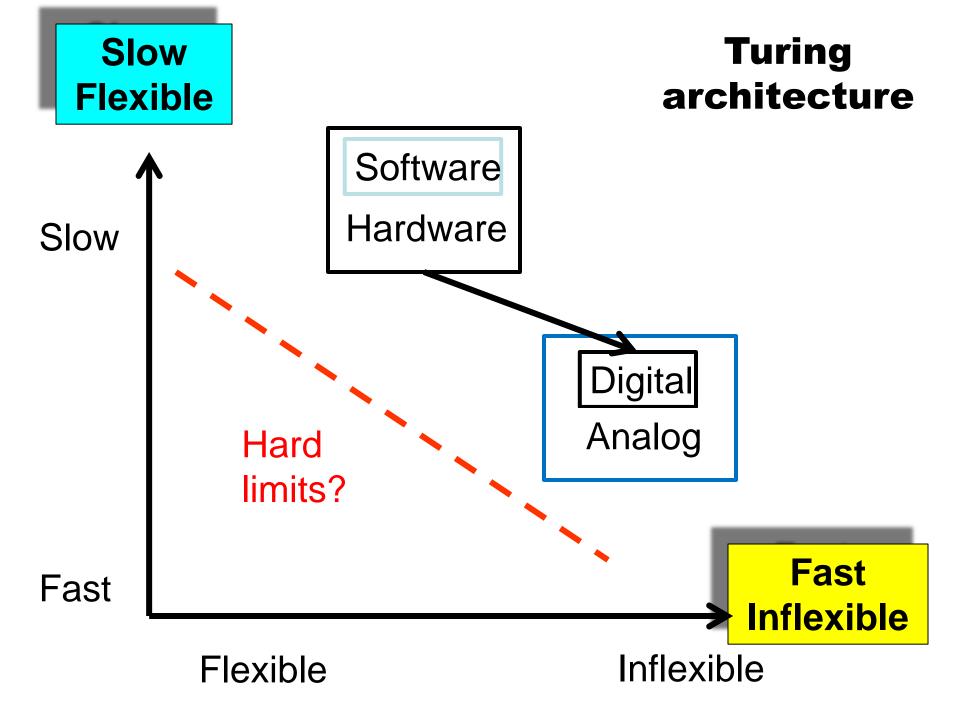
Lowering the barrier

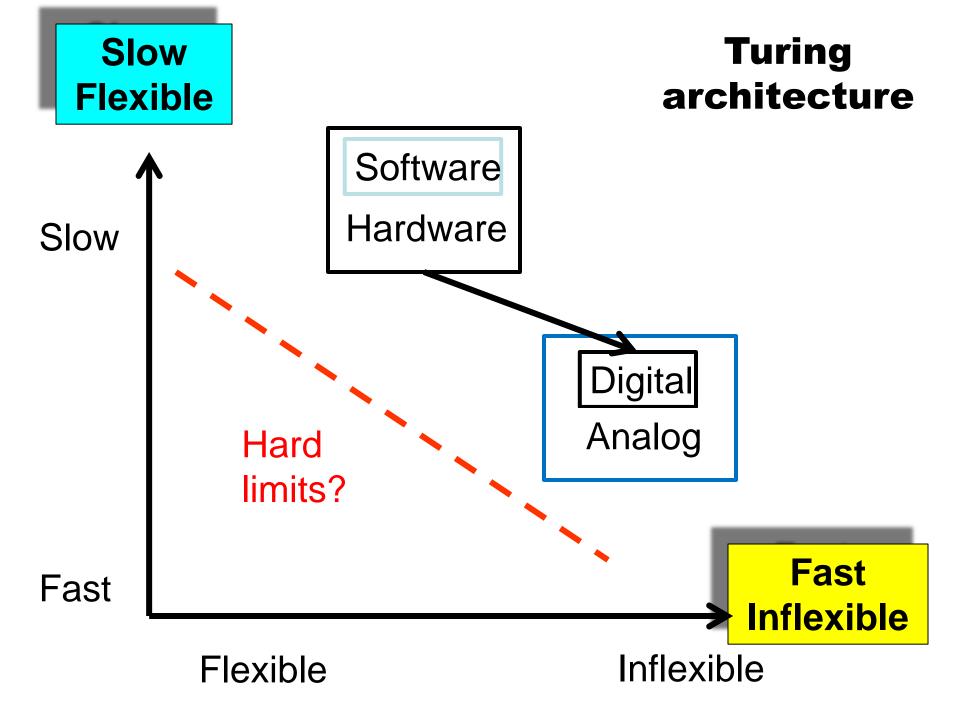
Shannon

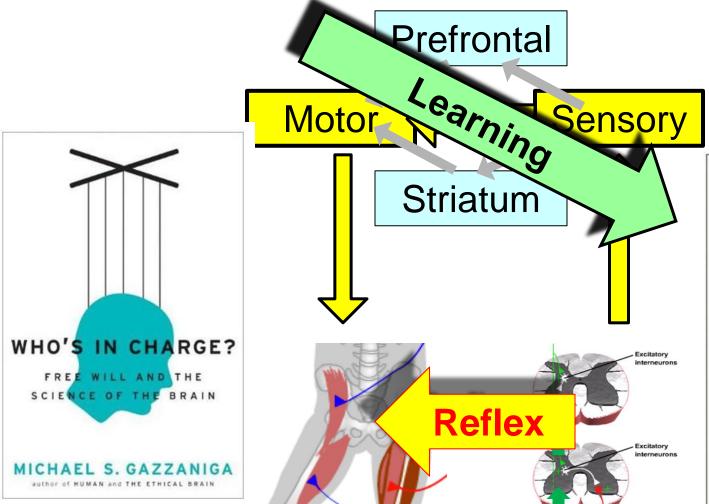


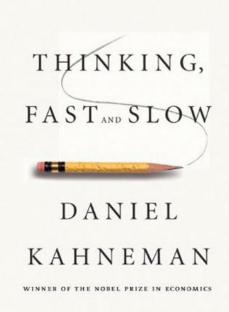




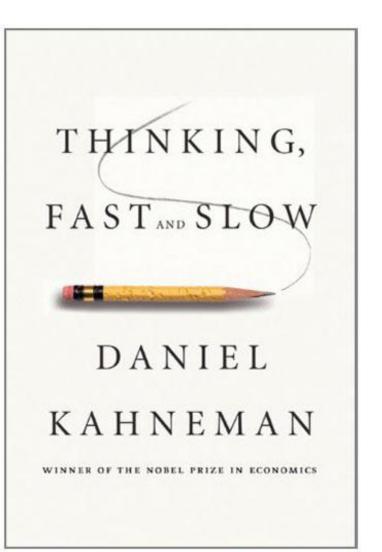








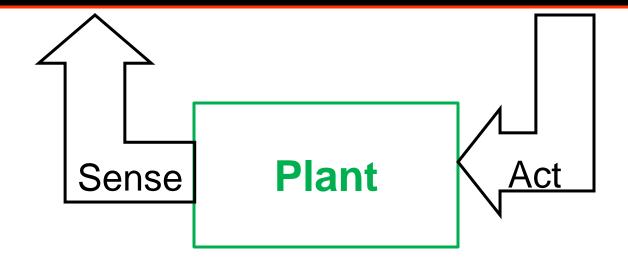
# **Essentials To Do**



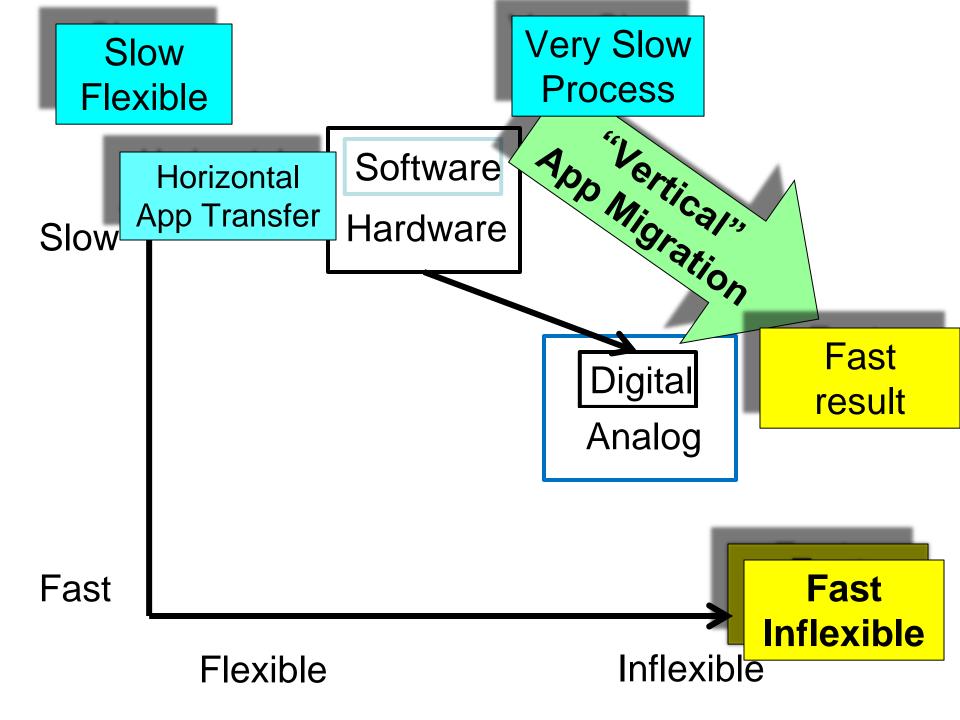
- Reyna/Brainerd: Gist, false memory
- Ashby: Automaticity, multiple memory systems,...
- Cosmides/Tooby: Risk, uncertainty, cooperation, evolution,...

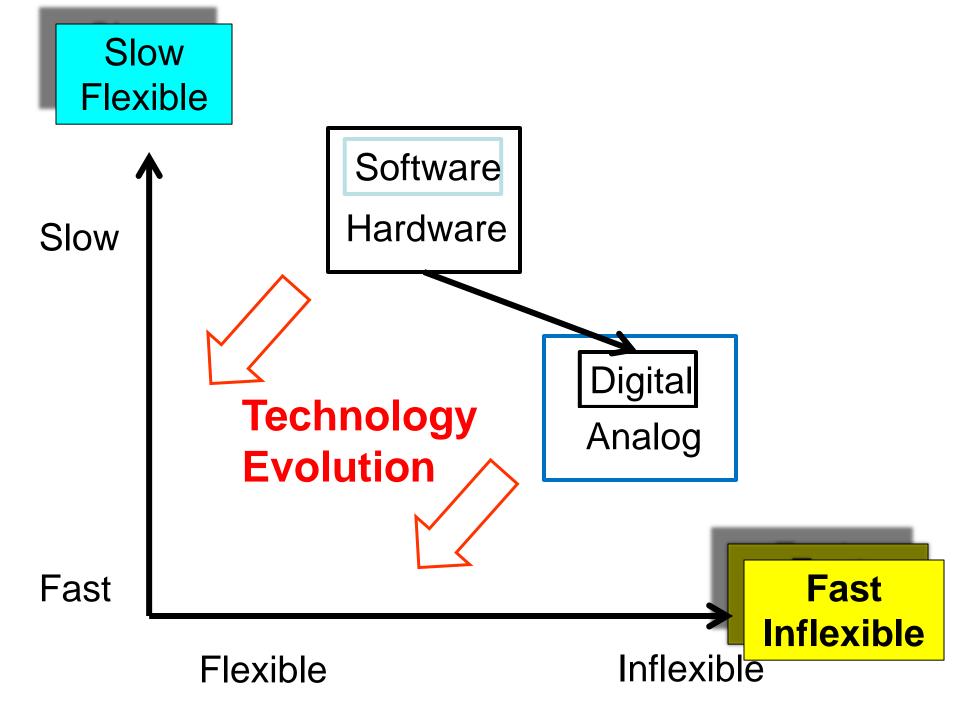
Wolpert, Grafton, etc

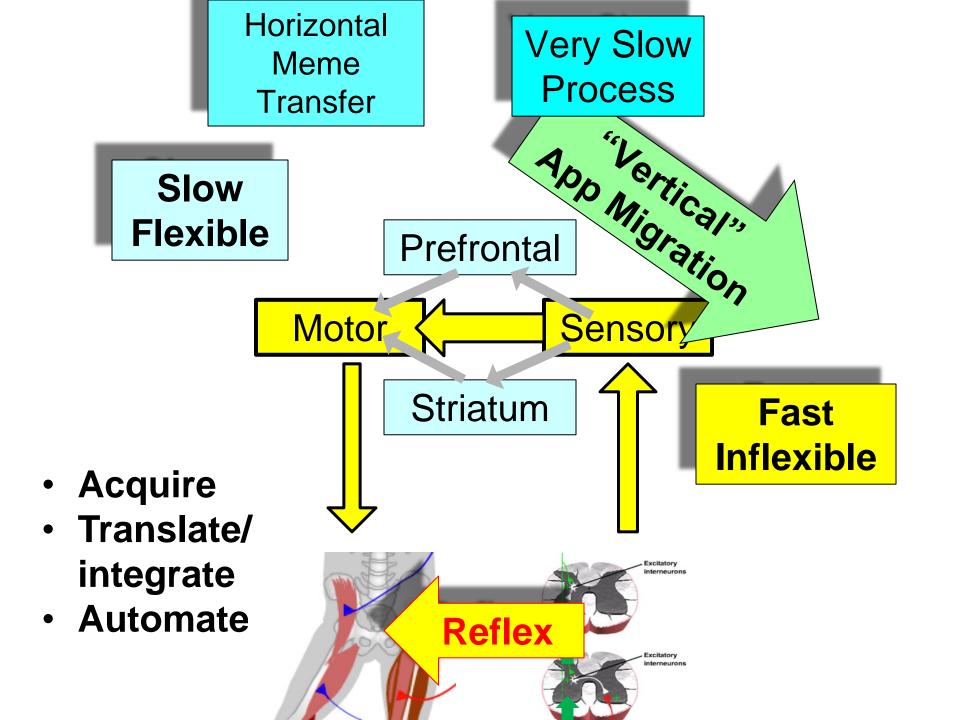
Brain as optimal controller

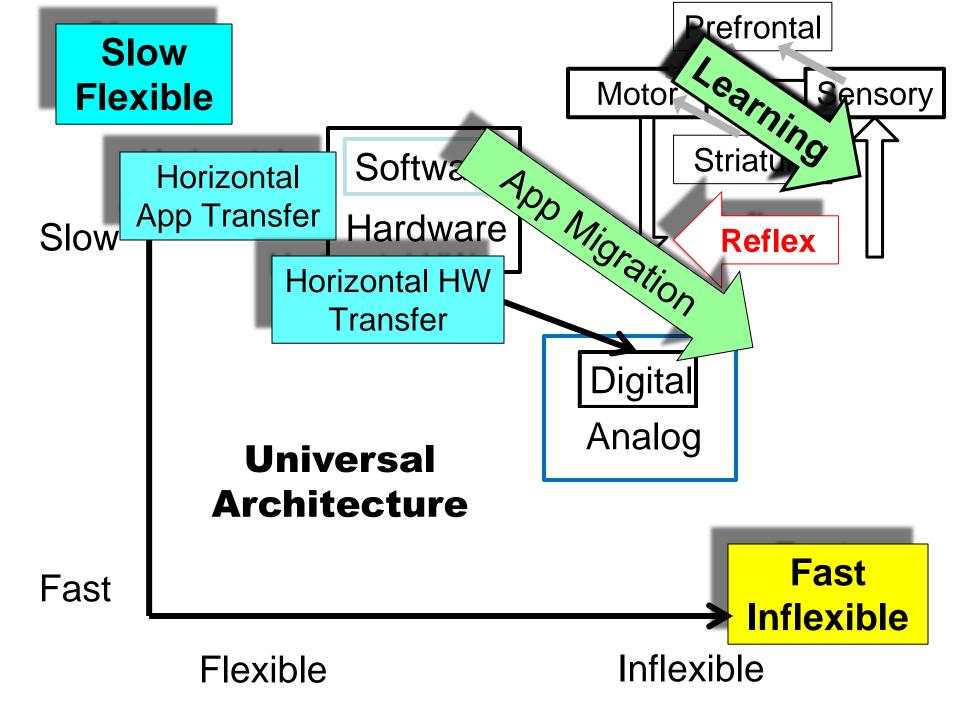


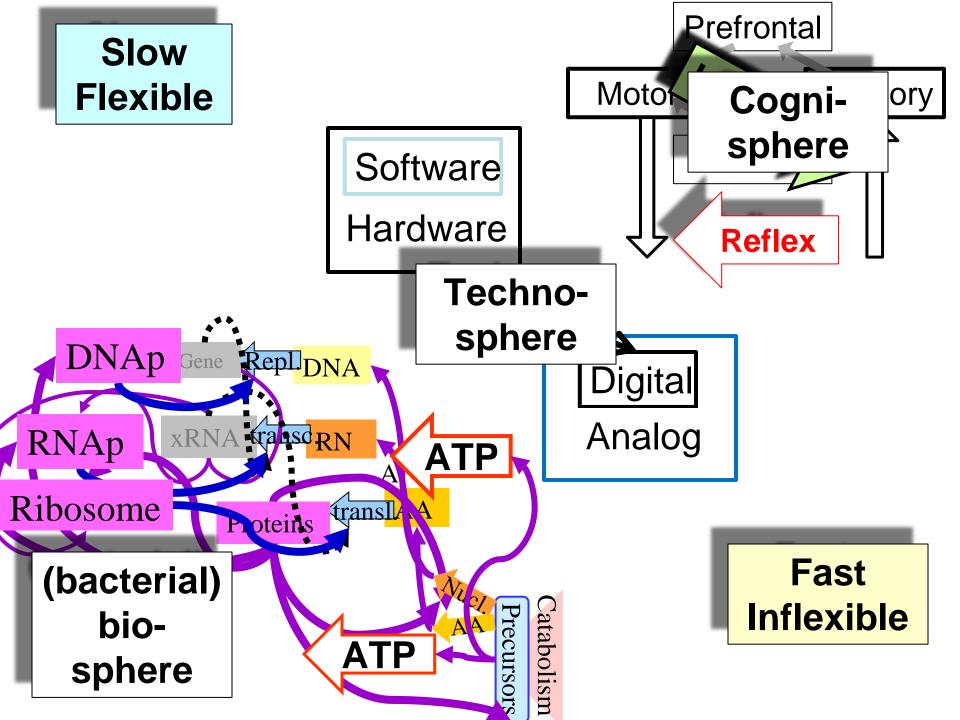
Speed and flexibility are crucial to implementing robust controllers.

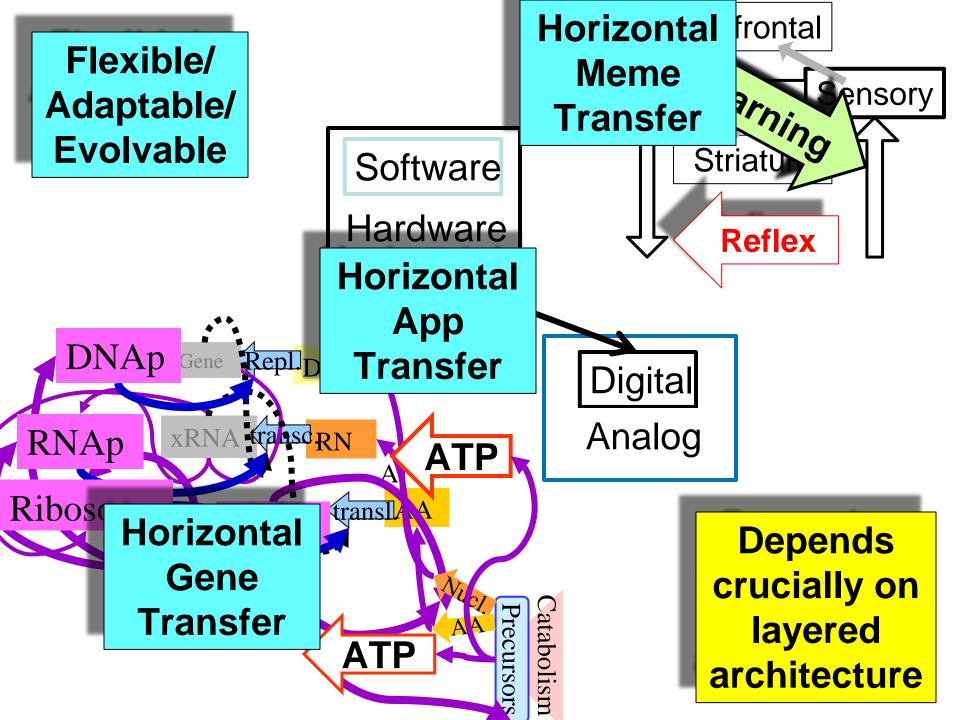












Horizontal Meme Transfer

Horizontal App Transfer

# Horizontal Gene Transfer

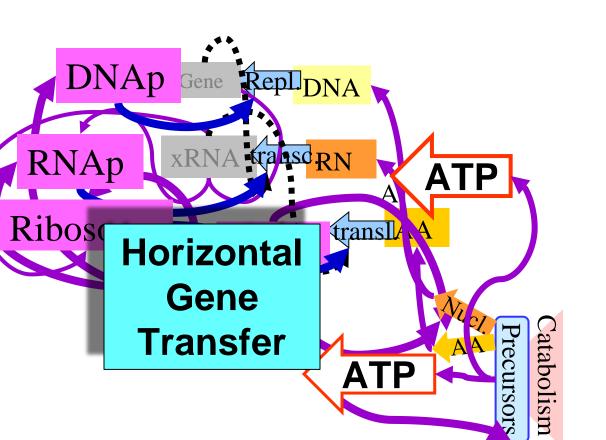
#### Most

- software and hardware
- new ideas (humans)
- new genes (bacteria)

is acquired by "horizontal" transfer, though sometimes it is evolved locally

# Sequence ~100 E Coli (not chosen randomly)

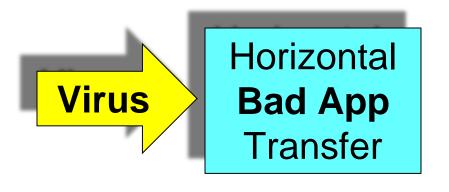
- ~ 4K genes per cell
- ~20K different genes in total
- ~ 1K universally shared genes



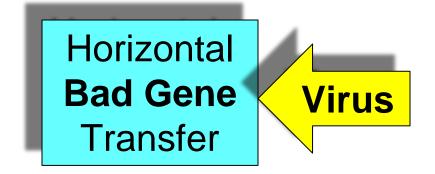
See slides on bacterial biosphere

Exploiting layered architecture

Horizontal **Bad Meme**Transfer



**Fragility?** 



Parasites & Hijacking

Depends crucially on layered architecture

# Build on Turing to show what is *necessary* to make this work.

Horizontal Meme Transfer

- Acquire
- Translate/ integrate
- Automate

Horizontal Gene Transfer Horizontal
App
Transfer

Amazingly Flexible/ Adaptable

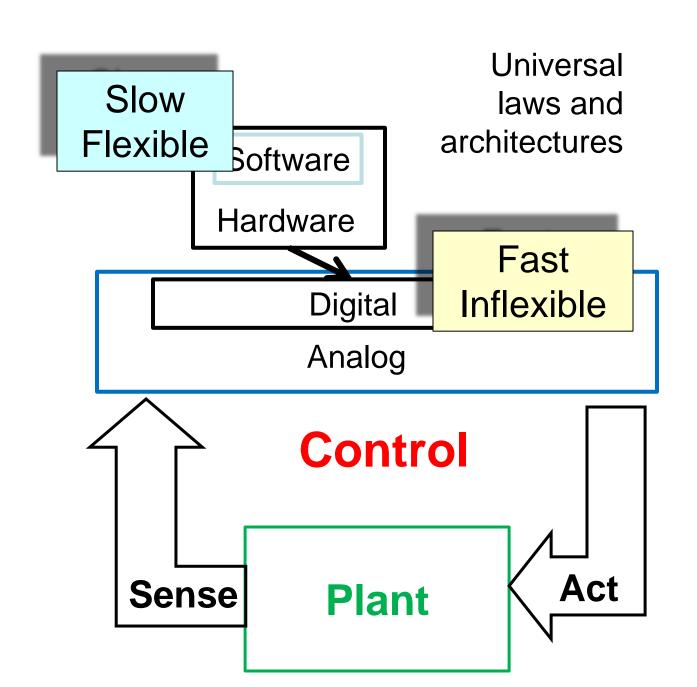
# Compute

**Turing** 

Delay is even more important

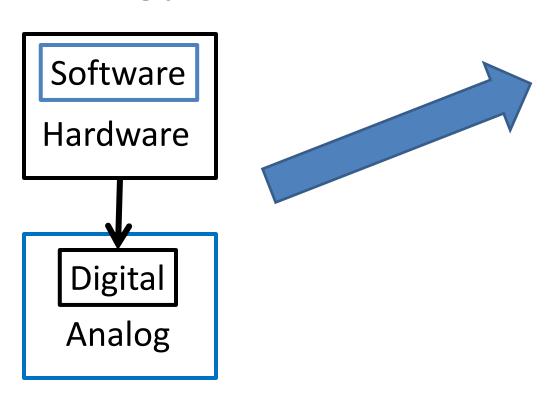
**Bode** 

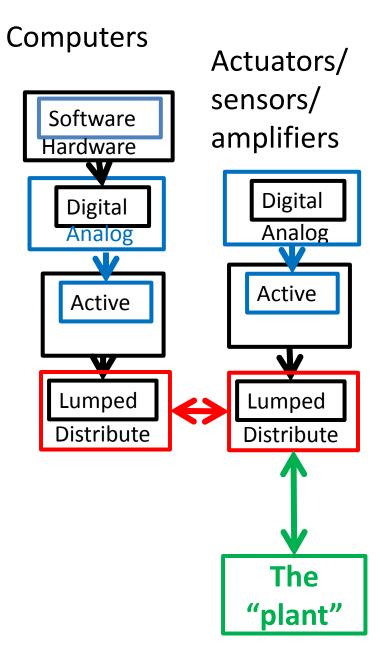
**Control** 



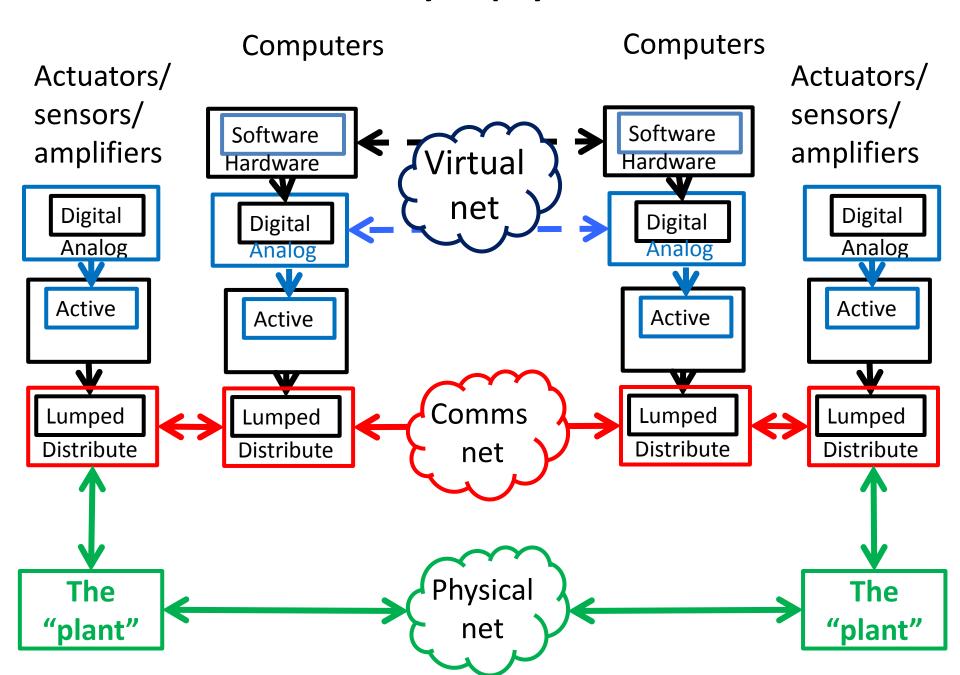
## Cyberphysical

# **Starting point**





## Cyberphysical

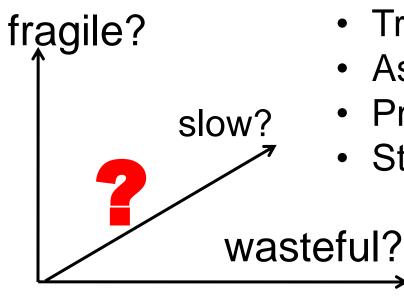


Control

**Comms** 

Shannon

Bode



- Each theory ≈ one dimension
- Tradeoffs across dimensions
- Assume architectures a priori
- Progress is encouraging, but...
- Stovepipes are an obstacle...

Carnot

**Boltzmann** 

Heisenberg

Einstein

**Physics** 

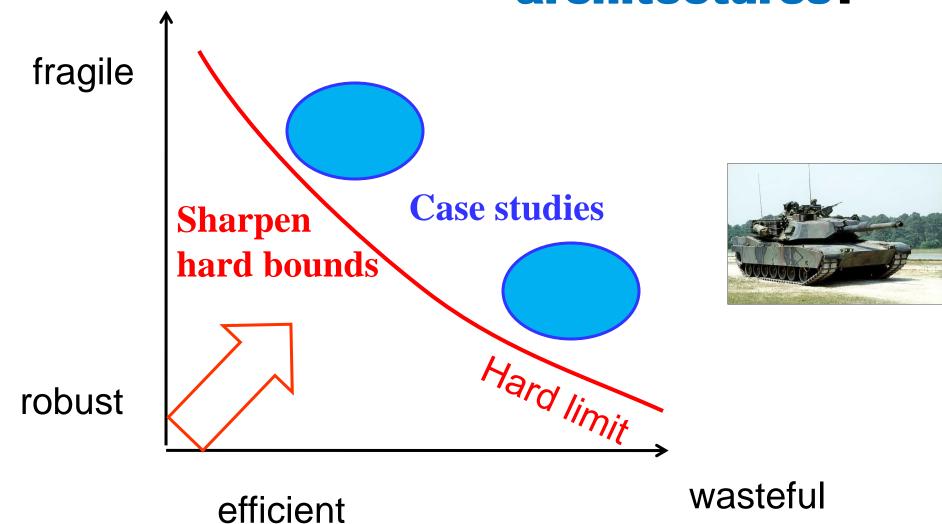
**Compute** 

**Turing** 

Godel



# laws and architectures?



# Viruses' Life History: Towards a Mechanistic Basis of a Trade-Off between Survival and Reproduction among Phages

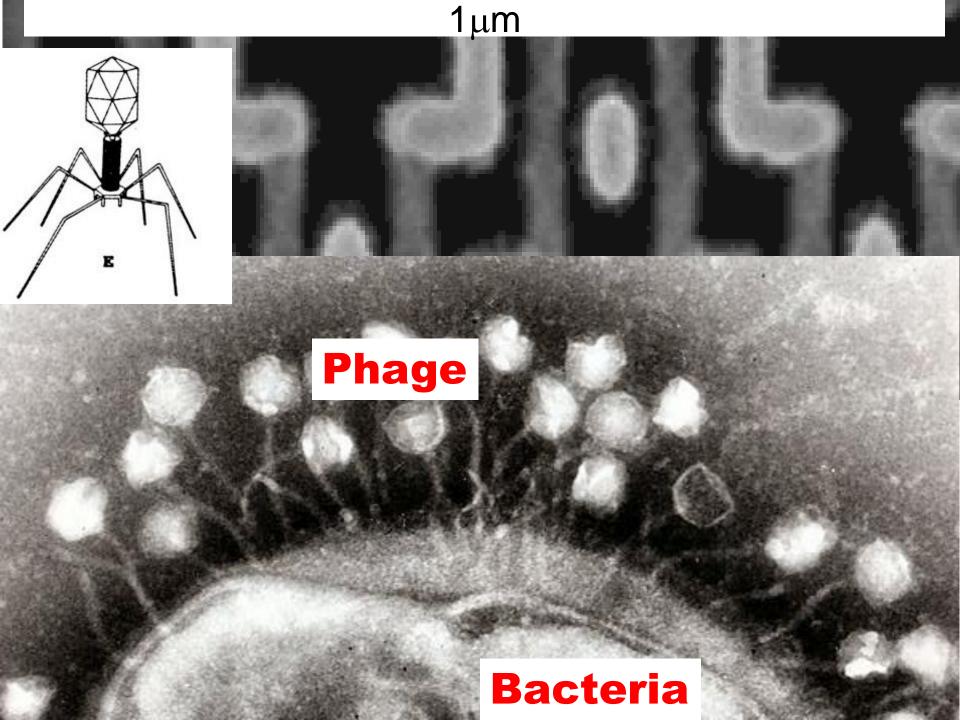
Marianne De Paepe, François Taddei\*

Laboratoire de Genetique Moleculaire, Evolutive et Medicale, University of Paris 5, INSERM, Paris, France

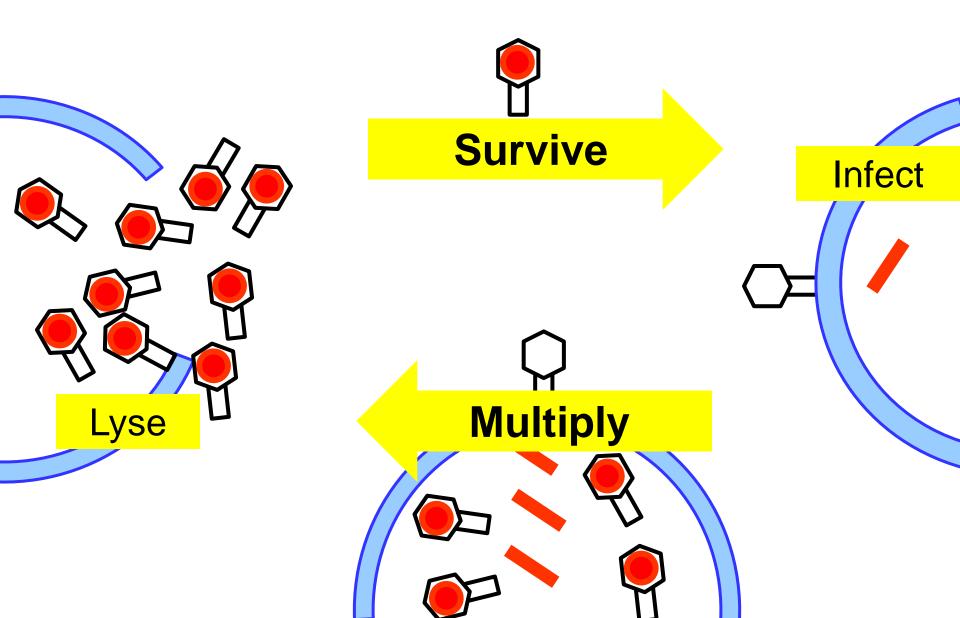
#### Marianne De Paepe, François Taddei®

Laboratoire de Genetique Moleculaire, Evolutive et Medicale, University of Paris 5, INSERM, Paris, France

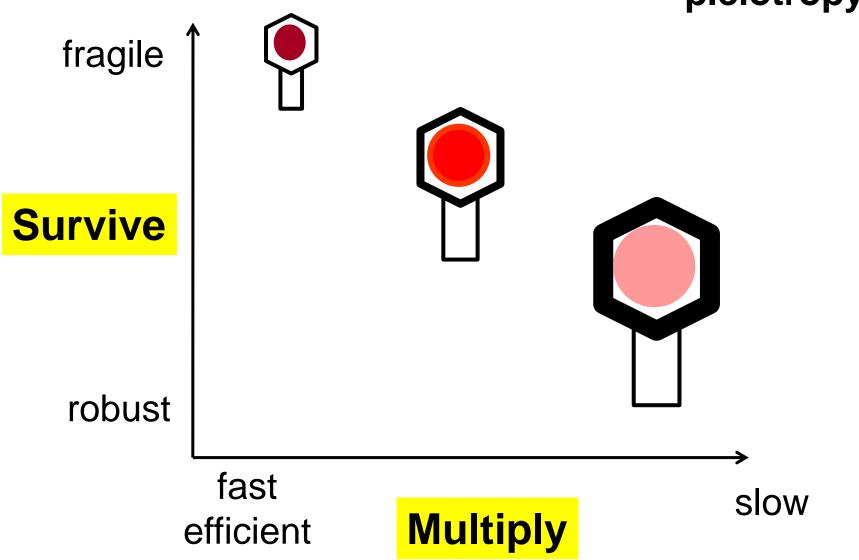
July 2006 | Volume 4 | Issue 7 | e193

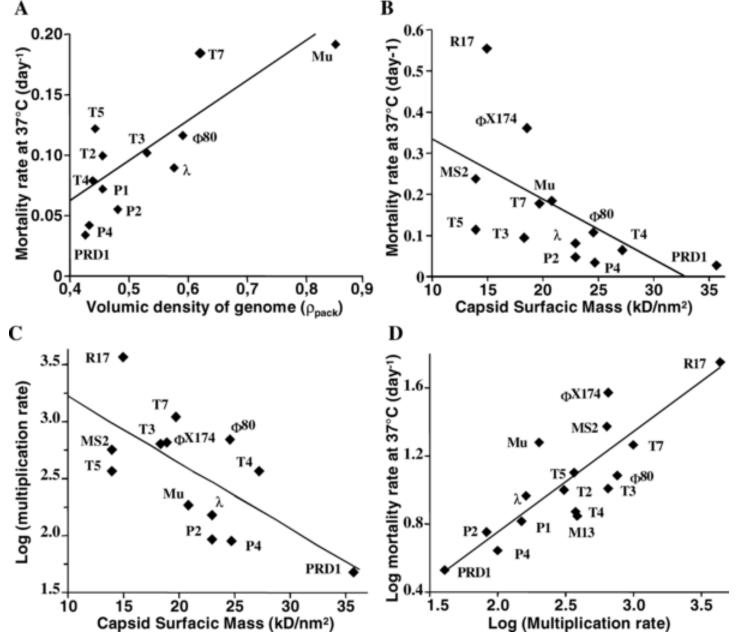


# Phage lifecycle

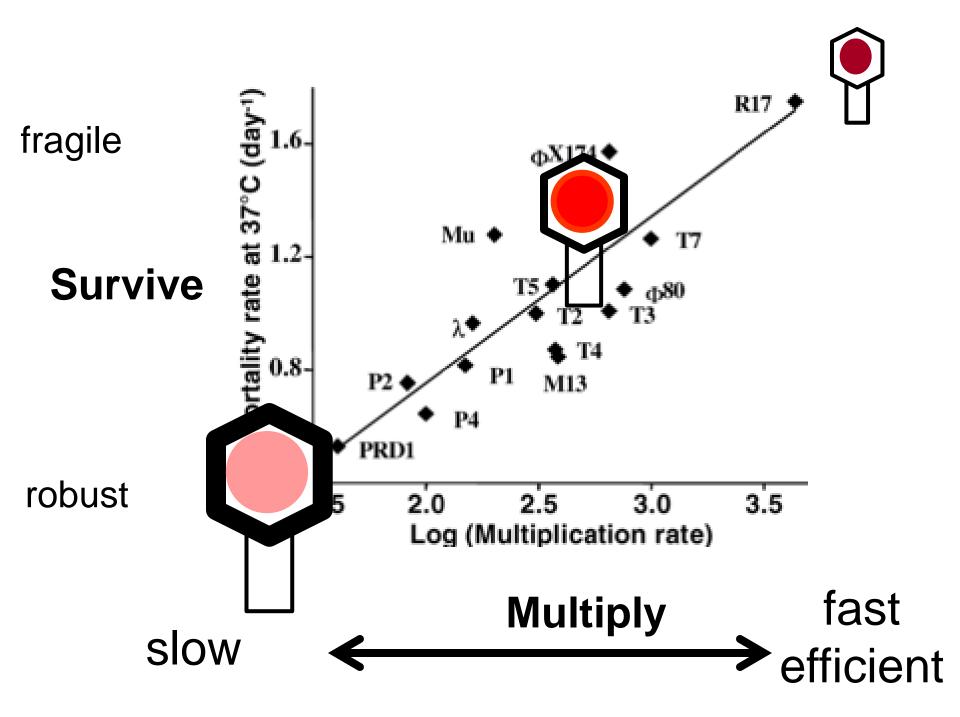


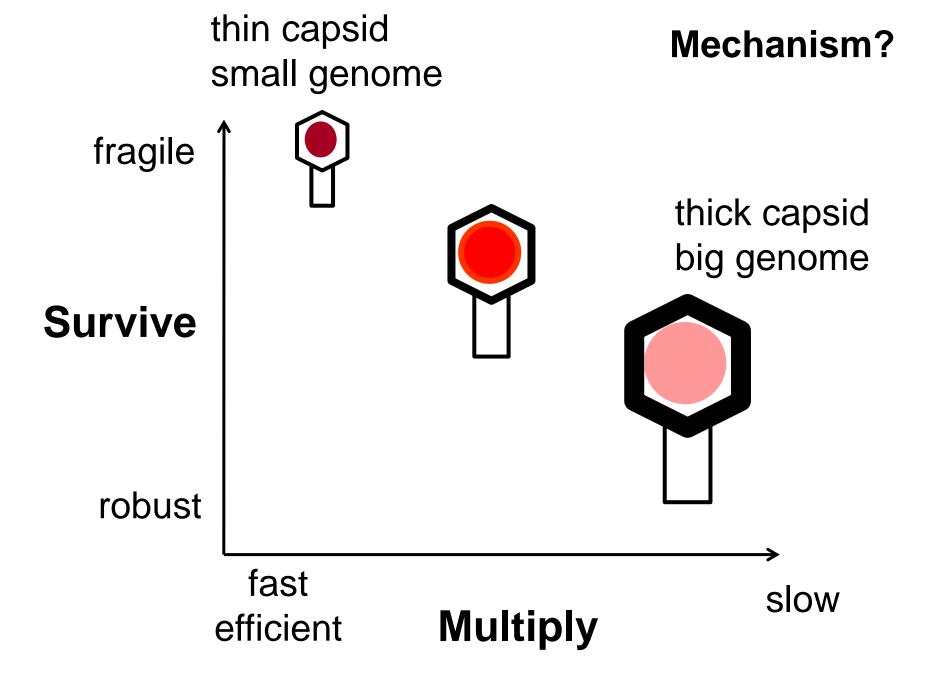
# antagonistic pleiotropy

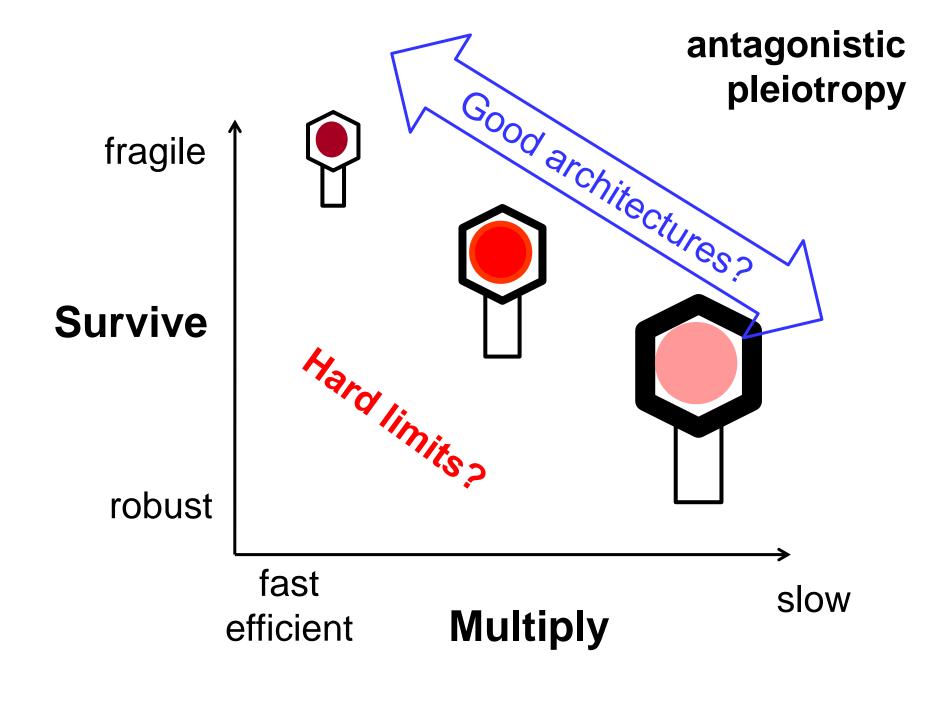




**Figure 4.** Correlations between Phage Life History Traits and Phage Particle Characteristics







Name	Type of Phage		Measured Life Cycle Characteristics						Published Structural Properties			Calculated Ratio	
	Family	Life Cycle	Decay Rate (d)			Multiplication Rate <sup>a</sup> (h <sup>-1</sup> )	Adsorption Rate (min <sup>-1</sup> )	E <sub>s</sub> b (kJ/mol)	Genome Size (kb)	Ext. Diameter <sup>c</sup> (nm)	Capsid MW <sup>d</sup> (kDa)	Surfacic Mass <sup>e</sup> (kDa/nm <sup>2</sup> )	Ppack
λ	Siphoviridae	Т	0.072	115	42	162	4.5 × 10 <sup>-10</sup>	142	49 [37]	63 [24]	22,500 [38]	22.7	0.572
M13	Inoviridae	Chronic				413	$9.0 \times 10^{-11}$	125	6 [37]	6.5x90 [37]	15,700 [39]	8.7	
MS2	Leviviridae	L	0.250	400	40	669	$6.5 \times 10^{-10}$	99	4 [37]	27 [40]	2,500 [41]	13.7	
Mu	Myoviridae	T	0.290	200	60	200	φ	111	43 [37]	54 [42]	15,000 [43]	20.6	0.845
P1	Myoviridae	T	0.077	400	60	149	$2.2 \times 10^{-10}$	119	100 [37]	85 [44]			0.435
P2	Myoviridae	T	0.041	160	48	88	$5.5 \times 10^{-11}$	123	34 [37]	60 [45]	20,400 [46]	22.7	0.468
P4	Myoviridae	T	0.045	300	60	101	$2.2 \times 10^{-10}$	105	12 [37]	45 [46]	12,400 [46]	24.5	0.429
φ80	Siphoviridae	T	0.120	600	5.5	776	$3.8 \times 10^{-10}$	114	45	61		24.3	0.585
φX174	Microviridae	L	0.200	180	15	697	2.9 × 10 <sup>-9</sup>	136	5 [37]	32 [47]	4,700 [48]	18.4	
PRD1	Tectiviridae	L	0.037	50	48	50	$4.6 \times 10^{-10}$	171	15 [49]	65 [49]	33,000 [49]	35.5	0.421
T2	Myoviridae	L	0.068	135	23	335	$4.0 \times 10^{-10}$		170 [37]	85x110 [50]		19.9	0.451
T3	Podoviridae	L	0.102	200	17	700	$1.6 \times 10^{-9}$	105	38 [51]	60 [52]		18.1	0.525
T4	Myoviridae	L	0.068	150	23	400	$5.0 \times 10^{-10}$	96	170 [37]	85×110 [50]	65,600 [50]	26.9	0.421
T5	Siphoviridae	L	0.120	290	44	399	$2.0 \times 10^{-10}$	115	122 [53]	65 [53]	27,500 [53]	13.7	0.439
T7	Podoviridae	L	0.187	260	13	1,131	$3.0 \times 10^{-9}$	100	40 [37]	60 [52]	16,300 [54]	19.4	0.615
R17	Leviviridae	L	0.520	3,570	53	4,288	$3.7 \times 10^{-9}$	99	4 [37]	27 [55]	2,600 [41]	14.7	

Mortality rate, burst size, latency period, and adsorption rate were measured as described in Material and Methods. Each value is the mean of at least three independent experiments. Genome size, diameter, and molecular weight were collected from published results. The internal volume used to calculate  $\rho_{peoc}$  has either been collected in structural studies of phage capsids or calculated by subtracting the thickness of the shell from the external diameter. Empty cells in the table correspond to data that were either not available or not measured. "Mean of the ratio obtained by dividing the burst size by the latency period, calculated for each experiment.

DOI: 10.1371/journal.pbio.0040193.t001

<sup>&</sup>lt;sup>b</sup>E<sub>o</sub>: energy of activation of the reaction leading to inactivation of virions, obtained from the Arrhenius equation linking mortality rate and temperature between 30 °C and 45 °C. The energy of activation represents the energy the system has to overcome so that the reaction occurs.

Ext. diameter: external diameter of the capsid.

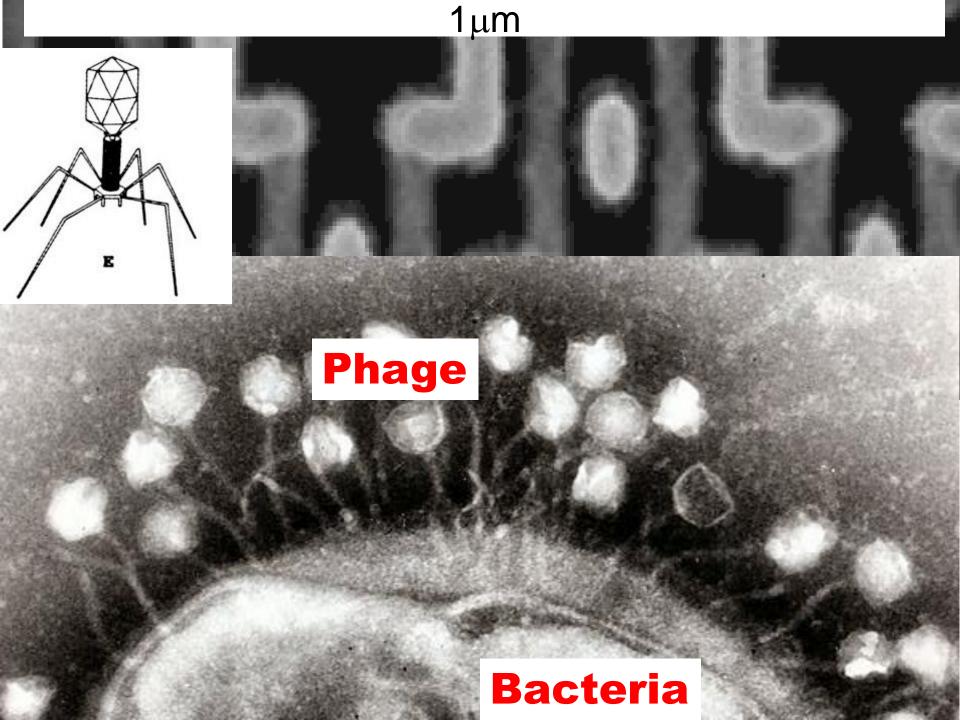
<sup>&</sup>lt;sup>d</sup>Molecular weight of the proteins constituting the capsid.

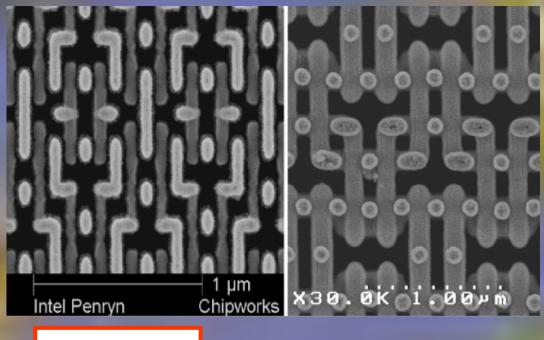
<sup>\*</sup>Capsid molecular weight divided by the surface of the capsid; this ratio represents the thickness of the shell.

Volume occupied by the genome divided by the internal volume of the capsid.

T: Temperate phage, L: Virulent Phage, Chronic: creates a chronic infection

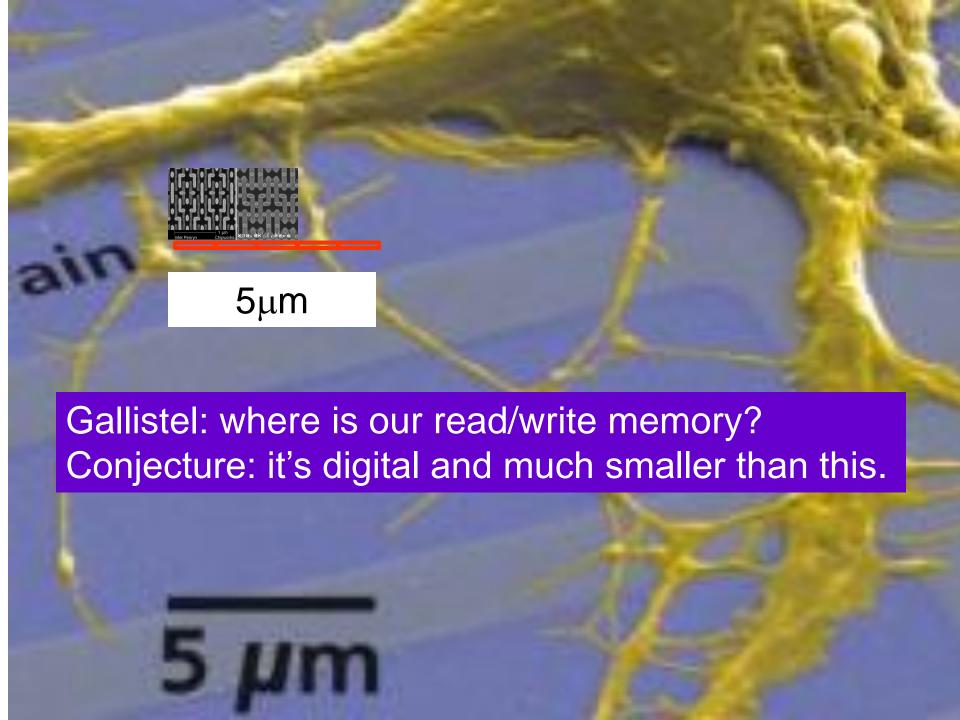
# $1\mu m$ D **Viruses** MINIMINA 1000 nm

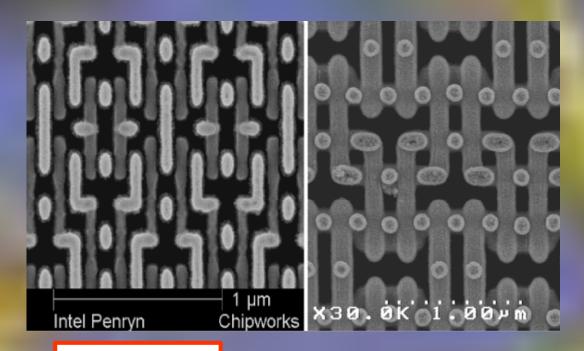




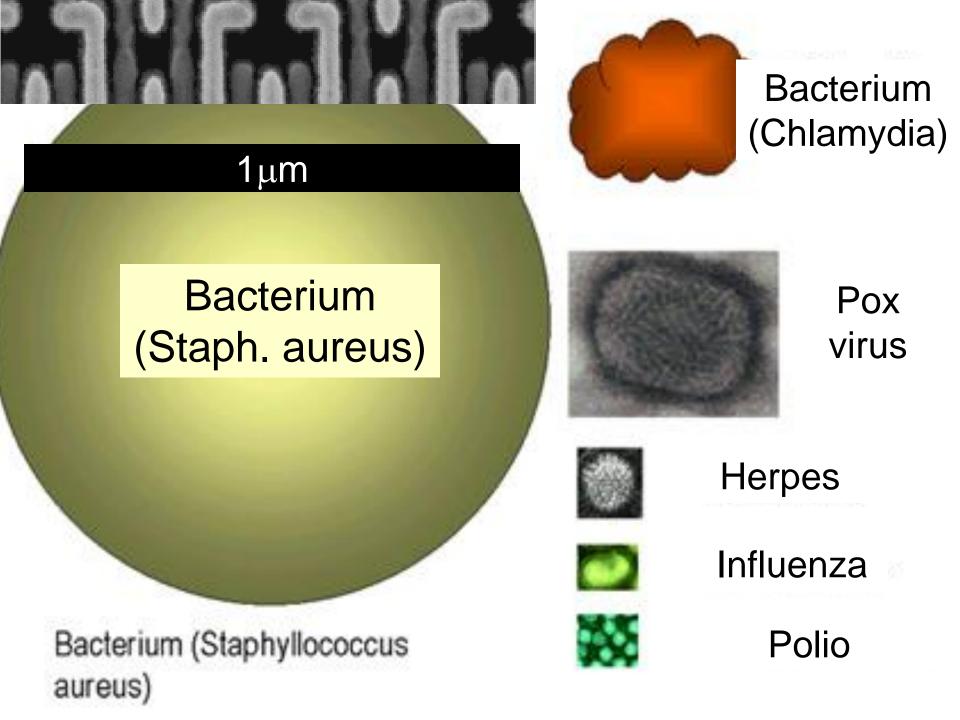
 $1\mu m$ 

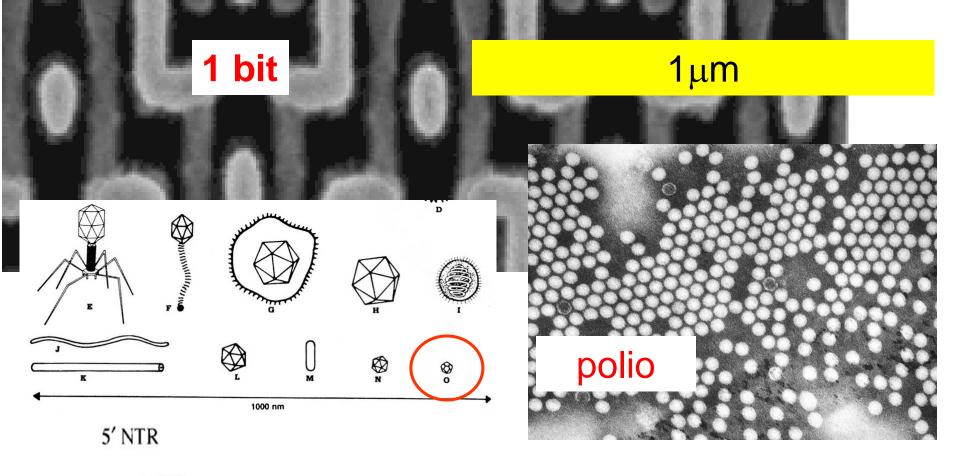
why computer memory is almost "free"

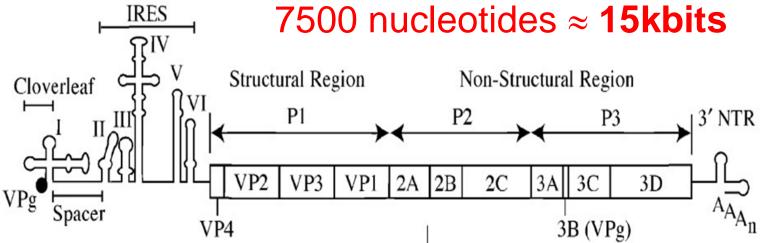


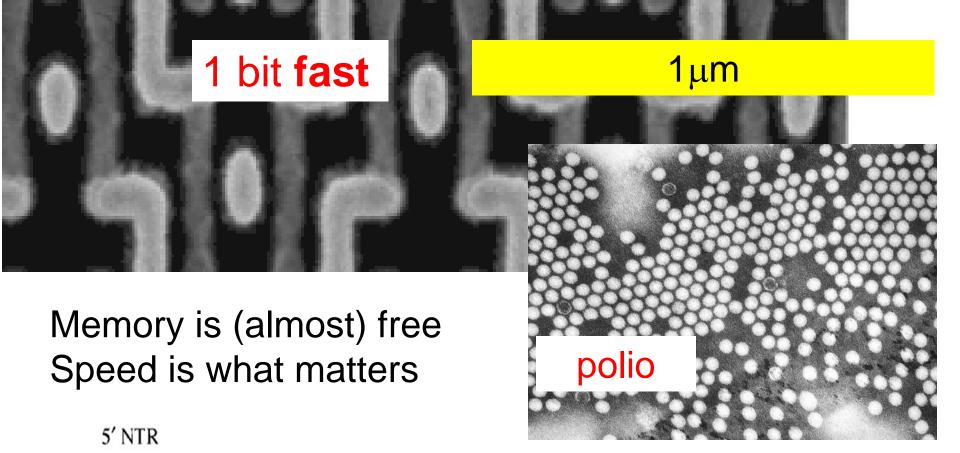


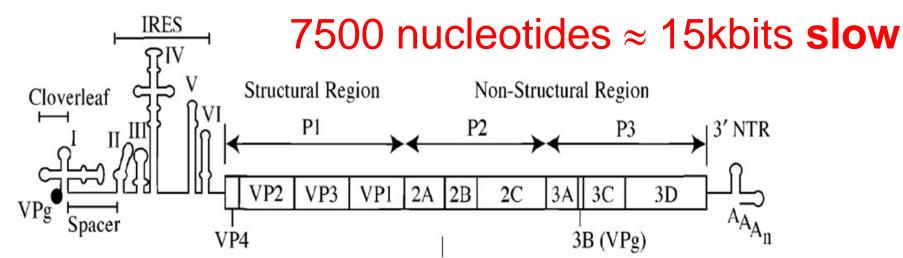
 $1\mu m$ 











#### **RESEARCH** ARTICLES

# Glycolytic Oscillations and Limits on Robust Efficiency

Fiona A. Chandra, 1\* Gentian Buzi, 2 John C. Doyle 2

Both engineering and evolution are constrained by trade-offs between efficiency and robustness, but theory that formalizes this fact is limited. For a simple two-state model of glycolysis, we explicitly derive analytic equations for hard trade-offs between robustness and efficiency with oscillations as an inevitable side effect. The model describes how the trade-offs arise from individual parameters, including the interplay of feedback control with autocatalysis of network products necessary to power and catalyze intermediate reactions. We then use control theory to prove that the essential features of these hard trade-off "laws" are universal and fundamental, in that they depend minimally on the details of this system and generalize to the robust efficiency of any autocatalytic network. The theory also suggests worst-case conditions that are consistent with initial experiments.

Chandra, Buzi, and Doyle

Most important paper so far.

### UG biochem, math, control theory

the cen's use of ATT. III glycolysis, two ATP molecules are consumed upstream and four are produced downstream, which normalizes to q = 1(each y molecule produces two downstream) with kinetic exponent a = 1. To highlight essential trade-offs with the simplest possible analysis, we normalize the concentration such that the unperturbed ( $\delta = 0$ ) steady states are  $\overline{y} = 1$  and  $\bar{x} = 1/k$  [the system can have one additional steady state, which is unstable when (1, 1/k) is stable]. [See the supporting online material (SOM) part I]. The basal rate of the PFK reaction and the consumption rate have been normalized to 1 (the 2 in the numerator and feedback coefficients of the reactions come from these normalizations). Our results hold for more general systems on discussed below and in SOM, but the analysis

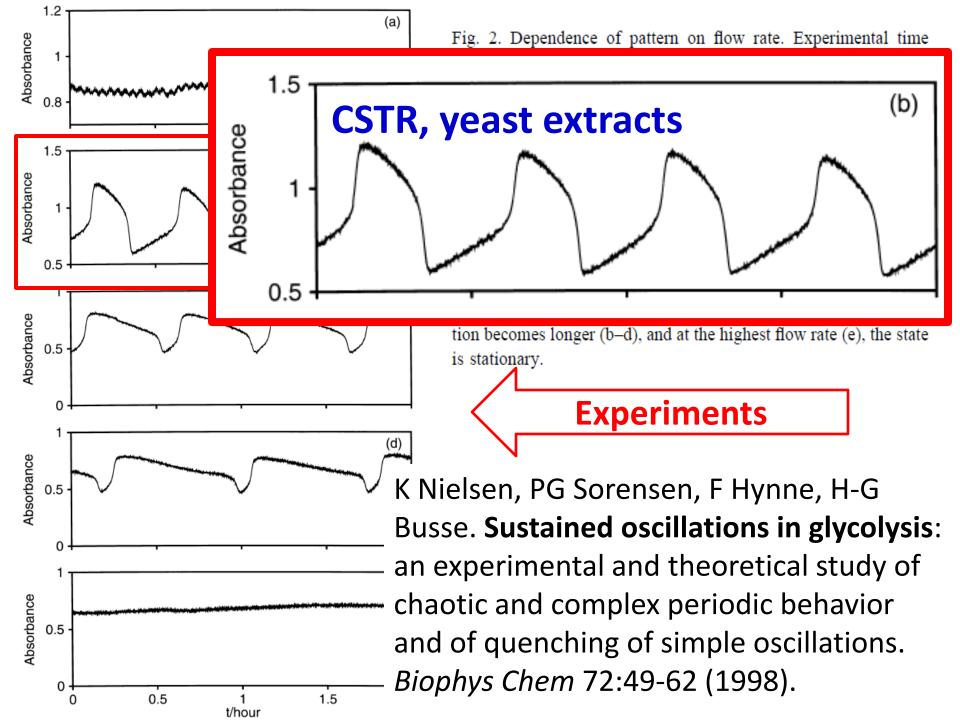


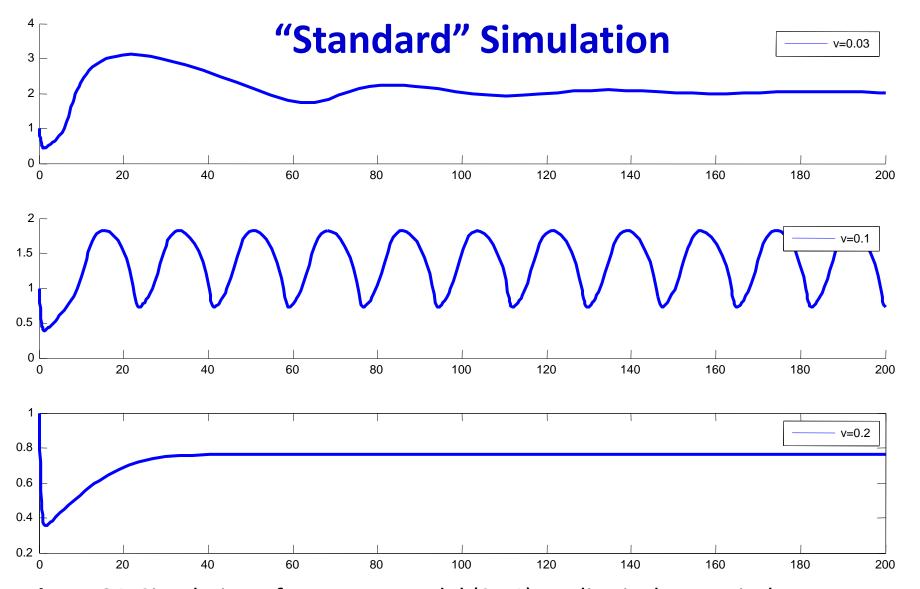
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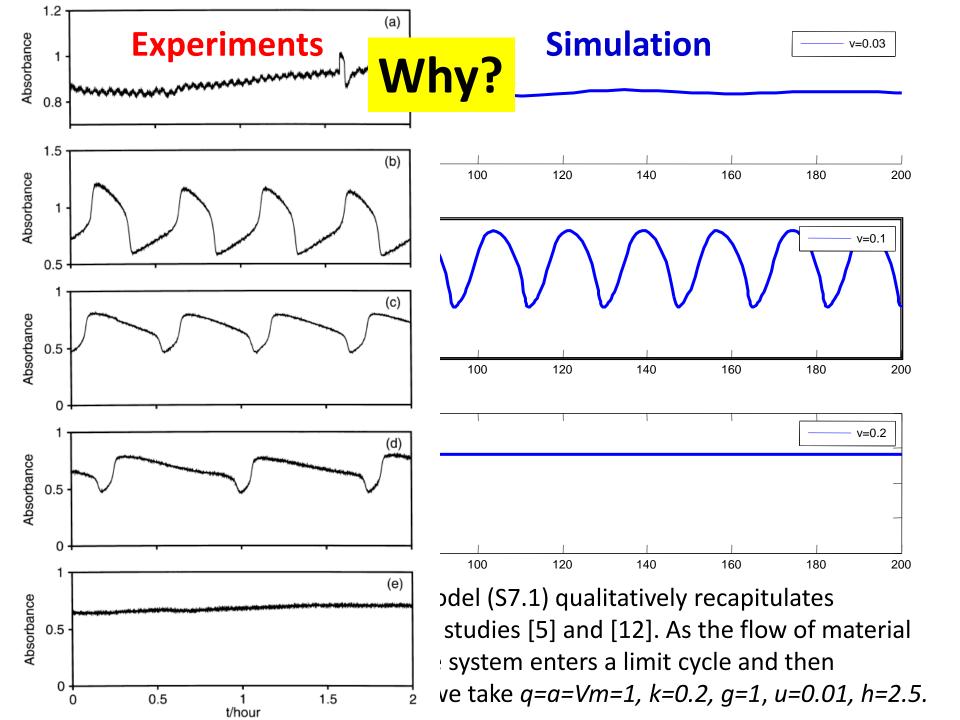
VOL 333

8 JULY 2011





**Figure S4**. Simulation of two state model (S7.1) qualitatively recapitulates experimental observation from CSTR studies [5] and [12]. As the flow of material in/out of the system is increased, the system enters a limit cycle and then stabilizes again. For this simulation, we take q=a=Vm=1, k=0.2, g=1, u=0.01, h=2.5.



### Why?

#### Levels of explanation:

- 1. Possible
- 2. Plausible
- 3. Actual

- 4. Mechanistic
- 5. Necessary

Science

Engineering

Medicine

### Glycolytic "circuit" and oscillations

- Most studied, persistent mystery in cell dynamics
- End of an old story (why oscillations)
  - side effect of hard robustness/efficiency tradeoffs
  - no purpose per se
  - just needed a theorem
- Beginning of a new one
  - robustness/efficiency tradeoffs
  - complexity and architecture
  - need more theorems and applications

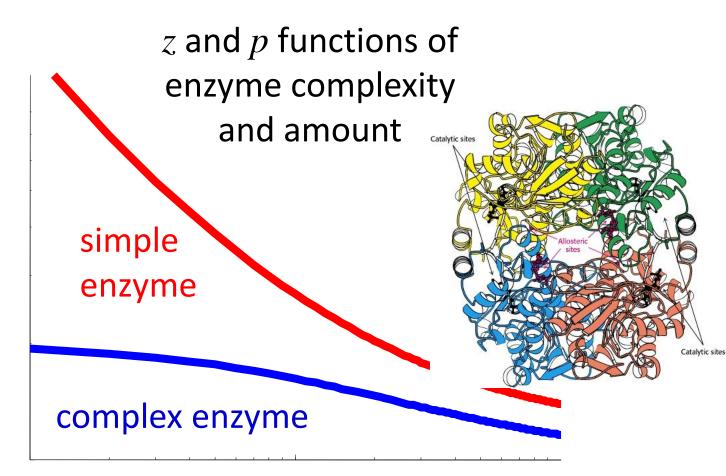


#### Theorem!

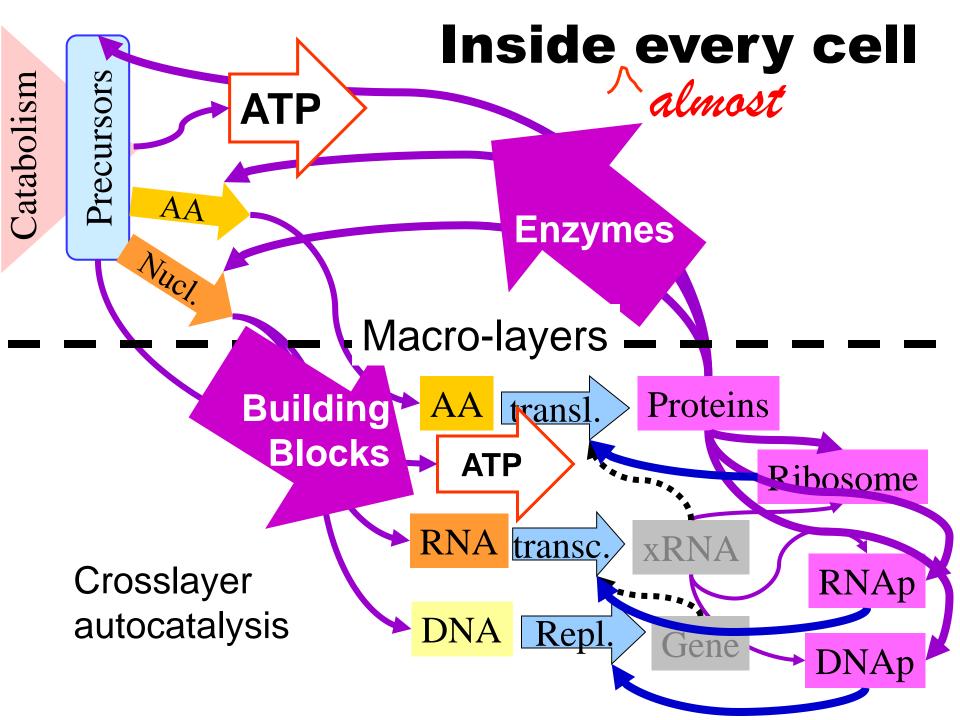
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$

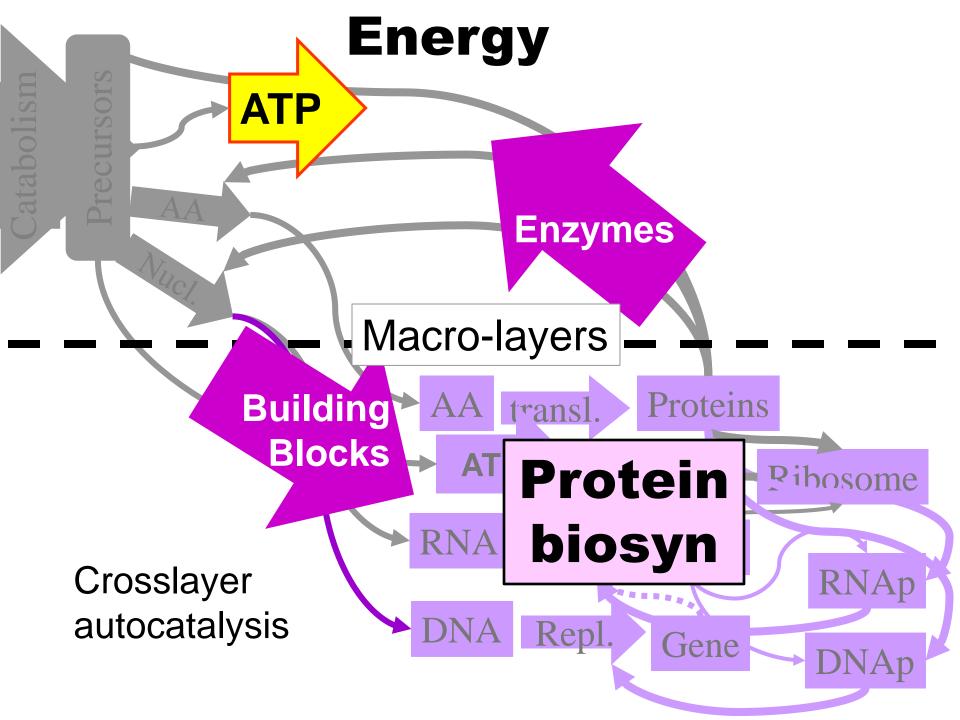


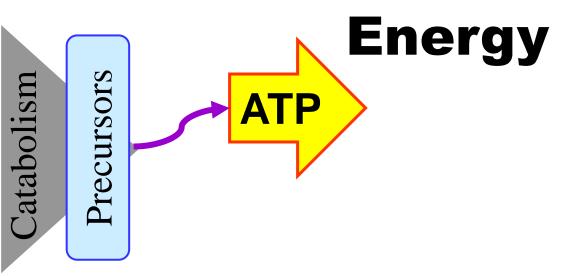
$$\ln \left| \frac{z+p}{z-p} \right|$$

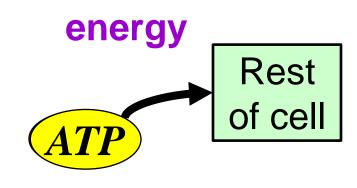


Enzyme amount



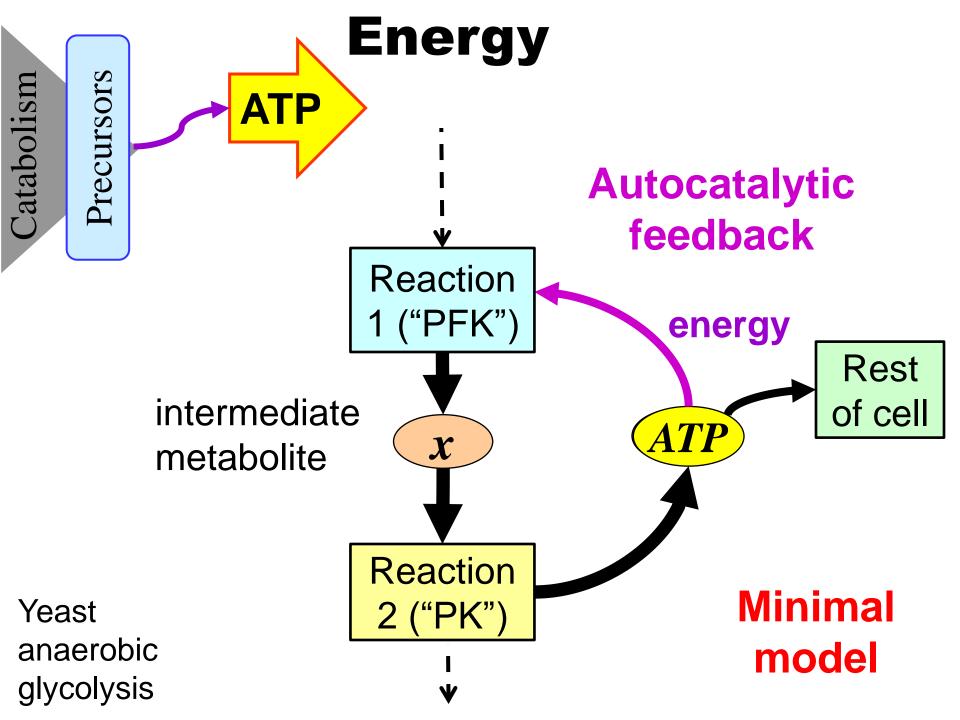




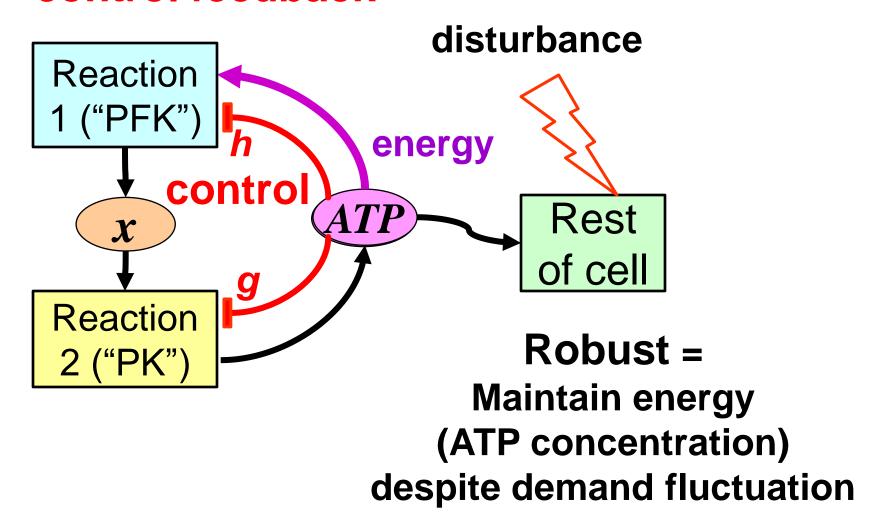


Yeast anaerobic glycolysis

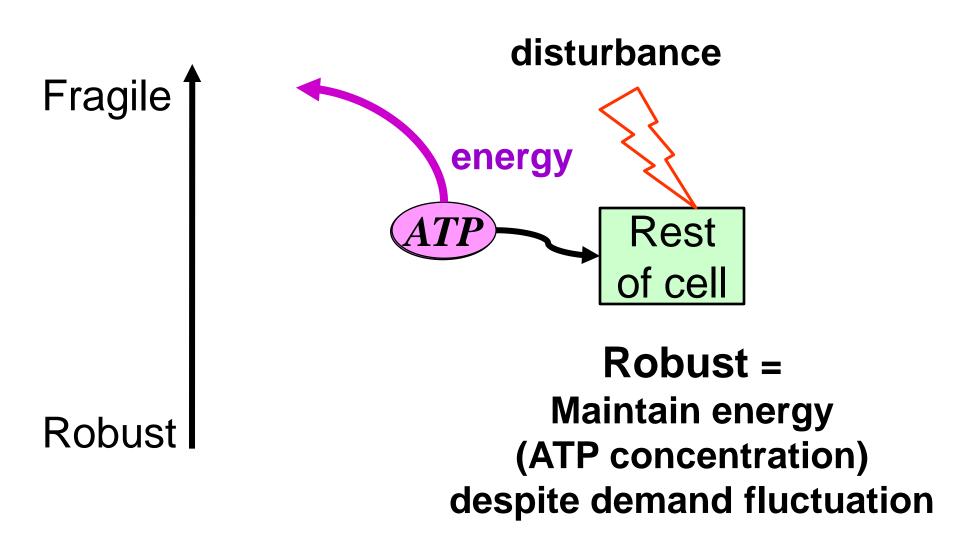
Minimal model



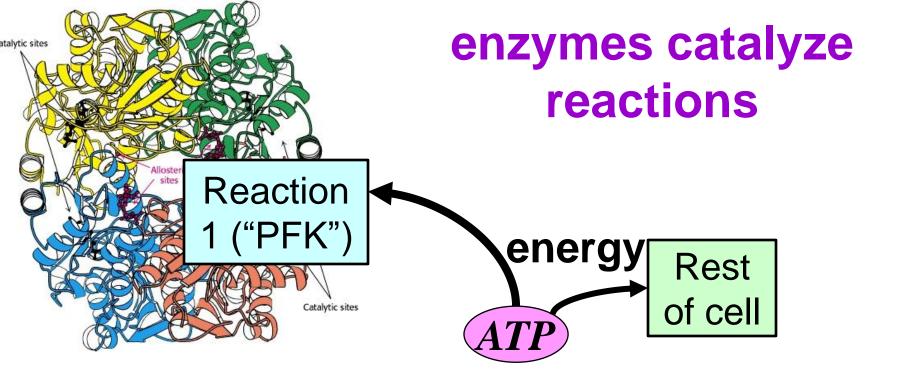
#### control feedback



Tight control creates "weak linkage" between power supply and demand

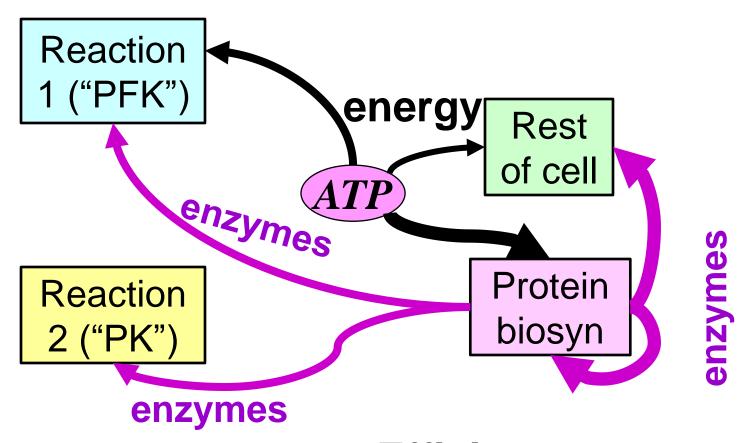


Tight control creates "weak linkage" between power supply and demand

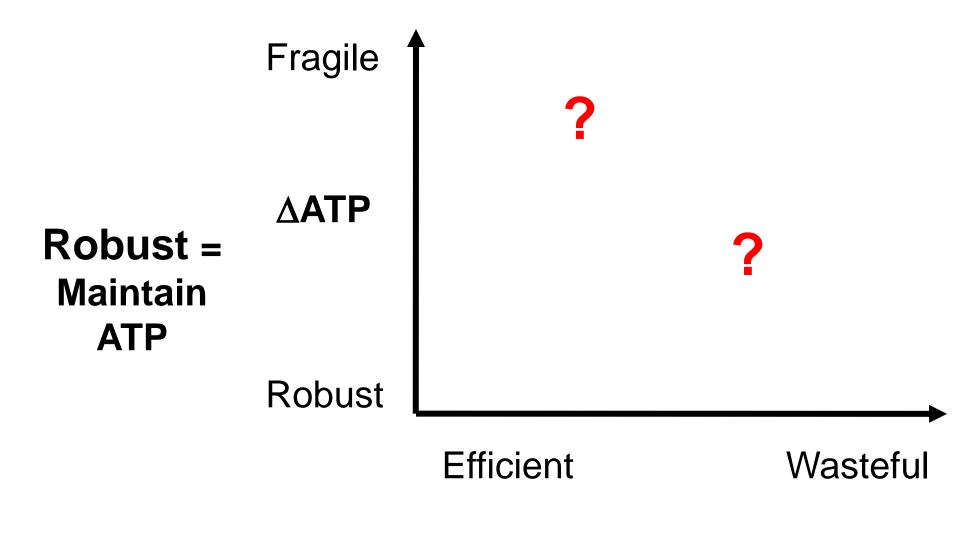


Reaction 2 ("PK")

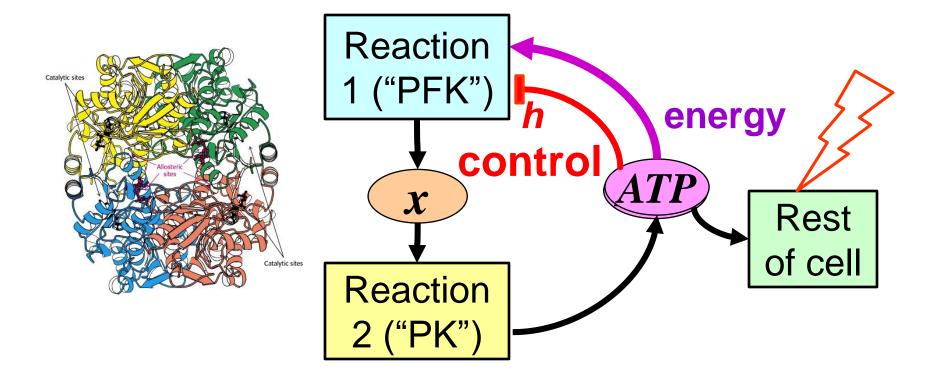
# enzymes catalyze reactions



Efficient = low metabolic overhead ≈ low enzyme amount



Efficient = low enzyme amount



#### **Standard story**:

Autocatalytic plus control feedback necessary and sufficient for oscillations

Proof: Dynamical systems model, simulation, bifurcation analysis

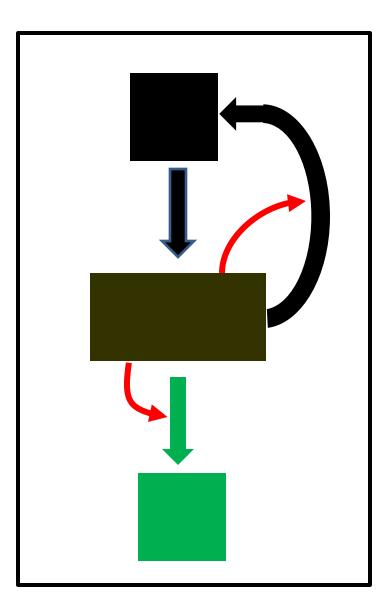
## **Control feedback**

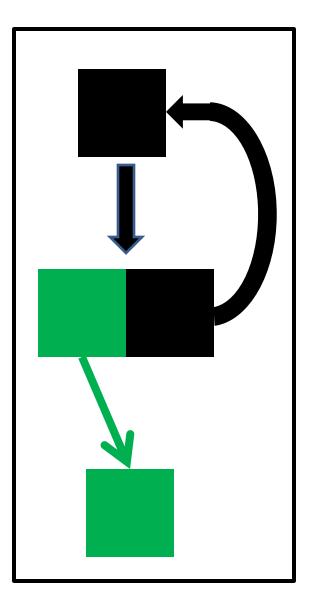
## Autocatalytic feedback

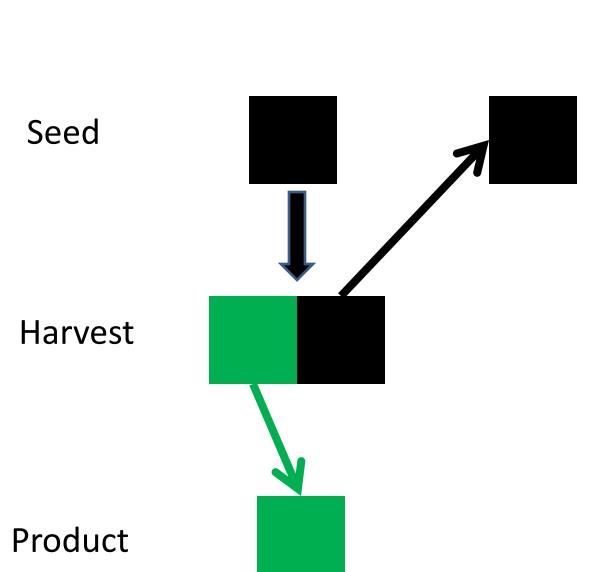
Seed

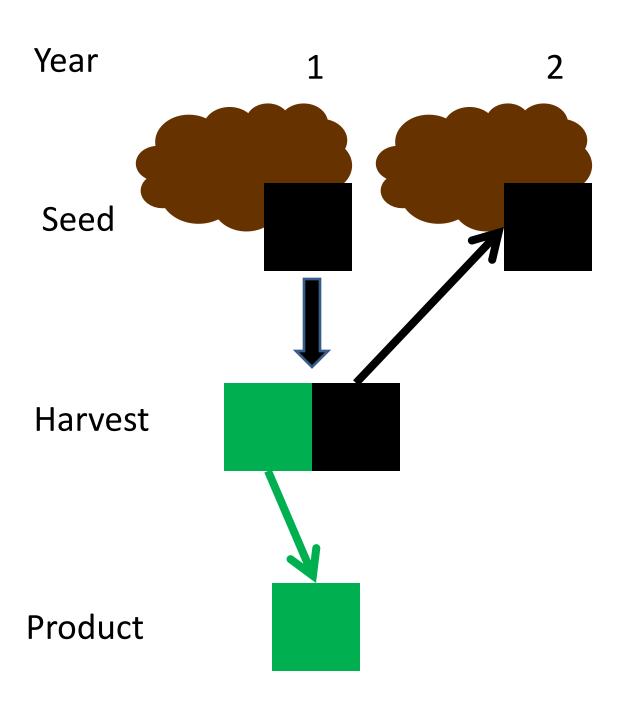
Harvest

**Product** 



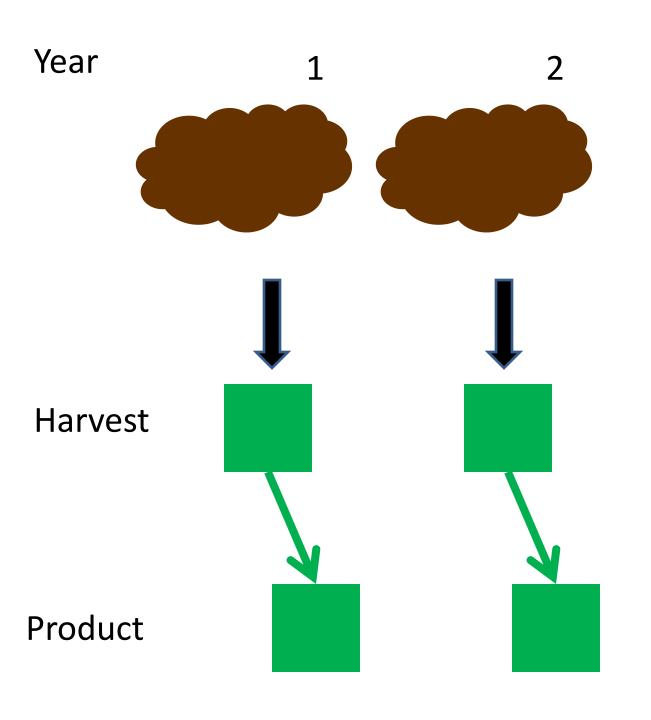




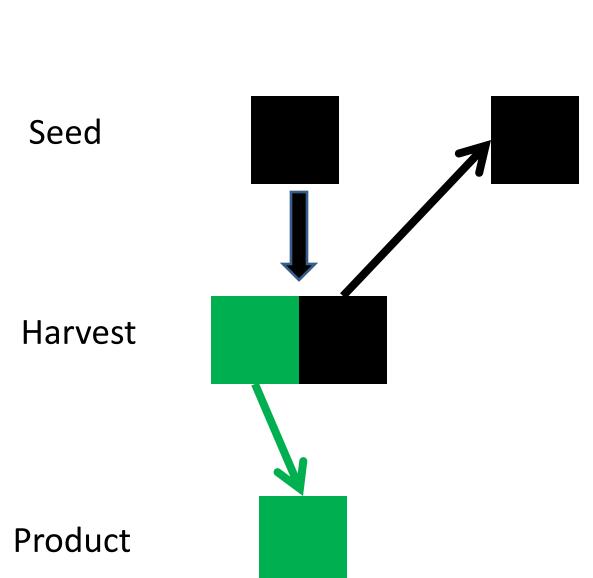


There may be other resources needed that aren't recycled

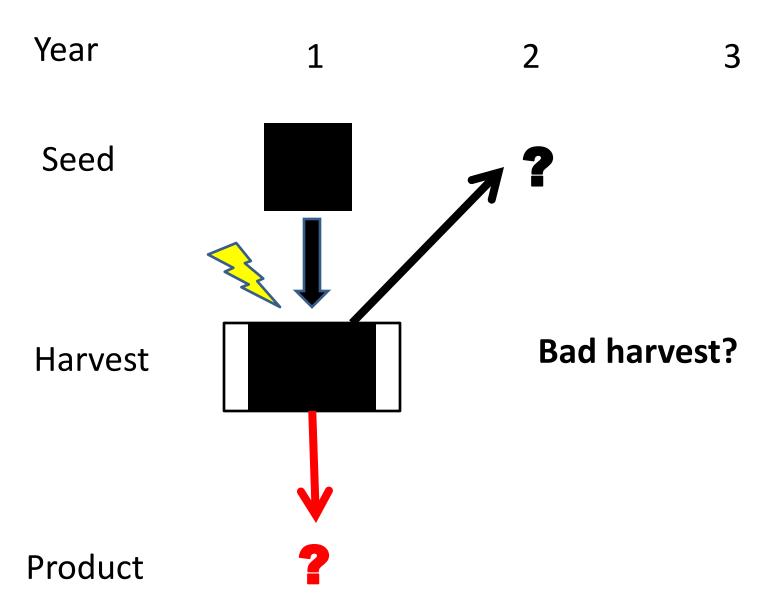
which we'll ignore for now



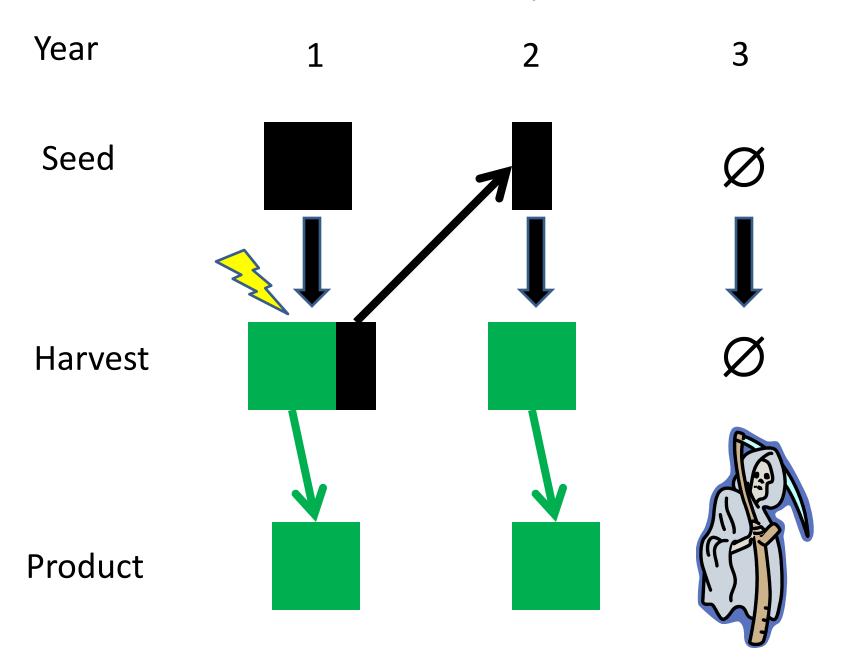
Some processes don't require autocatalysis

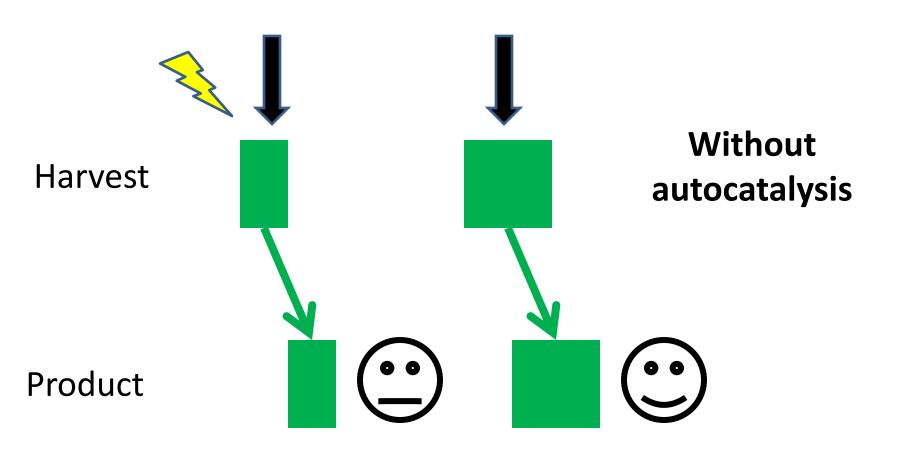


**Autocatalytic** Year feedback Seed Harvest **Product** 

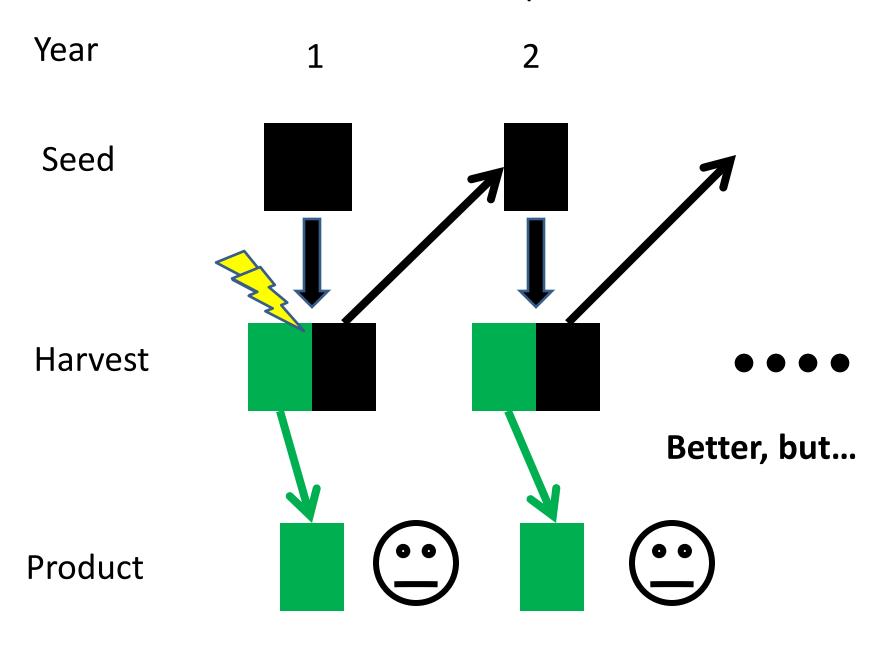


#### Maintain product?

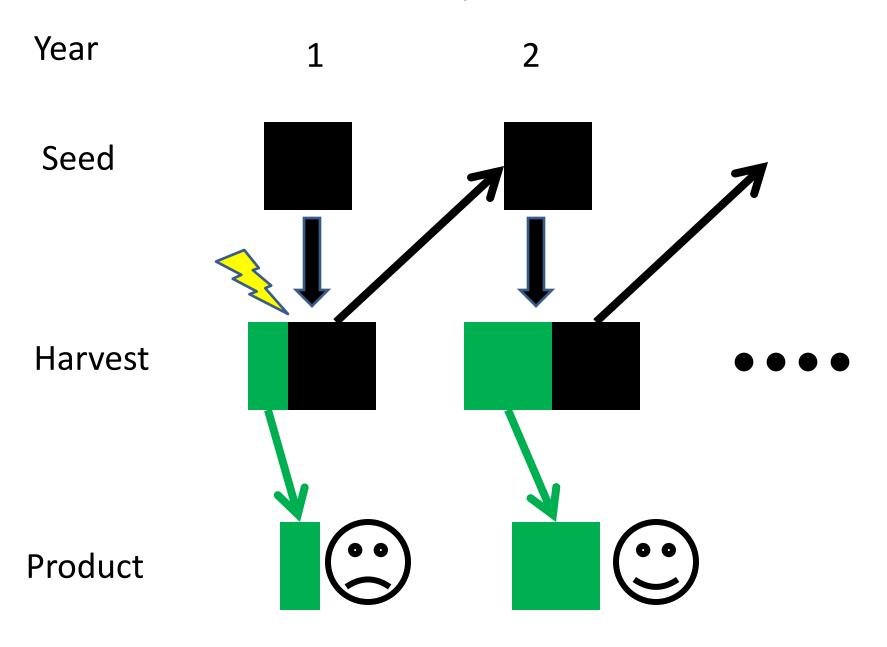




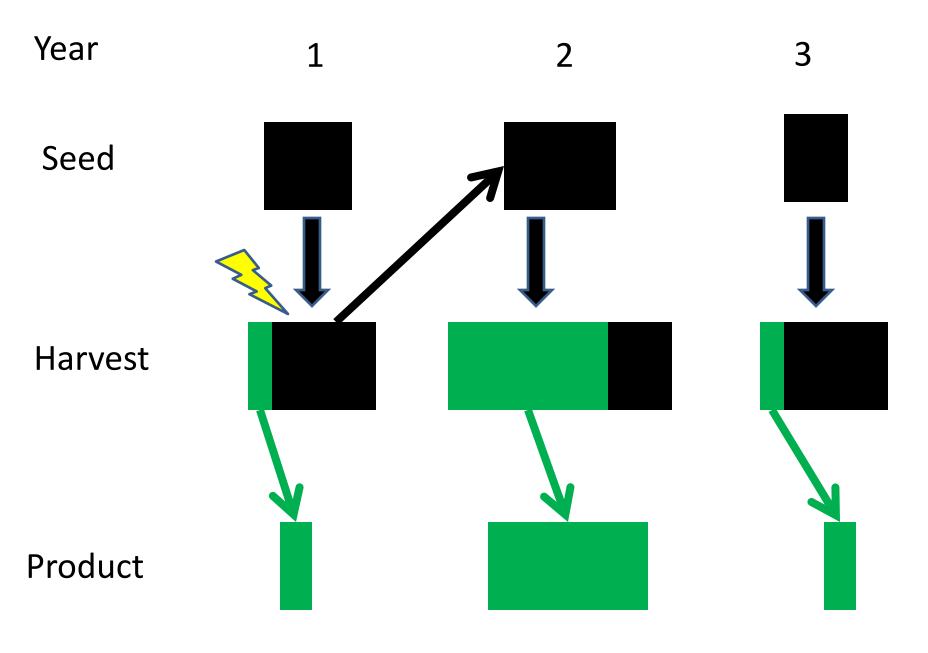
#### Cut back product



#### Cut back product more



#### Over-react and oscillate



Year

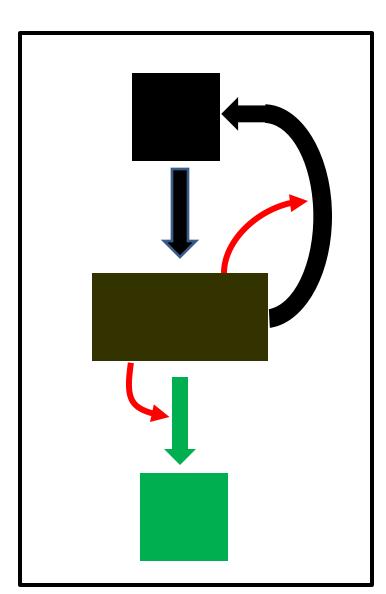
## Control feedback

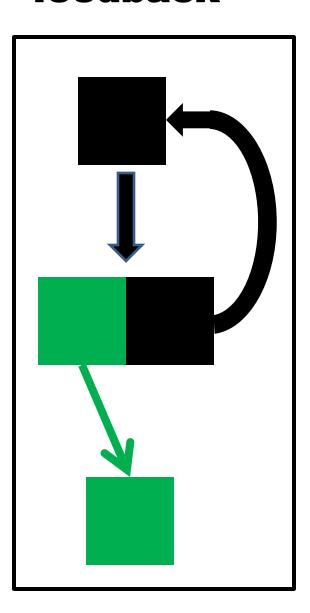
Autocatalytic feedback

Seed

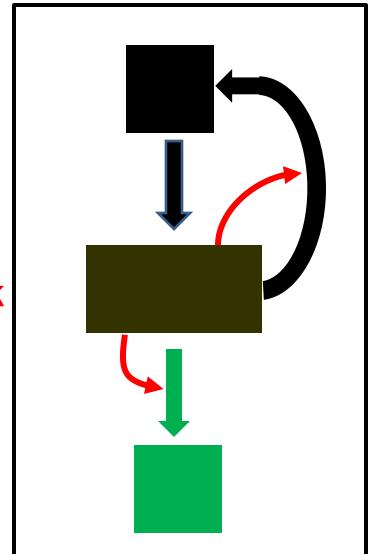
Harvest

**Product** 

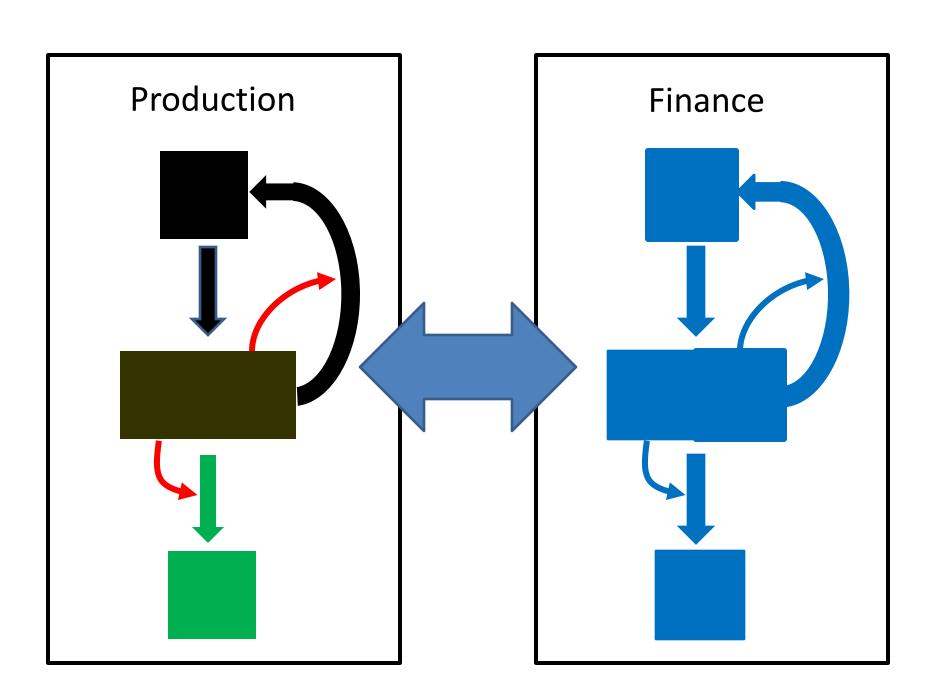




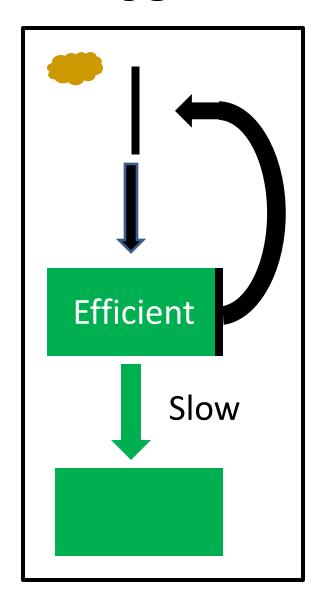
Control feedback



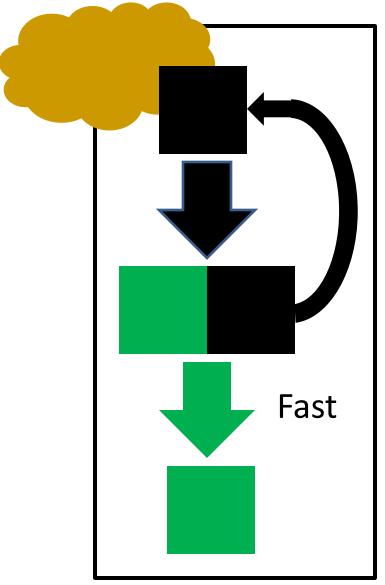
Autocatalytic feedback makes control harder



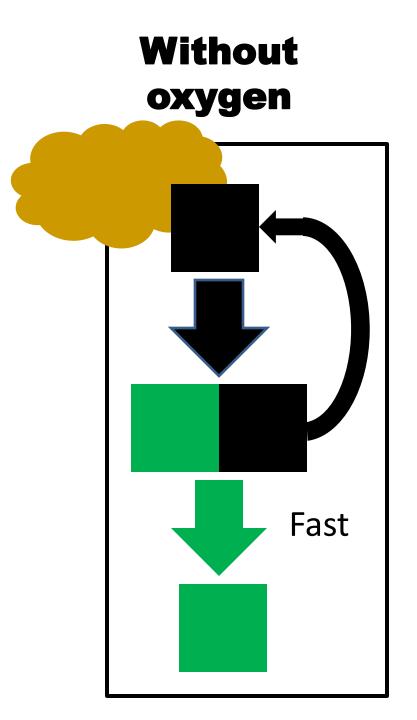
## With oxygen

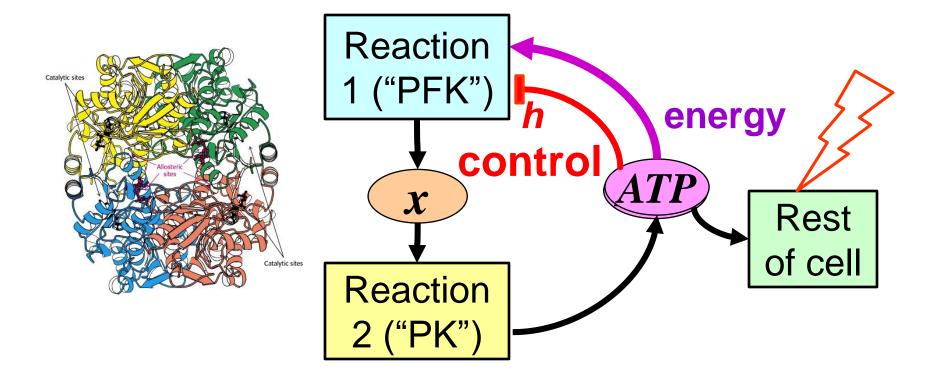


## Without oxygen



This is why we focus on anaerobic glycolysis, to maximize the autocatalytic feedback.





#### **Standard story**:

Autocatalytic plus control feedback necessary and sufficient for oscillations

Proof: Dynamical systems model, simulation, bifurcation analysis

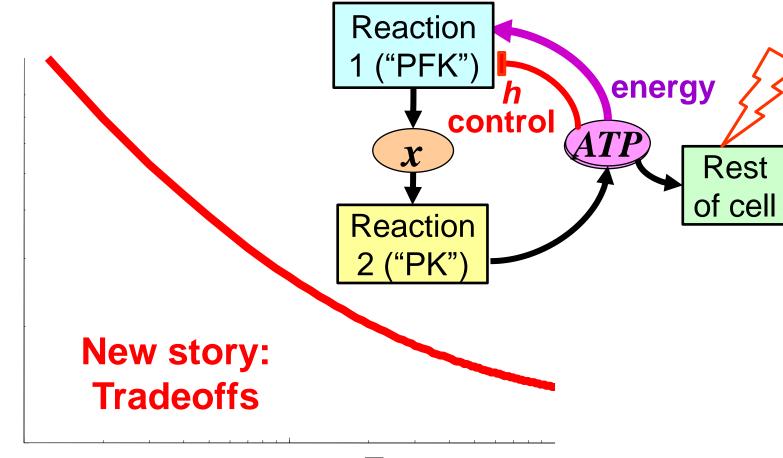
#### Theorem!

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$

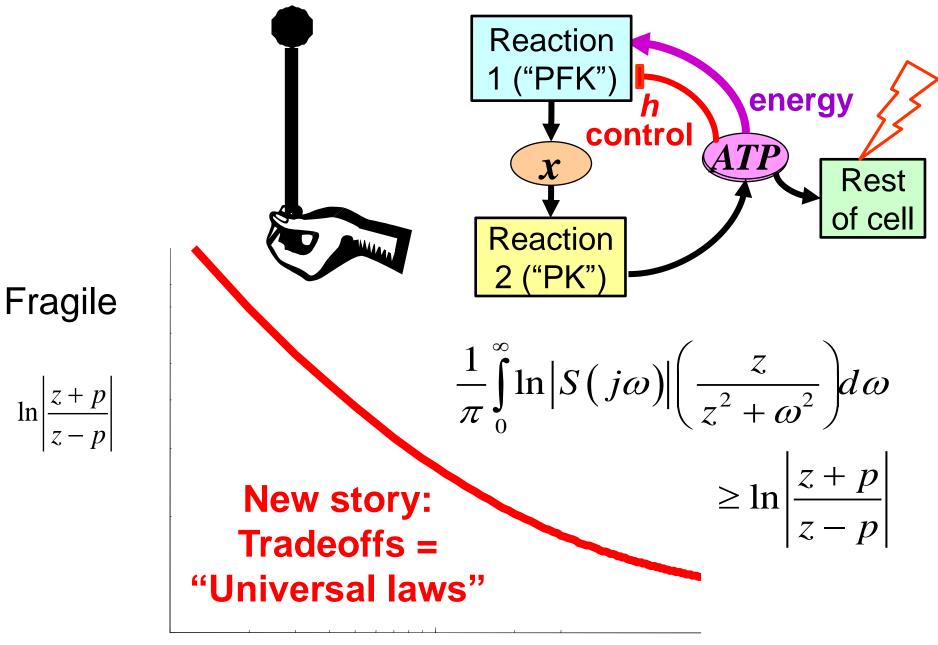
DS → CDS



$$\left| \ln \left| \frac{z+p}{z-p} \right| \right|$$

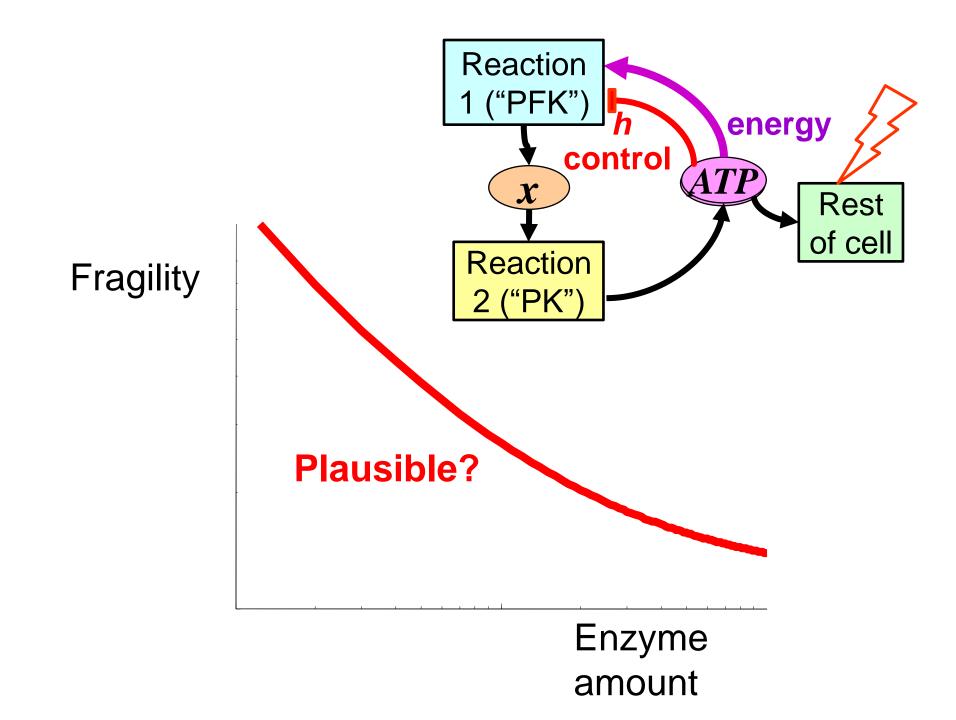


Enzyme amount

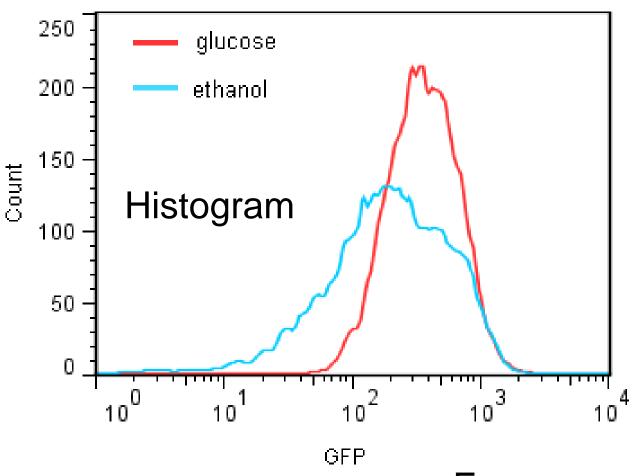


Cheap

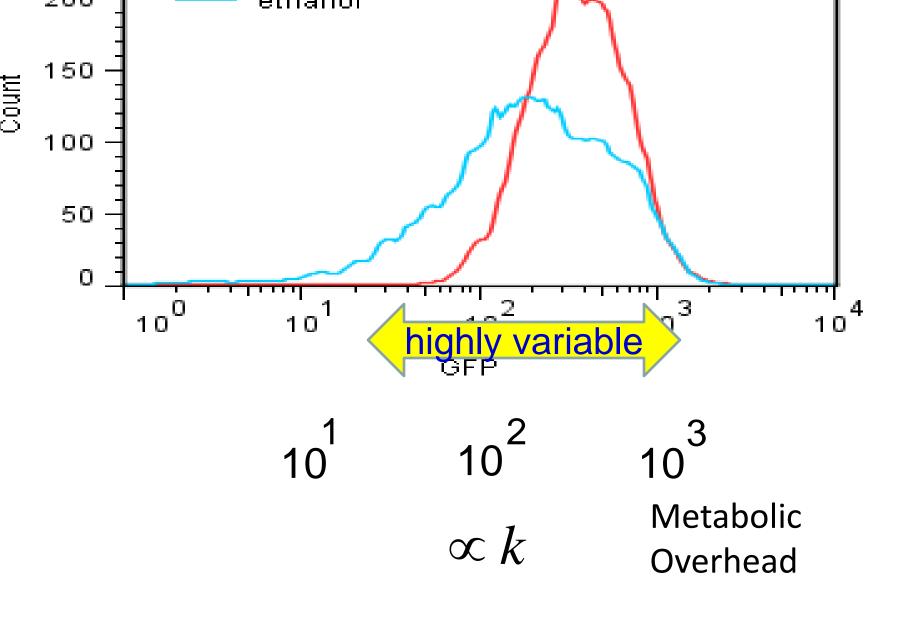
Expensive



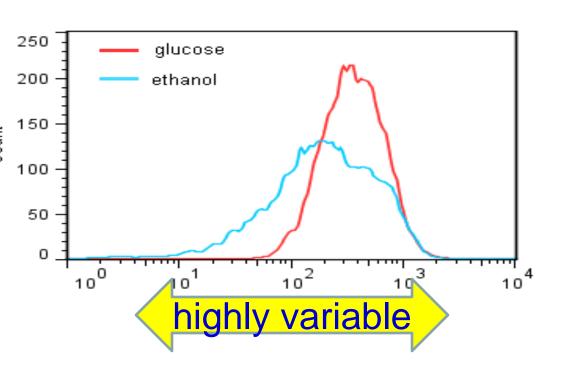
Fluorescence histogram (fluorescence vs. cell count) of GFP-tagged Glyceraldehyde-3-phosphate dehydrogenase (TDH3). Cells grown in ethanol have lower mean and median and higher variability.



Enzyme amount



See Lestas, Vinnicombe, Paulsson, Nature



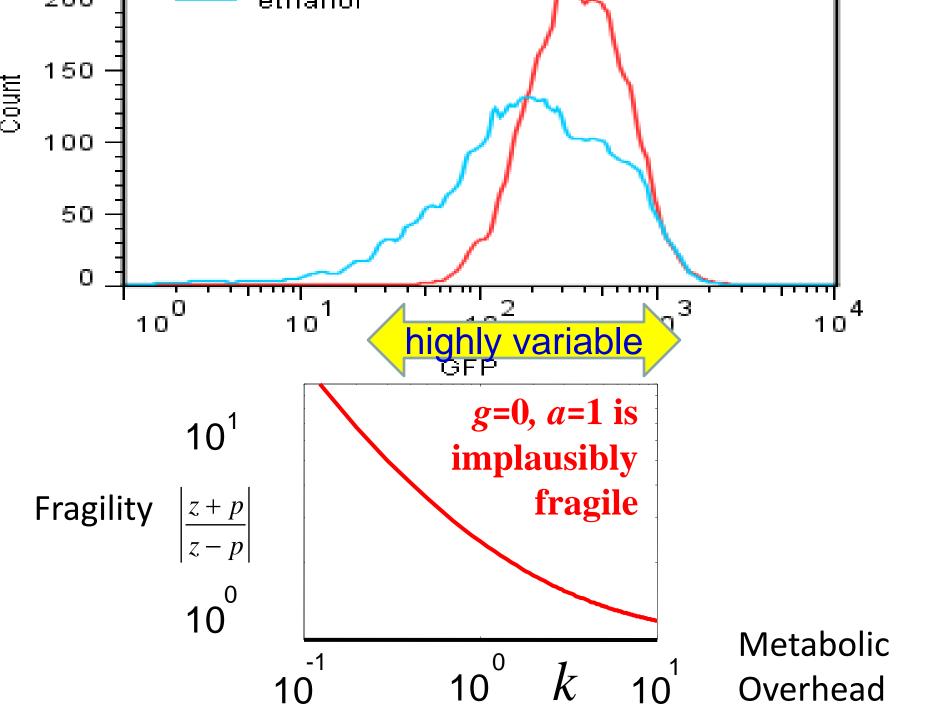
#### Communicate

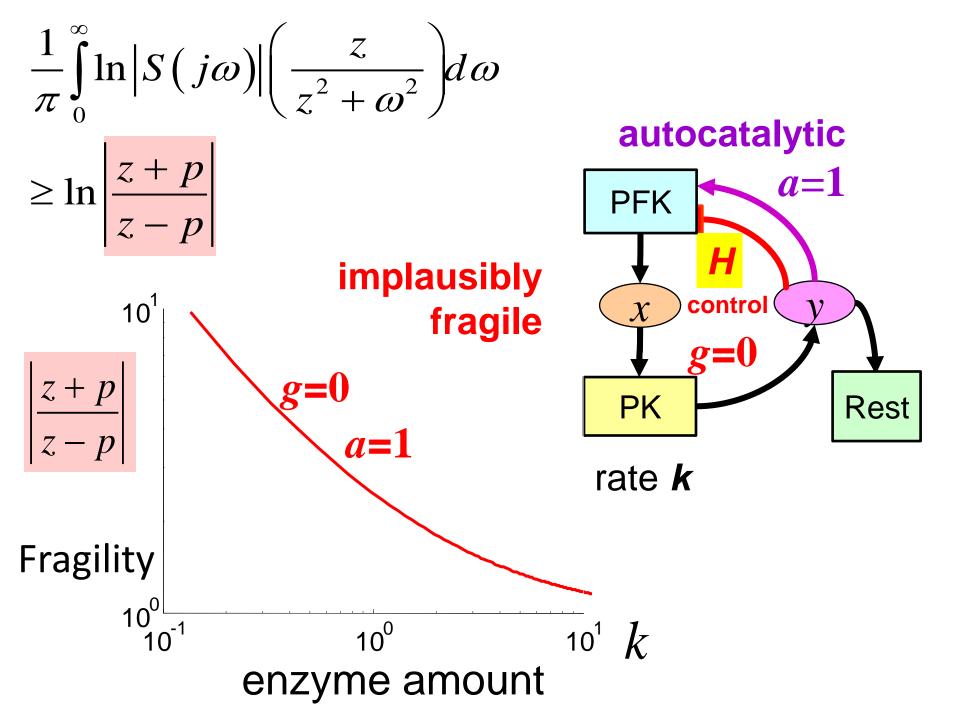
Shannon

Delay is least important

- Transcription is highly variable
- Even if you allow ∞ delay!
- So information theory applies

See Lestas, Vinnicombe, Paulsson, Nature





$$\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{z}{z^{2} + \omega^{2}}\right) d\omega$$

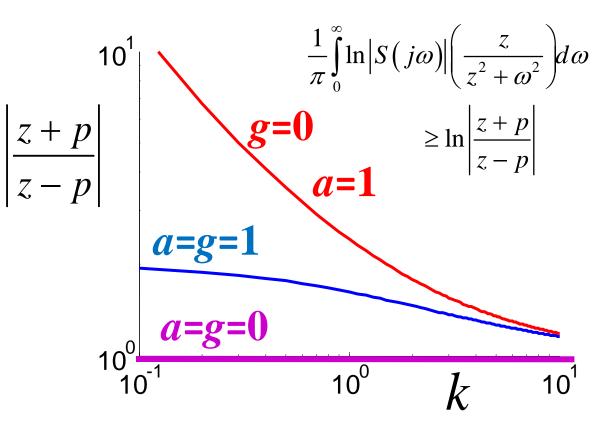
$$\geq \ln \left|\frac{z + p}{z - p}\right|$$

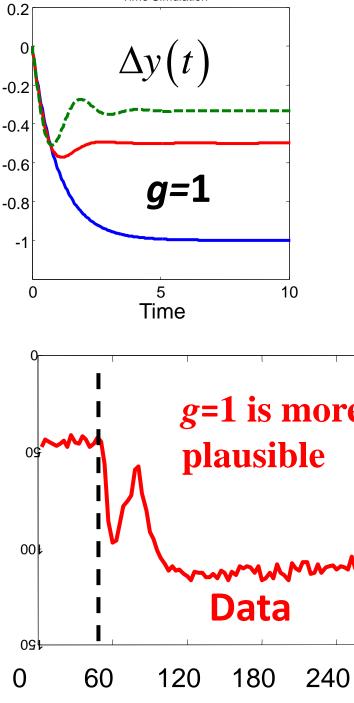
$$\frac{z + p}{z - p}$$

$$\frac{10^{1}}{z - p}$$

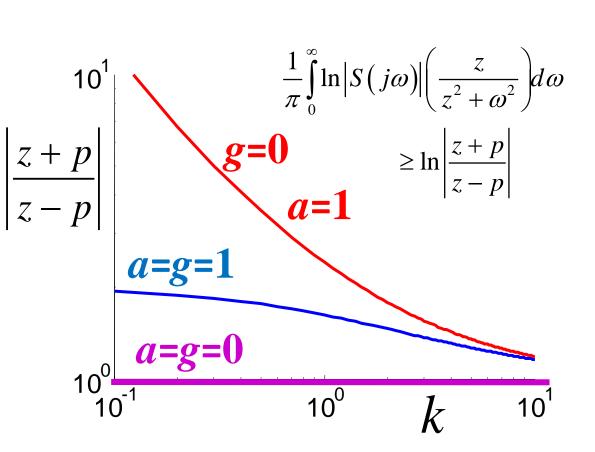
$$\frac{z + p}{z - p}$$

a=1 sufficient for oscillations
(and is actual)
g=1 necessary for robust
efficiency (and is actual)

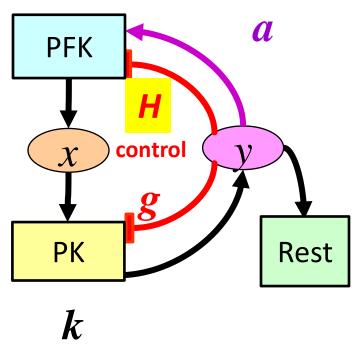




# a=1 sufficient for oscillations (and is actual) g=1 necessary for robust efficiency (and is actual)

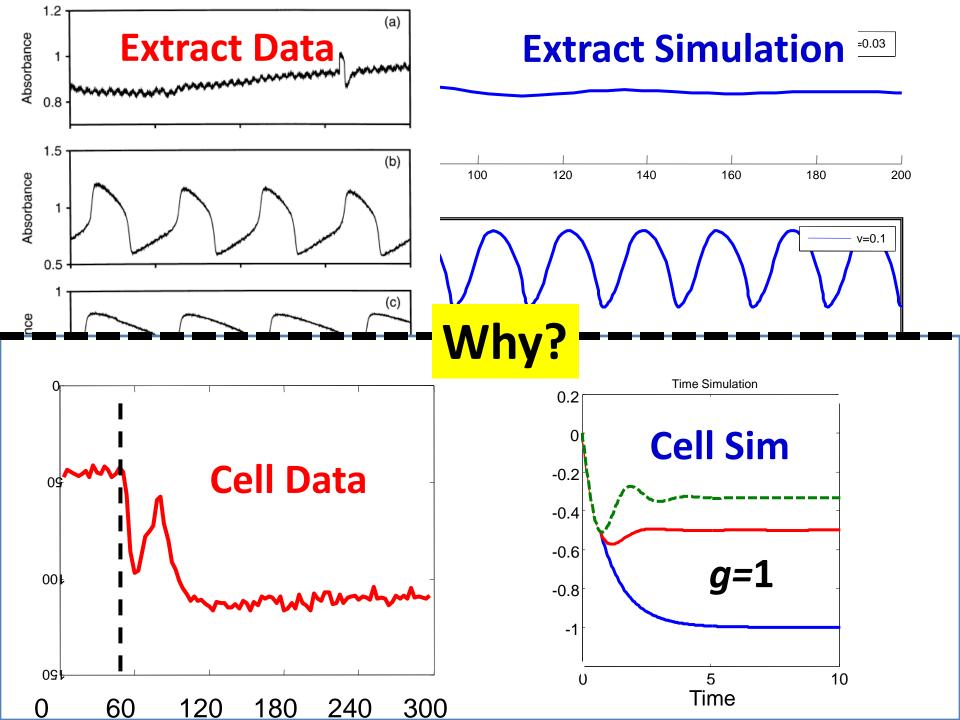


#### autocatalytic



## What (some) reviewers say

- "...to establish universality for all biological and physiological systems is simply wrong. It cannot be done..."
- "... a mathematical scheme without any real connections to biological or medical..."
- "If such oscillations are indeed optimal, why are they not universally present?"
- "...universality is well justified in physics... for biological and physiological systems ...a dream that will never be realized, due to the vast diversity in such systems."
- "...does not seem to understand or appreciate the vast diversity of biological and physiological systems..."
- "...a high degree of abstraction, which ...make[s] the model useless ..."

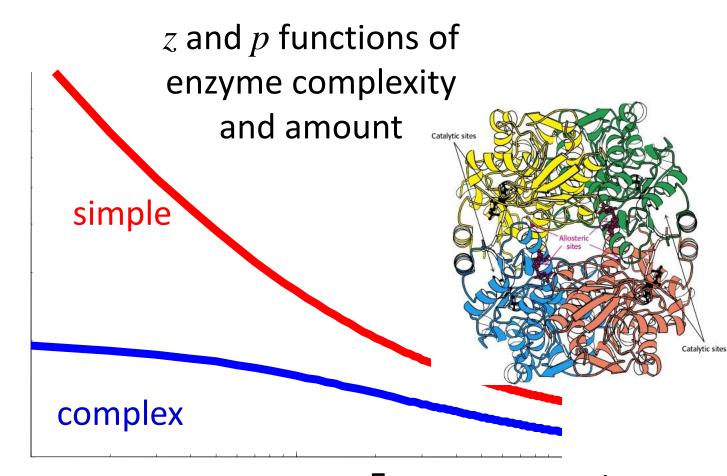


#### Theorem!

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$



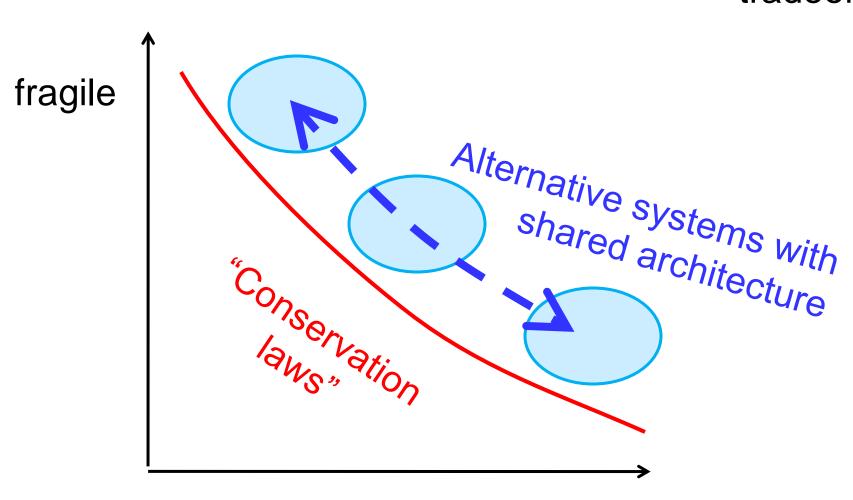
$$\ln \left| \frac{z+p}{z-p} \right|$$



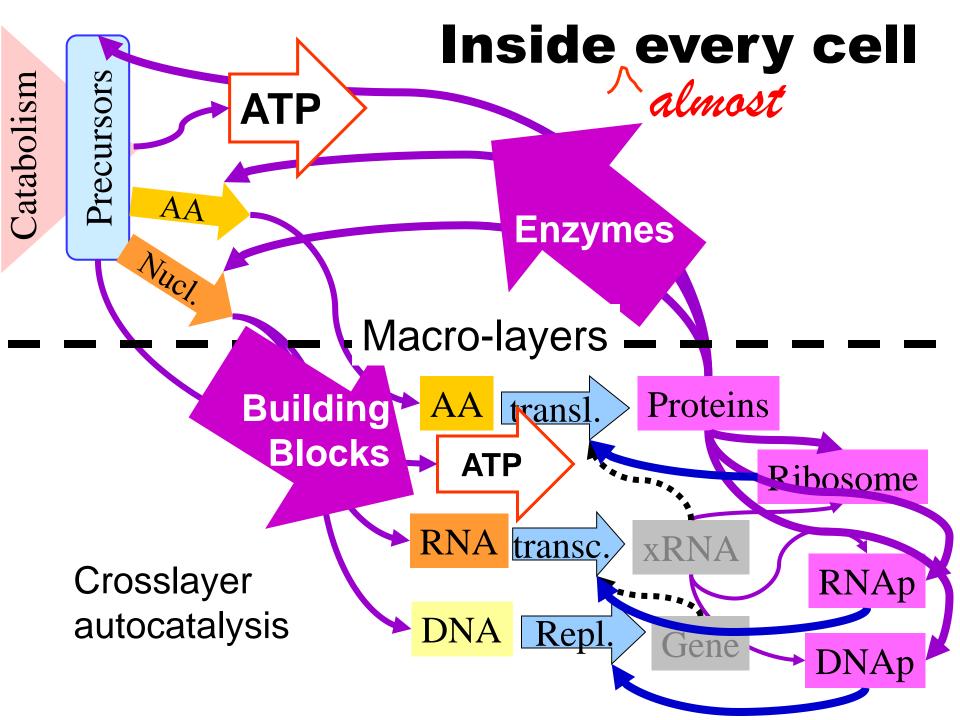
Enzyme amount

#### **Architecture**

Good architectures allow for effective tradeoffs



wasteful



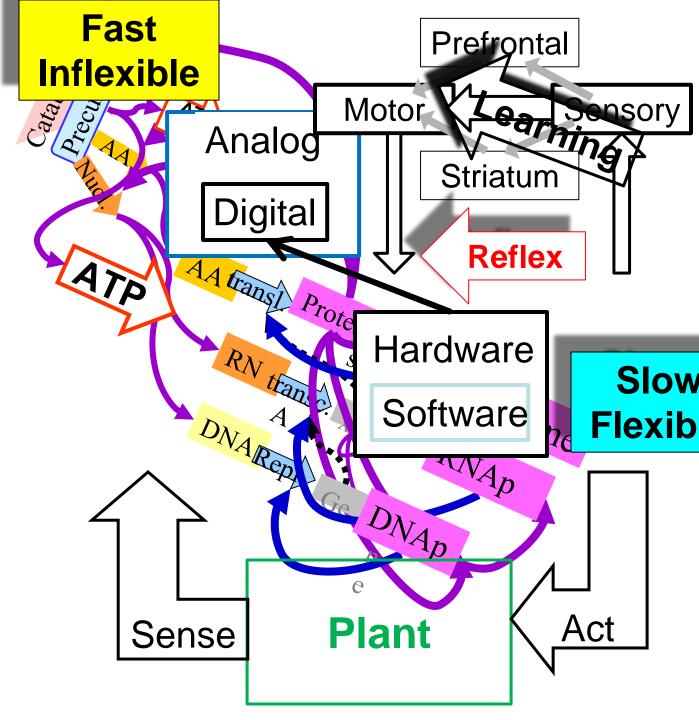
### Compute

**Turing** 

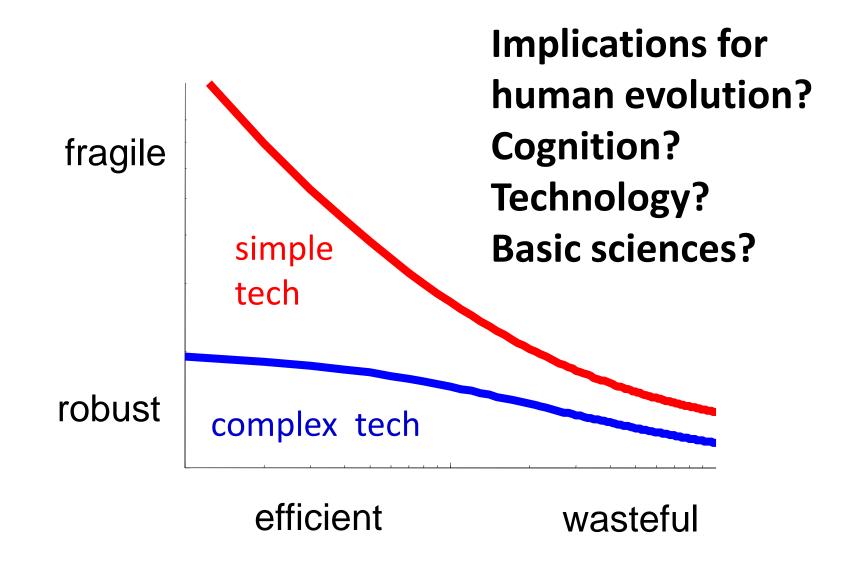
Delay is most important

**Bode** 

**Control** 



#### How general is this picture?



#### Supplementary materials has a demo.

#### Architecture, constraints, and behavior

m

John C. Doyle<sup>a,1</sup> and Marie Csete<sup>b,1</sup>

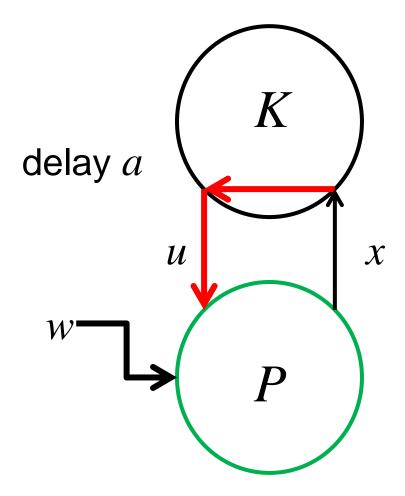
<sup>a</sup>Control and Dynamical Systems, California Institute of Technology, Pasadena, CA 91125; and <sup>b</sup>Department of Anesthesiology, University of California, San Diego, CA 92103

Edited by Donald W. Pfaff, The Rockefeller University, New York, NY, and approved June 10, 2011 (received for review March 3, 201

This paper aims to bridge progress in neuroscience involving sophisticated quantitative analysis of behavior, including the use of robust control, with other relevant conceptual and theoretical frameworks from systems engineering, systems biology, and mathematics. Familiar and accessible case studies are used to illustrate concepts of robustness, organization, and architecture (modularity and protocols) that are central to understanding complex networks. These essential organizational features are hidden during normal function of a system but are fundamental for understanding the nature, design, and function of complex biologic and technologic systems.

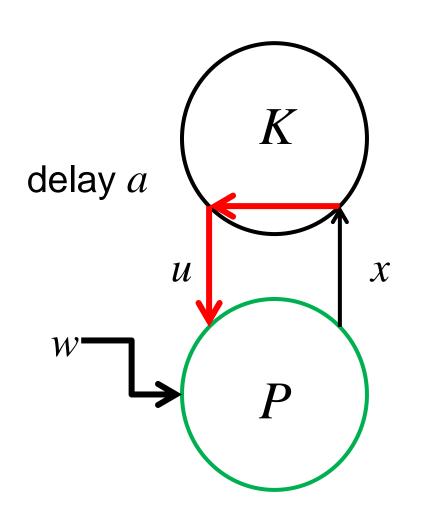
evolved for sensorimotor control and retain mi h of that evolved architecture, then the apparent distinctions be ween perceptual, cognitive, and motor processes may be anoth form of illusion (9), reinforcing the claim that robust con M and adaptive feedback (7, 11) rather than more convent nal serial signal processing might be more useful in interpretical hvsiology data (9). This view also seems broadly arguments from grounded cognition that bodily states, and situated action underly not but cognition in general (12), including language (13). Furthermore, the myriad constraints involved in the evolution of circuit

Doyle and Csete, Proc Nat Acad Sci USA, online JULY 25 2011



$$x_{t+1} = px_t + w_t + u_{t-a}$$

delay a



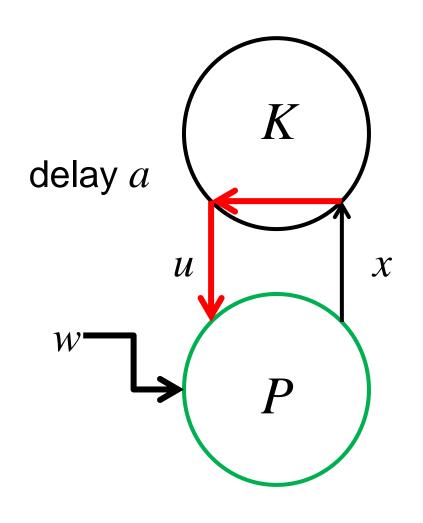
No delay or no uncertainty

$$u_{t-a} = -(px_t + w_t)$$

$$\Rightarrow ||x|| \approx 0 \quad ||u|| \approx ||w||$$

$$x_{t+1} = px_t + w_t + u_{t-a}$$

$$p > 1$$



$$x_{t+1} = px_t + w_t + u_{t-a}$$
$$p > 1$$

No delay or no uncertainty

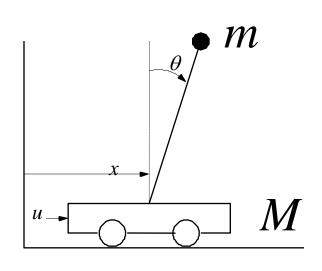
$$u_{t-a} = -(px_t + w_t)$$

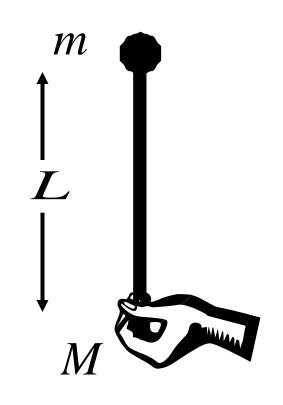
$$\Rightarrow ||x|| \approx 0 \quad ||u|| \approx ||w||$$

With delay *and* uncertainty

$$\Rightarrow \|x\| \approx \|u\| \approx p^a \|w\|$$

# Linearized pendulum on a cart



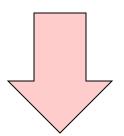


$$\frac{d}{dt} \begin{bmatrix} x \\ \theta \\ \dot{x} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & \frac{m^2 g l^2}{q} & \frac{-(J+ml^2)b}{q} & 0 \\ 0 & \frac{mgl(M+m)}{q} & \frac{-mlb}{q} & 0 \end{bmatrix} x + \begin{bmatrix} 0 \\ 0 \\ J+ml^2 \\ \frac{ml}{q} \end{bmatrix} u$$

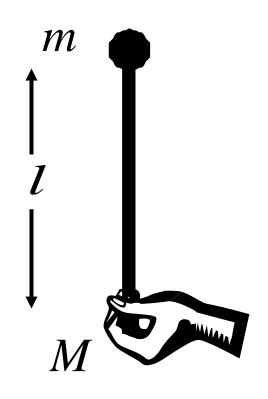
$$q = J(M+m) + Mml^2$$

$$(M + m)\ddot{x} + ml(\ddot{\theta}\cos\theta - \dot{\theta}^2\sin\theta) = u$$
  
$$\ddot{x}\cos\theta + l\ddot{\theta} + g\sin\theta = 0$$
  
$$y = x + \alpha l\sin\theta$$

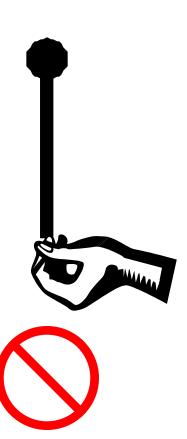


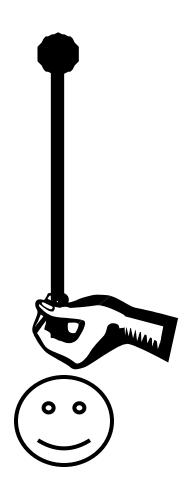


$$(M + m)\ddot{x} + ml\ddot{\theta} = u$$
$$\ddot{x} + l\ddot{\theta} \pm g\theta = 0$$
$$y = x + \alpha l\theta$$



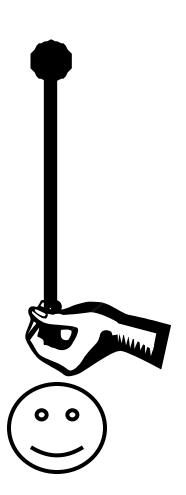
Robust =agile and balancing

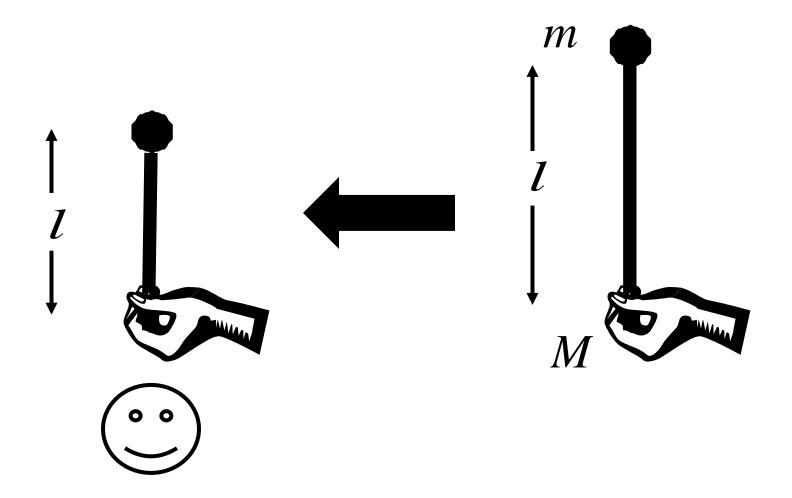




Robust =agile and balancing







Efficient=length of pendulum (artificial)

$$\begin{bmatrix} x \\ \theta \end{bmatrix} = \frac{1}{D(s)} \begin{bmatrix} ls^2 \pm g \\ -s^2 \end{bmatrix} u$$

$$D(s) = s^{2} (Mls^{2} \pm (M + m)g)$$

$$y = x + \alpha l\theta = \frac{\varepsilon l s^2 \pm g}{D(s)}$$

$$\varepsilon = 1 - \alpha$$

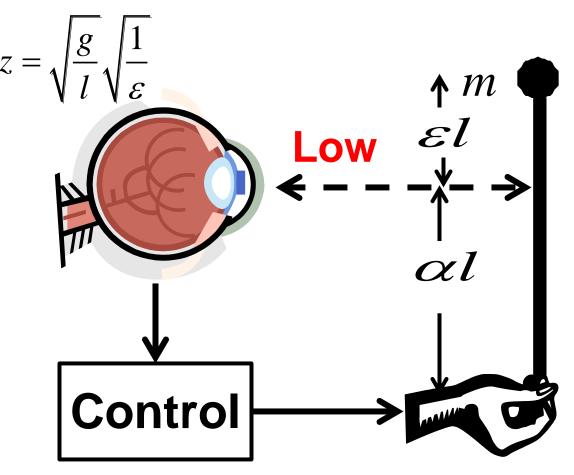
$$p = \sqrt{\frac{g}{l}}\sqrt{1+r} \quad r = \frac{m}{M} \quad z = \sqrt{\frac{g}{l}}\sqrt{\frac{1}{\varepsilon}}$$

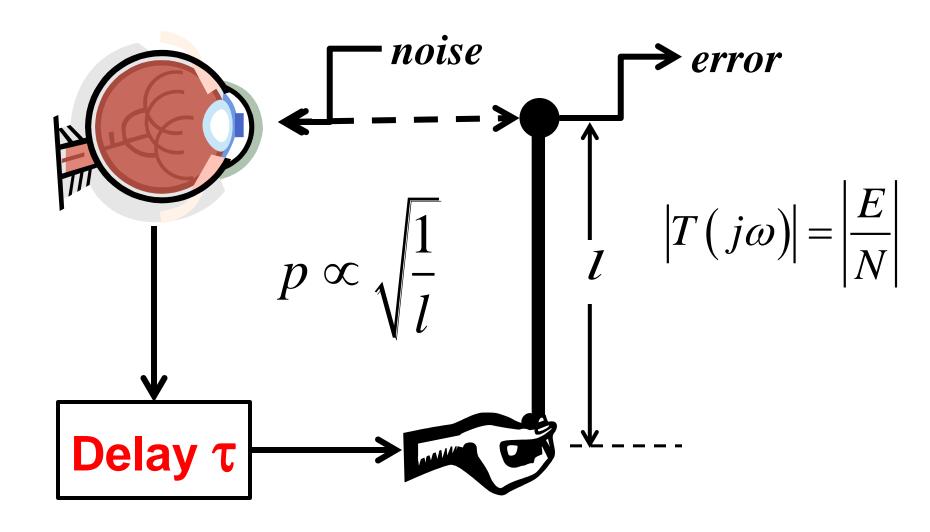


$$(M+m)\ddot{x}+ml\ddot{\theta}=u$$

$$\ddot{x} + l\ddot{\theta} \pm g\theta = 0$$

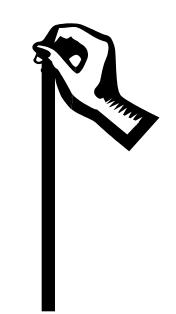
$$y = x + \alpha l\theta$$







$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| d\omega \ge 0$$

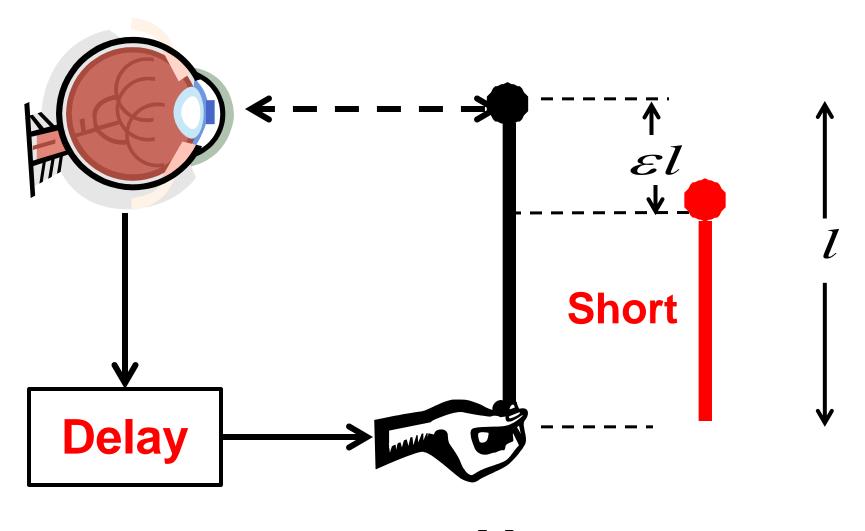


Easy, even with eyes closed No matter what the length

Proof: Standard UG control theory:

Easy calculus, easier contour integral,
easiest Poisson Integral formula

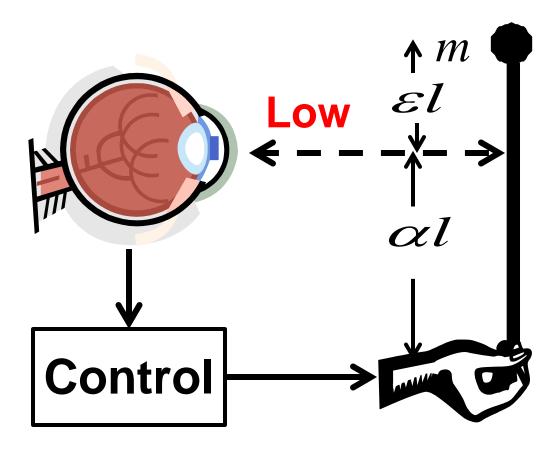
## Harder if delayed or short



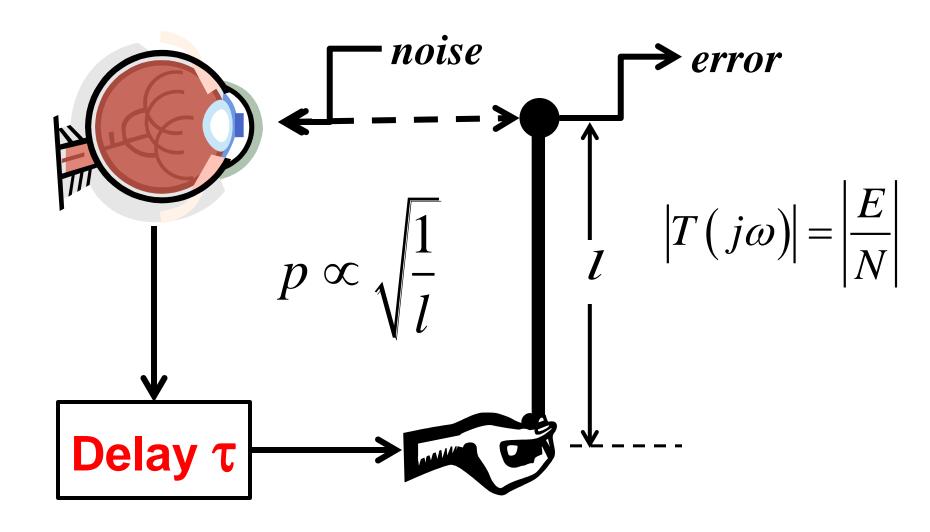
M

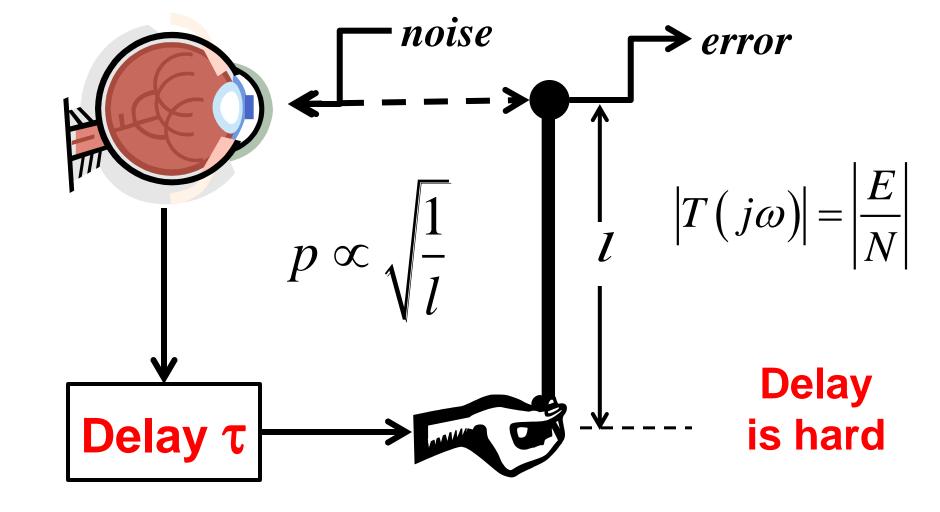
#### Also harder if sensed low

$$r = \frac{m}{M}$$

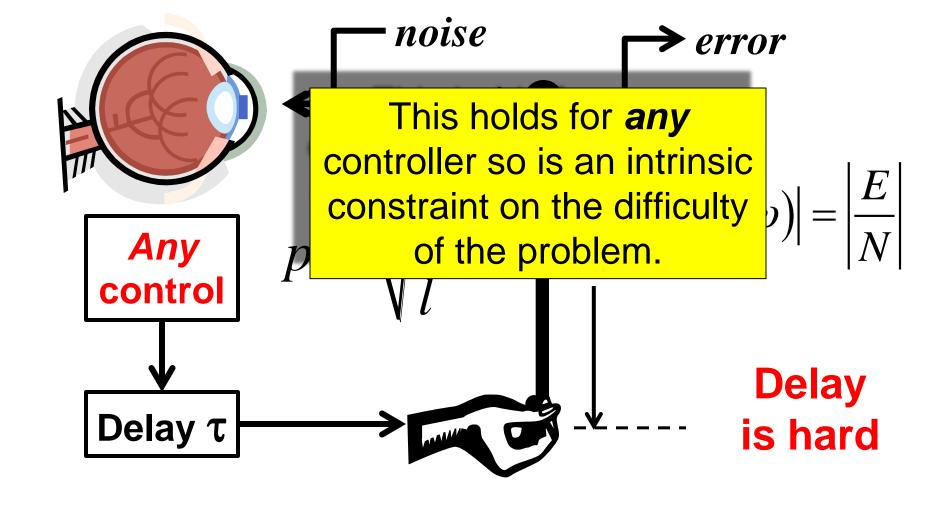








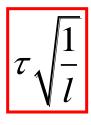
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

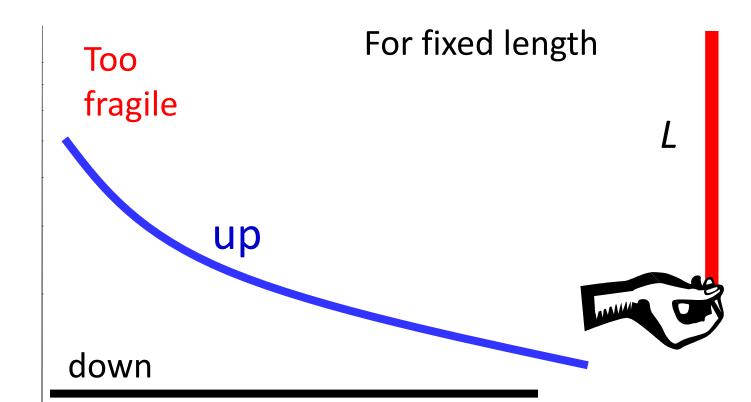


$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge p\tau \propto \tau \sqrt{\frac{1}{l}}$$

Fragility





large τ small 1/τ small τ large 1/τ

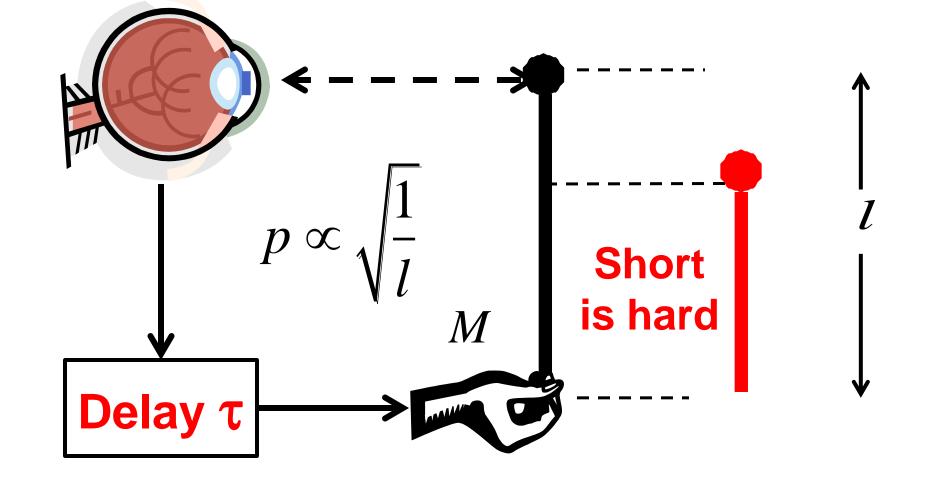
1/delay

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge p\tau \propto \tau \sqrt{\frac{1}{l}}$$

We would like to tolerate large delays (and small lengths), but large delays severely constrain the achievable robustness.

large  $\tau$  small  $1/\tau$ 

small  $\tau$  large  $1/\tau$ 



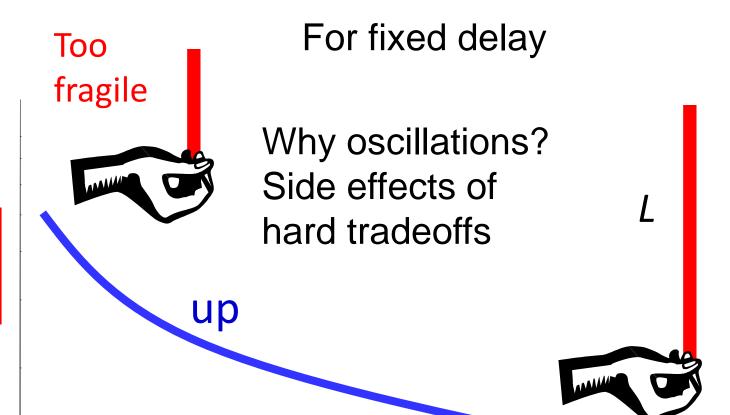
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

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Fragility

$$p \propto \sqrt{\frac{1}{l}}$$

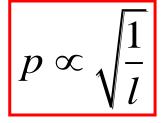
down

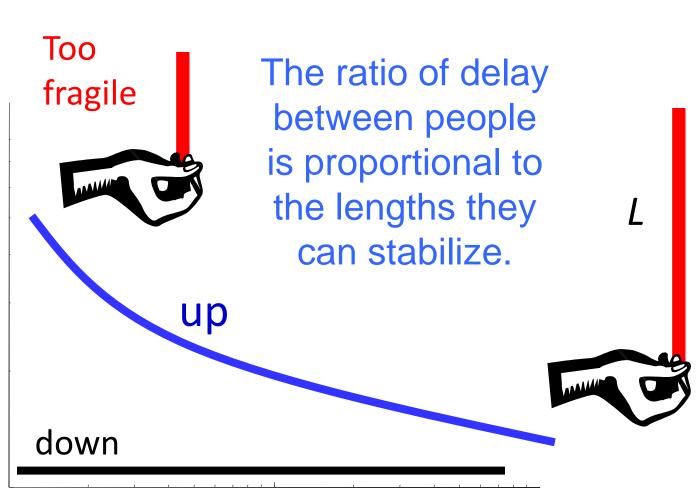


length L

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

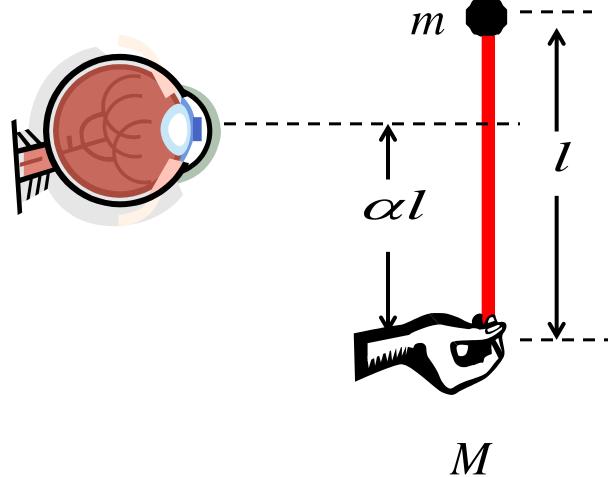




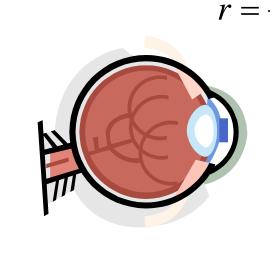


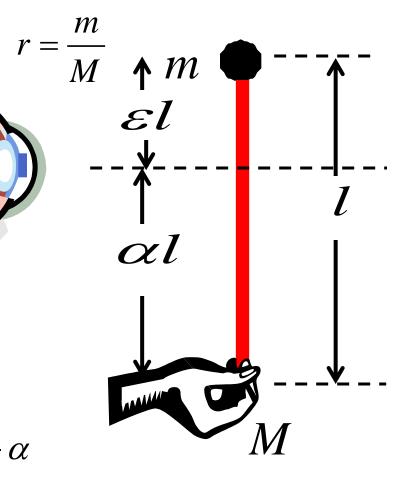
length L

# Eyes moved down is harder (RHP zero) Similar to delay



Suppose 
$$r = \frac{m}{M} << 1$$
  
Units  $\Rightarrow M = g = 1$ 





$$y = x + \alpha l\theta = \frac{\varepsilon l s^2 \pm g}{s^2 (l s^2 \pm g)} \qquad \varepsilon = 1 - \alpha$$

$$p \approx \sqrt{\frac{g}{l}} \qquad z = \sqrt{\frac{g}{l}} \sqrt{\frac{1}{\varepsilon}} \Rightarrow \frac{z + p}{z - p} = \frac{1 + \sqrt{\varepsilon}}{1 - \sqrt{\varepsilon}}$$

#### Compare

$$p = \sqrt{\frac{g}{l(1-\varepsilon)}} \sqrt{1+r} = p_0 \sqrt{\frac{1}{(1-\varepsilon)}} \approx p_0 \left(1 + \frac{\varepsilon}{2}\right)$$

#### Move eyes

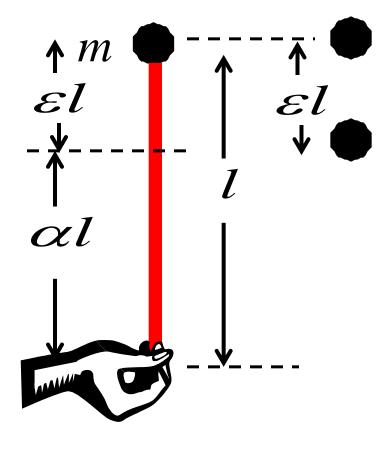
$$p = \sqrt{\frac{g}{l}}\sqrt{1+r} \quad r = \frac{m}{M} \quad z = \sqrt{\frac{g}{l}}\sqrt{\frac{1}{\varepsilon}}$$

$$p = z \Rightarrow 1+r = \frac{1}{\varepsilon} \Rightarrow \varepsilon = \frac{1}{1+r}$$

$$p\left(1+\frac{1}{3}\frac{p^2}{z^2}\right) = \sqrt{\frac{g}{l}}\sqrt{1+r}\left(1+\frac{1}{3}\varepsilon\right) = p\left(1+\frac{\varepsilon}{3}\right)$$

$$= p\left(1+\frac{1-\alpha}{3}\right)$$

$$r = \frac{m}{M}$$



M

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \left(\frac{2p}{p^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$

$$\varepsilon = \frac{1}{1 + r}$$

$$\ln \left|\frac{z + p}{z - p}\right|$$

$$\frac{z + p}{z - p} = \frac{1 + \sqrt{\varepsilon}}{1 - \sqrt{\varepsilon}}$$

$$\frac{z + p}{z - p} = \frac{1 + \sqrt{\varepsilon}}{1 - \sqrt{\varepsilon}}$$

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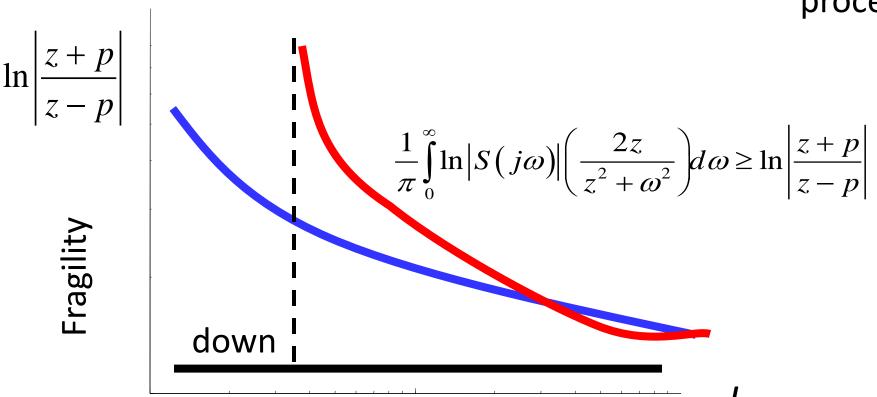
$$\frac{z + p}{z - p} = \frac{1 + \sqrt{\varepsilon}}{1 - \sqrt{\varepsilon}}$$

$$\frac{z + p}{z - p} = \frac{1 + \sqrt{\varepsilon}}{$$

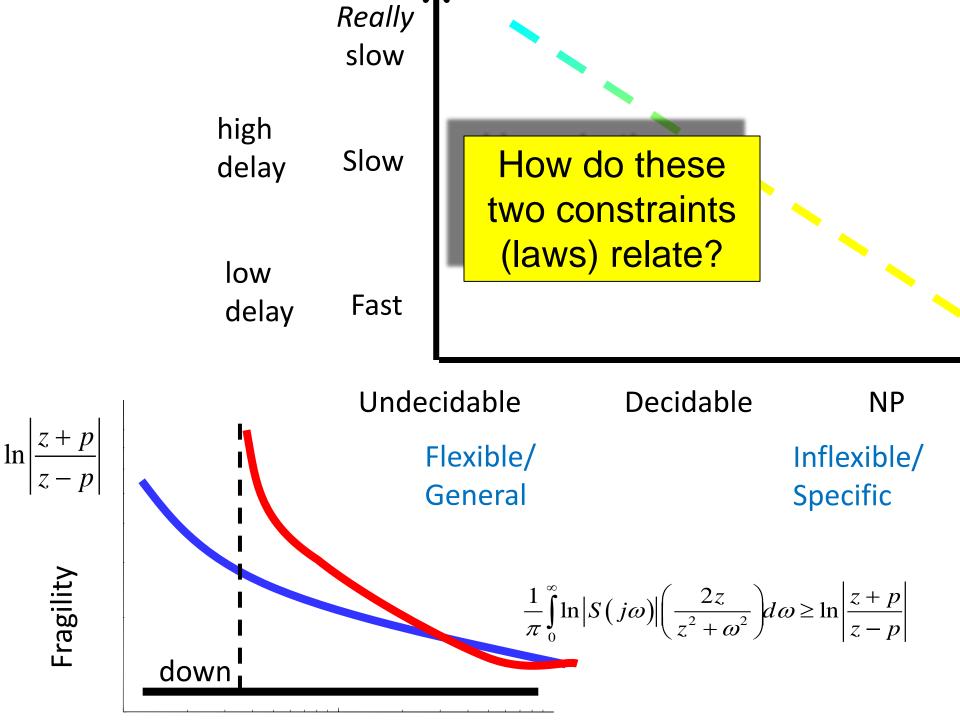
 $\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{2z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$ 

Hard limits on the *intrinsic* robustness of control *problems*.

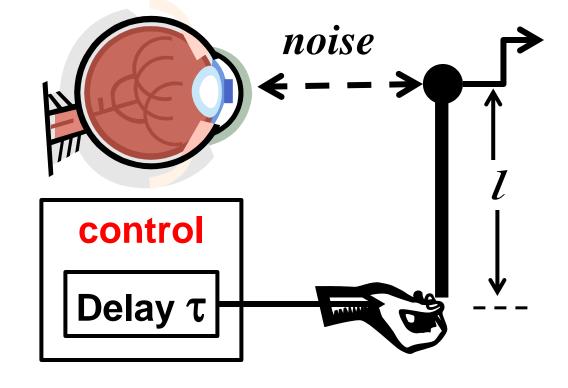
Must (and do) have algorithms that achieve the limits, and architectures that support this process.



This is a cartoon, but can be made precise.



Delay comes from sensing, communications, computing, and actuation.
Delay limits robust performance.

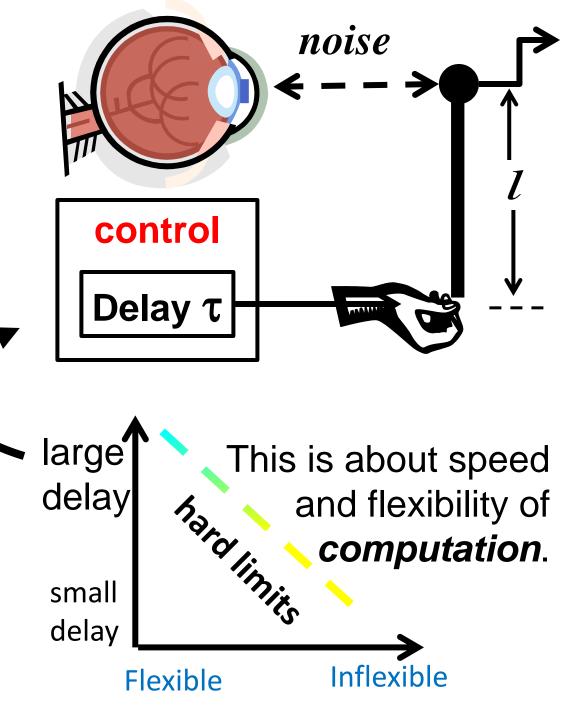


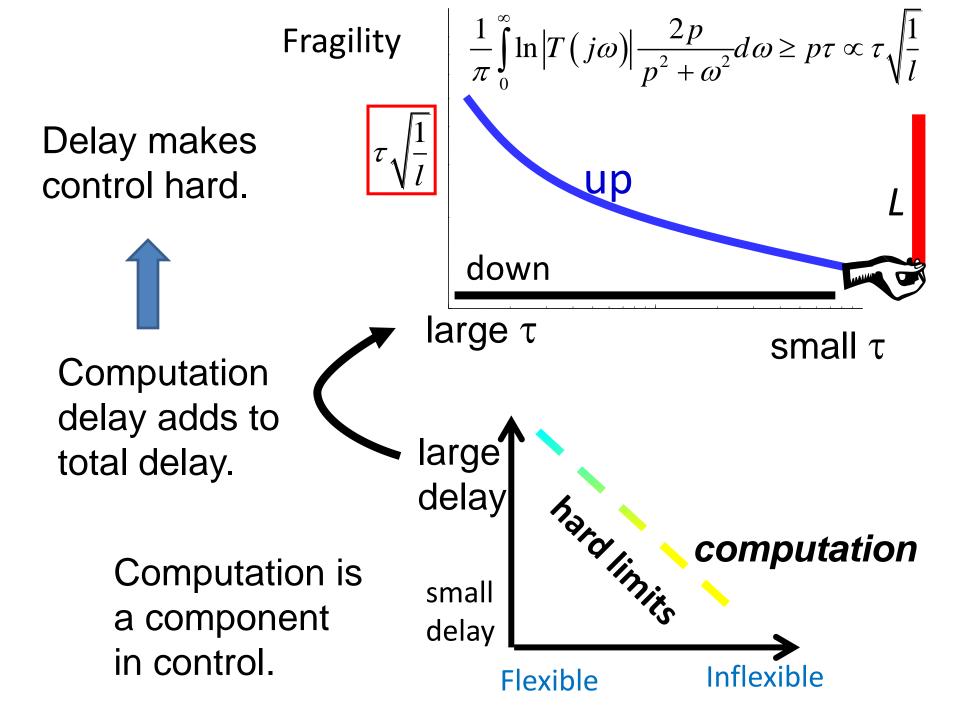
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

How do these two constraints (laws) relate?

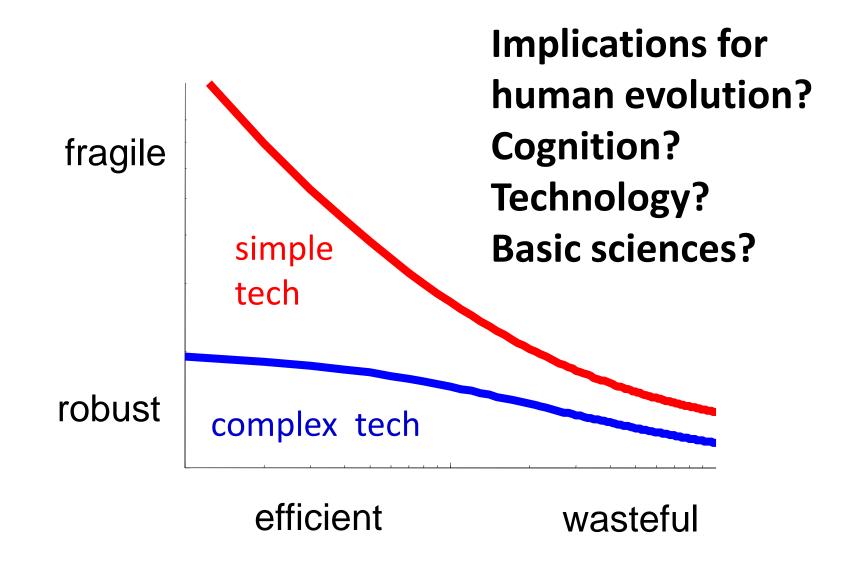
Computation delay adds to total delay.

Computation is a component in control.





#### How general is this picture?



# Next (and last) time

- Universal laws in more depth
- Universal architectures revisited/compared
  - Computers and networks
  - Cells
  - Brains and minds
- Architecture & laws at the extremes
  - evolution
  - eusociality

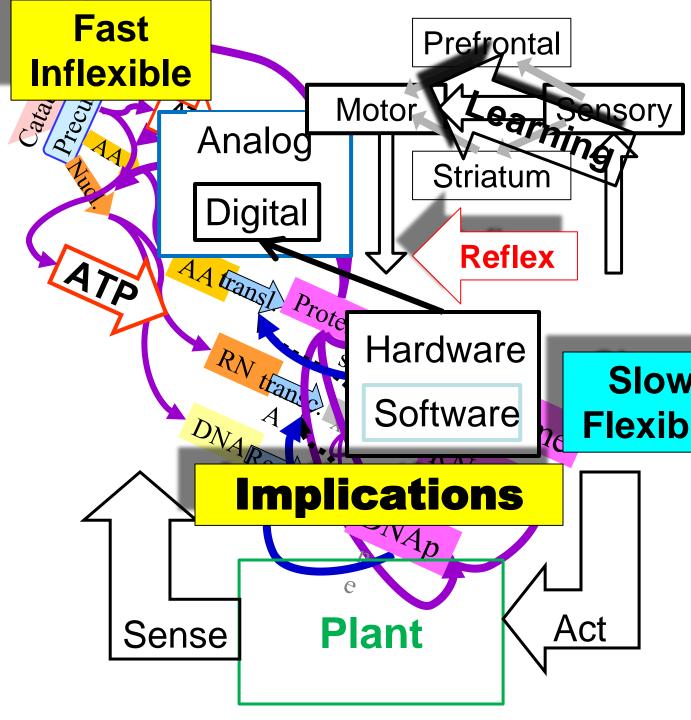
# Compute

**Turing** 

Delay is most important

**Bode** 

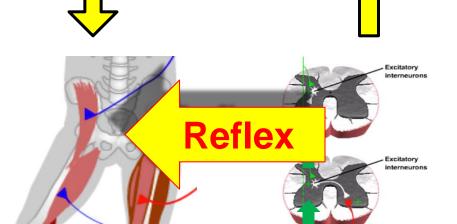
**Control** 



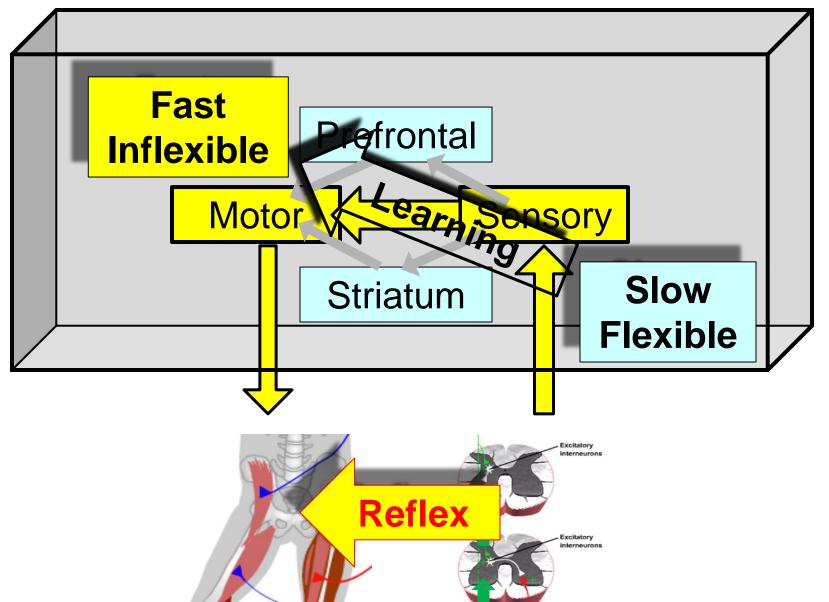


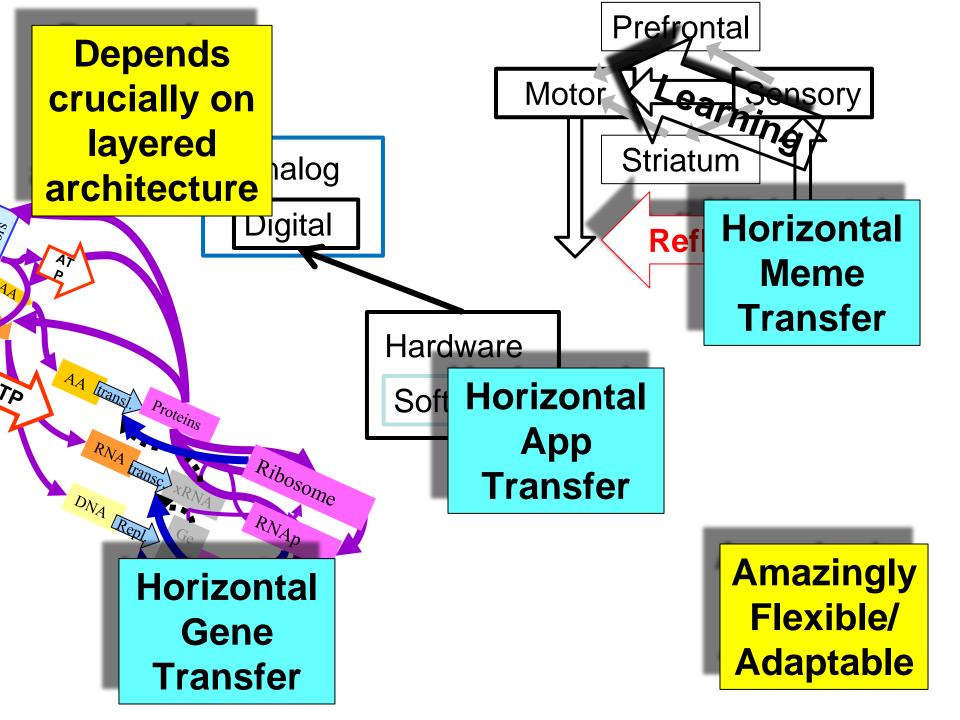
Brain as optimal controller

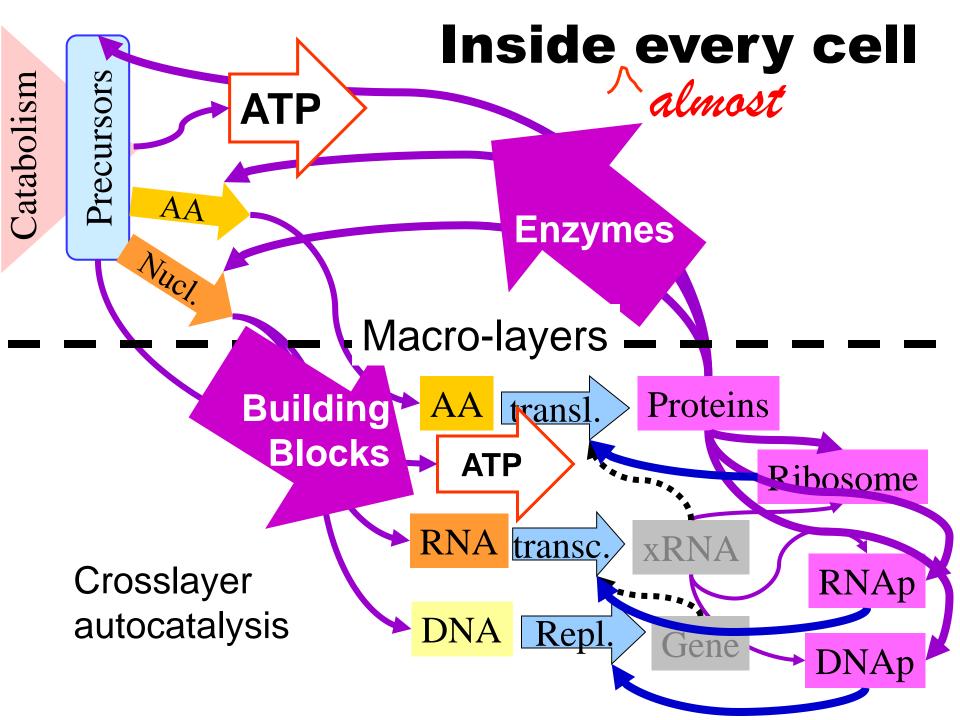
- Acquire
- Translate/ integrate
- Automate



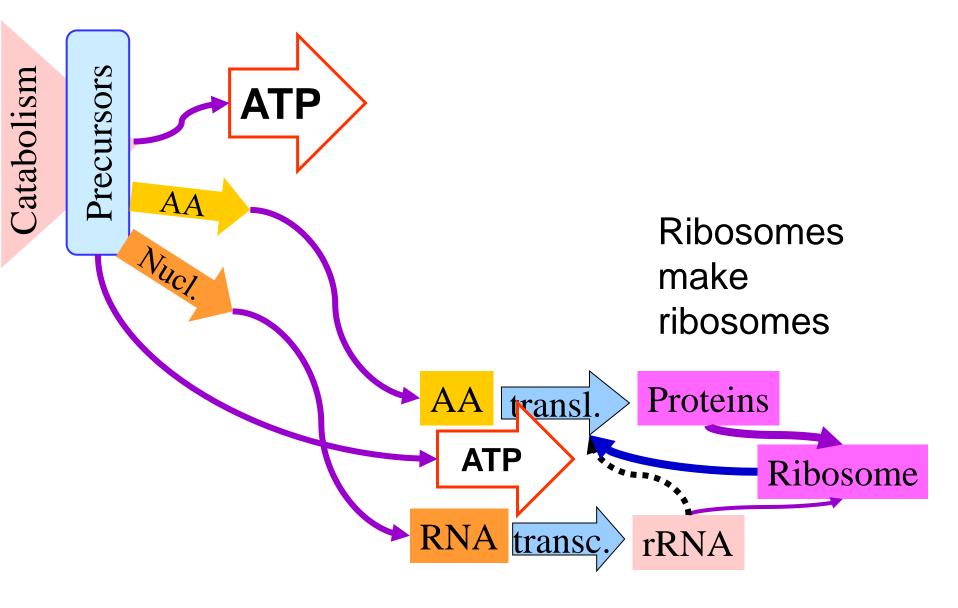
# Going beyond black box: control is decentralized with internal delays.







Translation: Amino acids polymerized into proteins



Ribosomes are made of proteins and RNA

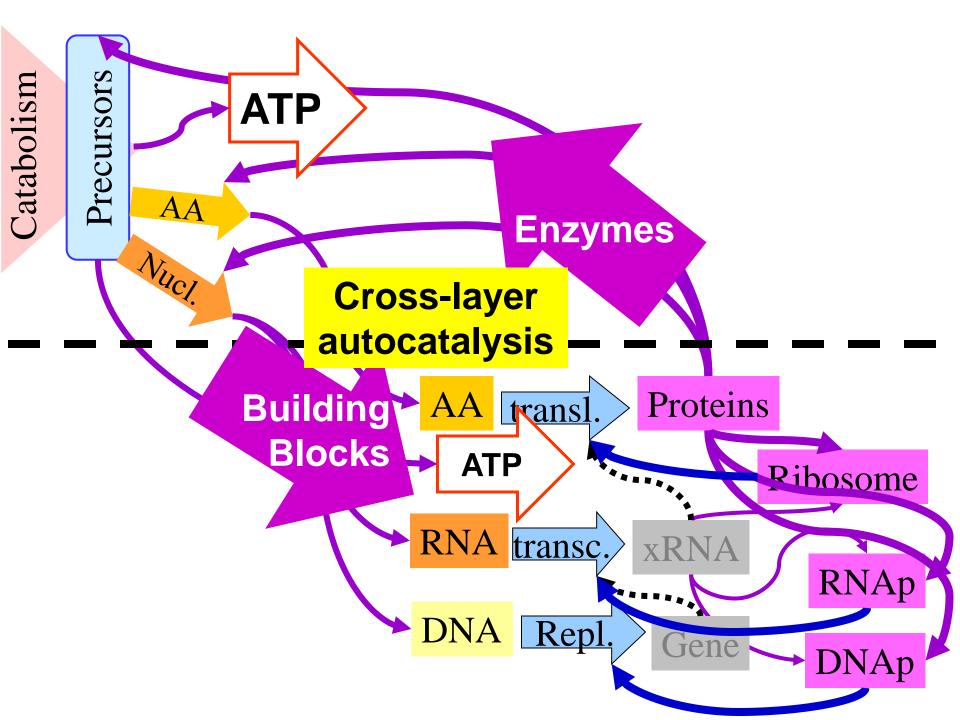
Ribosomes make ribosomes

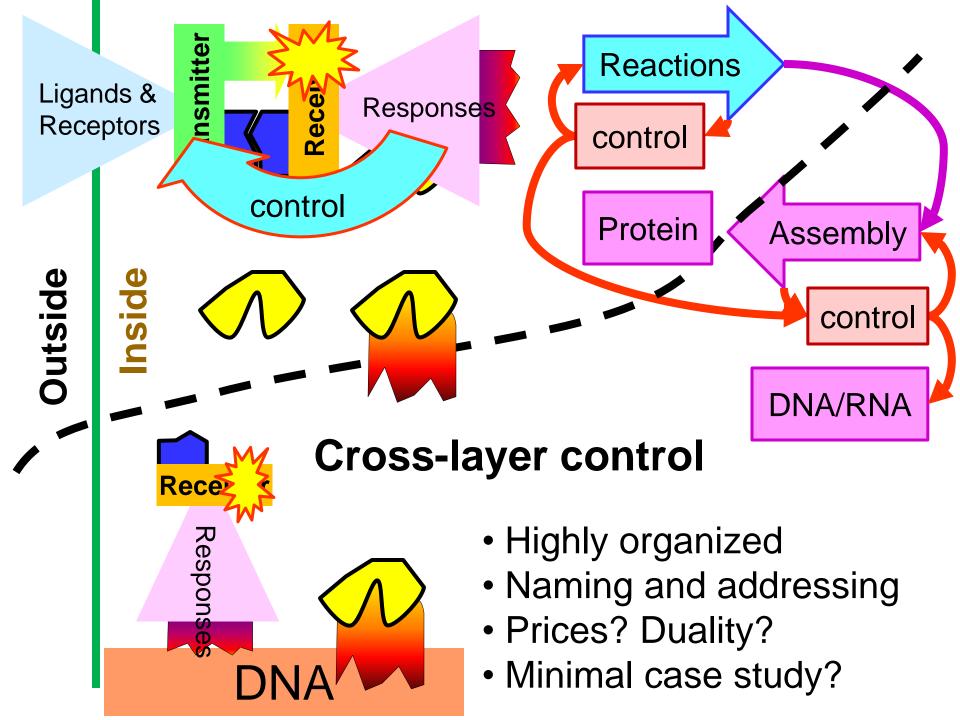
**Autocatalytic** 

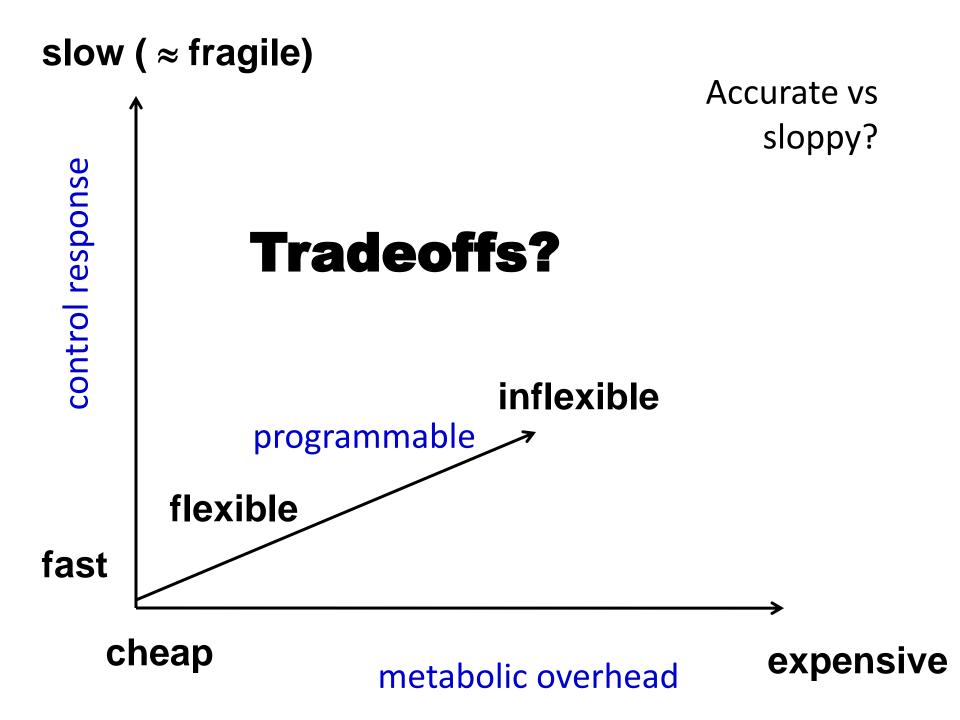
RNA transc. rRNA

Organisms differ in the proportion of ribosomal protein vs rRNA

Ribosomes are made of proteins and rRNA







## Evolution and architecture

Nothing in biology makes sense except in the light of evolution

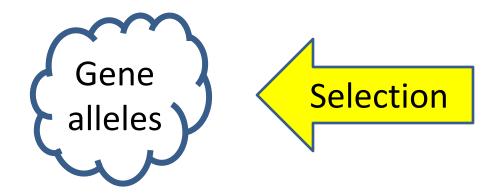
Theodosius Dobzhansky (see also de Chardin)

Nothing in evolution makes sense except in the light of biology

**55555** 

Standard theory:
natural selection + genetic drift
+ mutation + gene flow

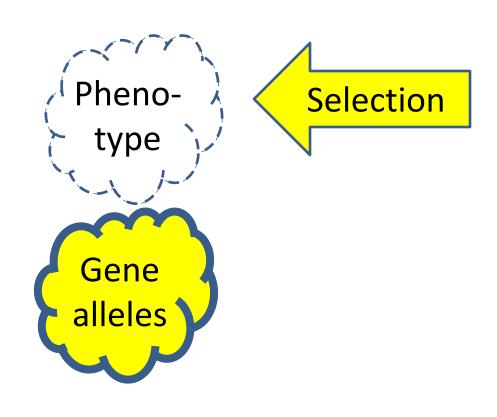
Greatly abridged cartoon here



Shapiro explains well what this is and why it's incomplete (but Koonin is more mainstream)

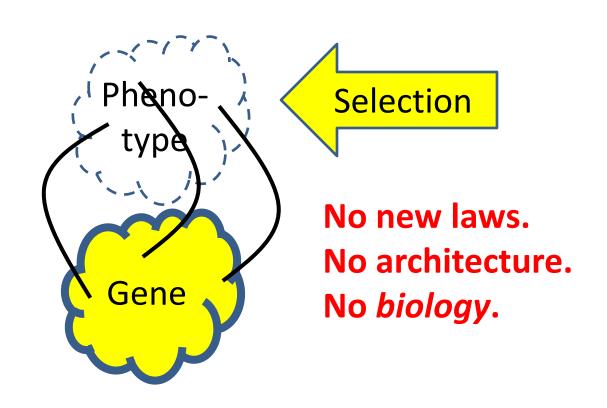
### Standard theory:

selection + drift + mutation + gene flow

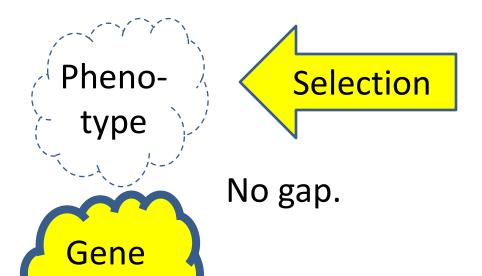


### Standard theory:

selection + drift + mutation + gene flow



selection + drift + mutation + gene flow



alleles

All complexity is emergent from random ensembles with minimal tuning.

No new laws.

No architecture.

### The battleground



Phenotype

Gene
alleles

No gap. Just physics.

Huge gap.
Need
supernatural



Genes?

### What they agree on

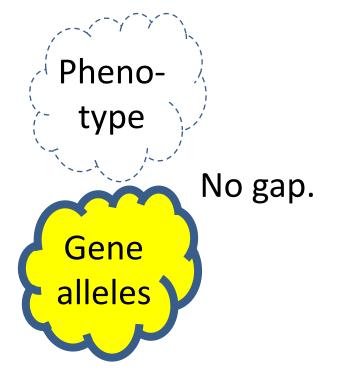
No new laws. No architecture. No biology.



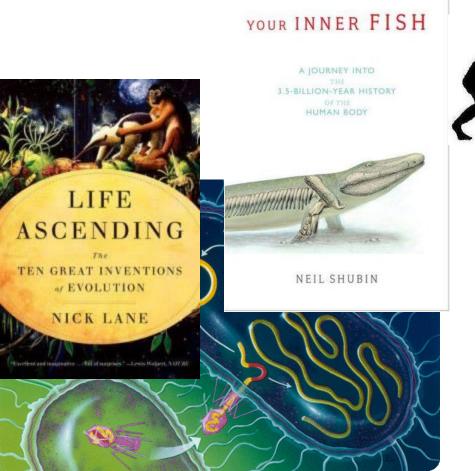
Huge gap.



Genes

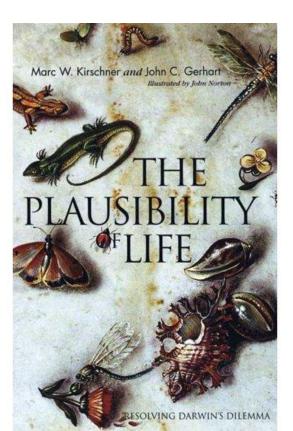


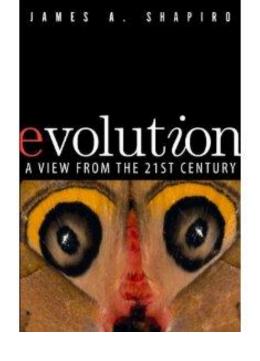
## Putting biology back into evolution

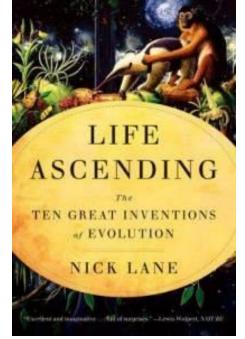


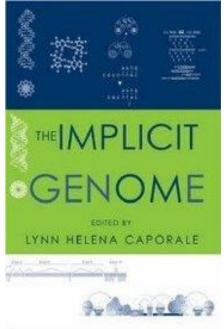


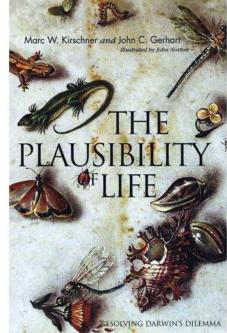










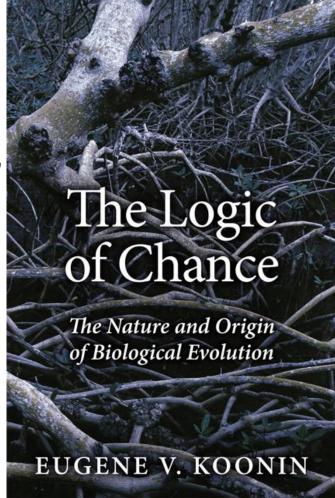


#### The heresies

- Many mechanisms for "horizontal" gene transfer
- Many mechanisms to create large, functional mutations
- At highly variable rate, can be huge, global
- Selection alone is a very limited filtering mechanism
- Mutations can be "targeted" within the genomes
- Can coordinate DNA change w/ useful adaptive needs
- Viruses can induce DNA change giving heritable resistance
- Still myopic about future, still produces the grotesque

THE
SOCIAL
CONQUEST
OF EARTH

Surprising heresies from "conservatives"



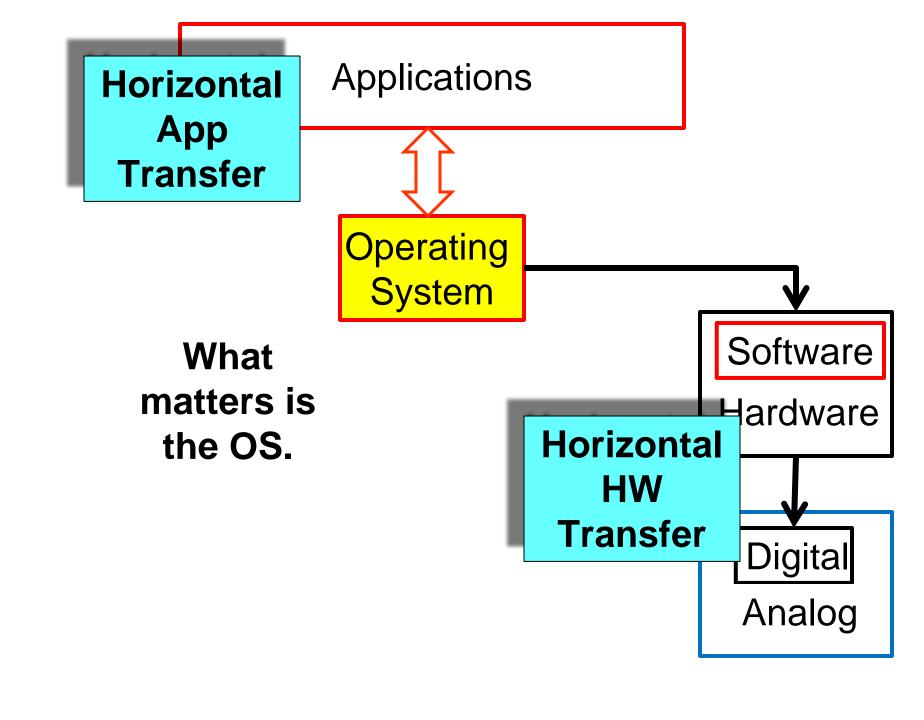


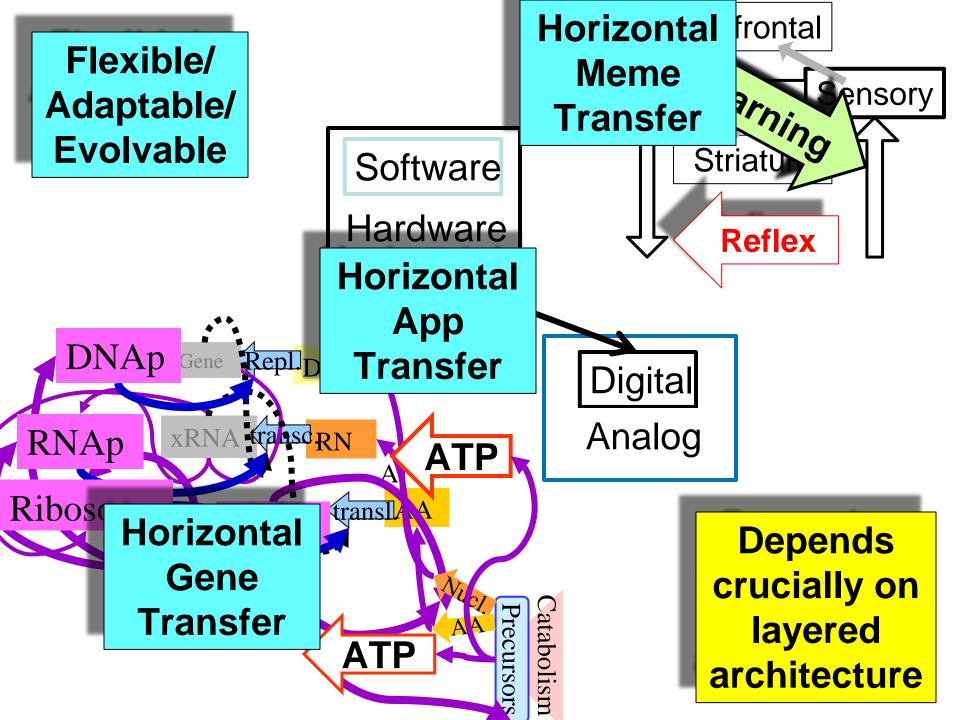
EDWARD O. WILSON

WINNER of the PULITZER PRIZE



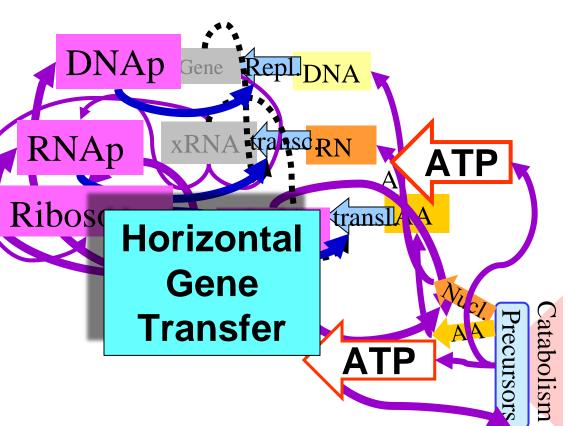






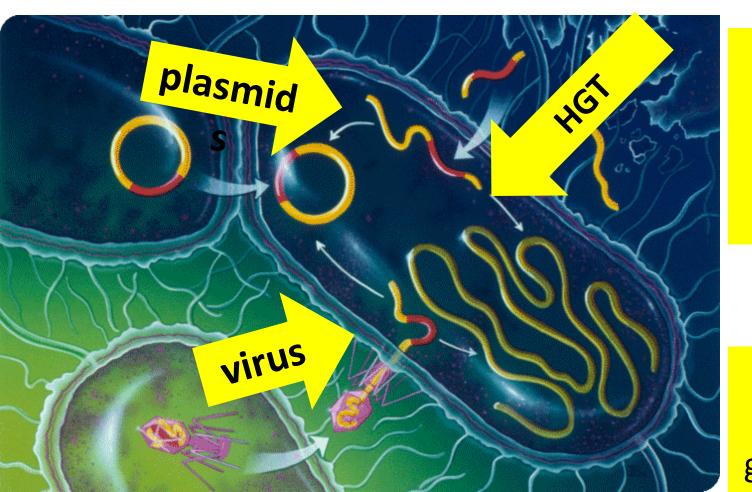
### Sequence ~100 E Coli (not chosen randomly)

- ~ 4K genes per cell
- ~20K different genes in total
- ~ 1K universally shared genes



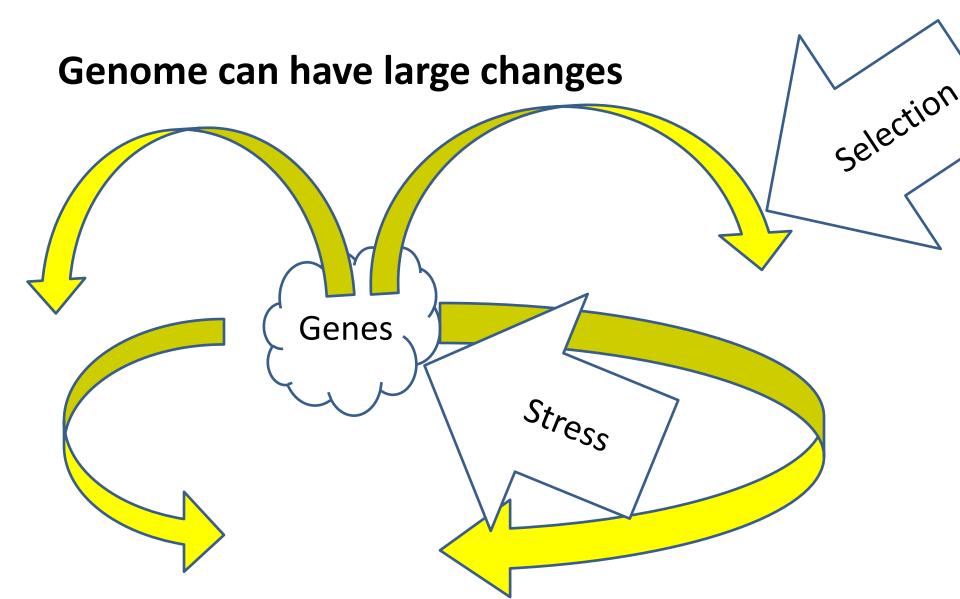
See slides on microbial biosphere laws and architectures.

# selection + drift + mutation + gene flow + facilitated *variation*

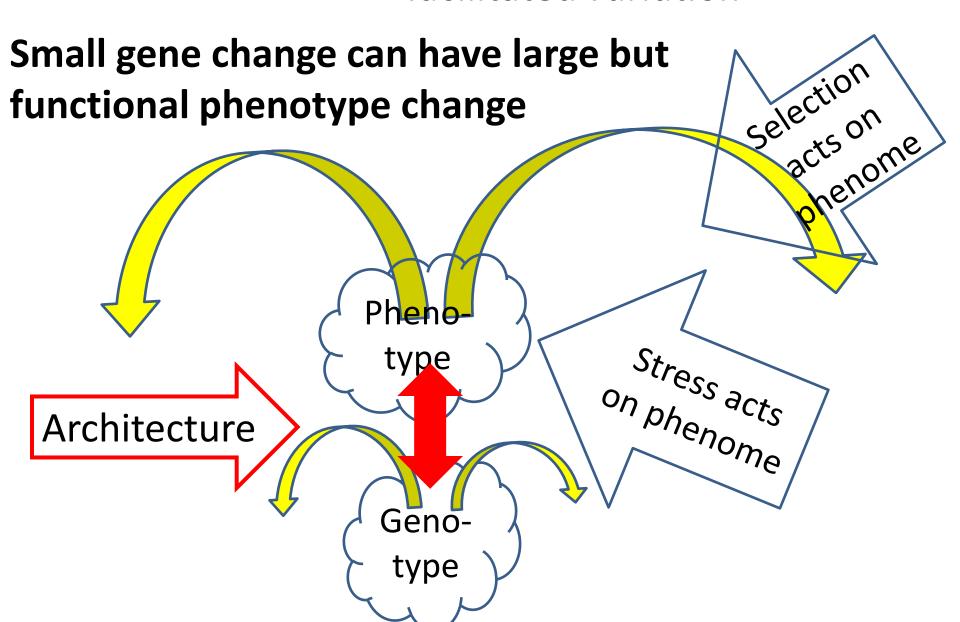


large functional changes in genomes

HGT = horizontal gene transfer natural selection + genetic drift + mutation + gene flow + facilitated *variation* 

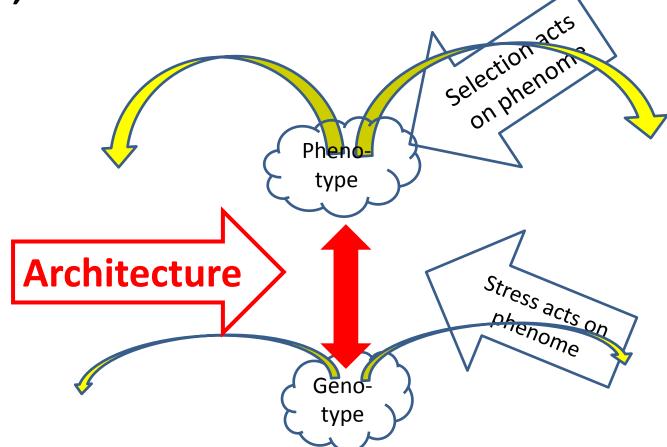


natural selection + genetic drift + mutation + gene flow + facilitated variation



natural selection + genetic drift + mutation + gene flow + facilitated variation

Only possible because of shared, layered, network architecture



### Reading?

- See refs in 2011 PNAS paper but also...
- Turing: Gallistel (+ Wolpert on control/bayes)
- Brain/Mind: Gazzaniga, Kahneman + Reyna/Brainerd, Ashby, Cosmides/Tooby,...
- Evolution: Gerhart & Kirschner, Shapiro, Lane, Koonin, Caporale (+ fire + running)
- Apes: De Waal (Bonobos), Sapolsky (Baboons)
- Eusociality: Wilson
- Juarrero